

**IRSN**

INSTITUT  
DE RADIOPROTECTION  
ET DE SÛRETÉ NUCLÉAIRE

# USE OF FISSION PRODUCT EXPERIMENTS FOR BURNUP CREDIT VALIDATION

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International Workshop on Advances in Applications of Burnup Credit for  
Spent Fuel Storage, Transport, Reprocessing, and Disposition

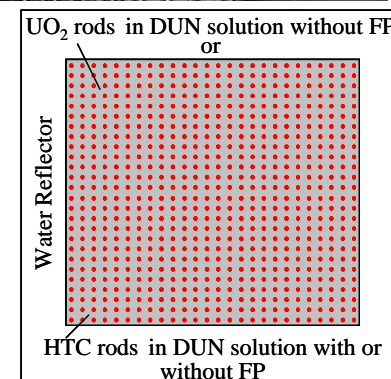
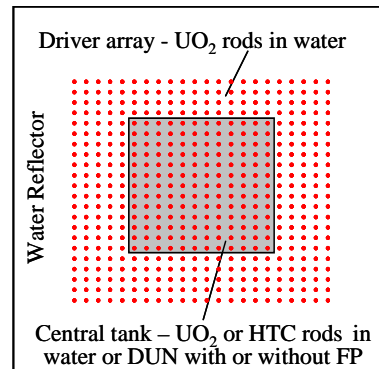
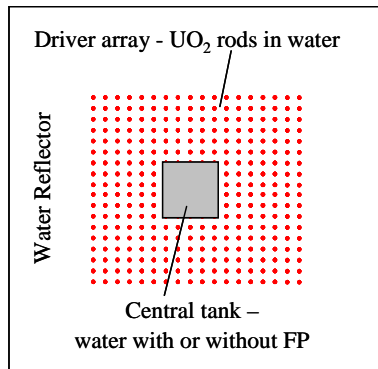
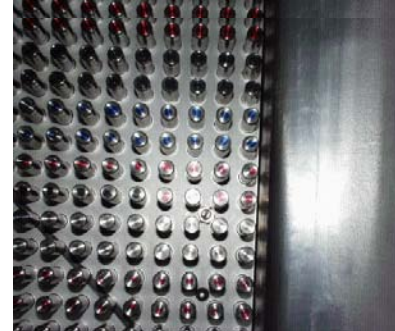
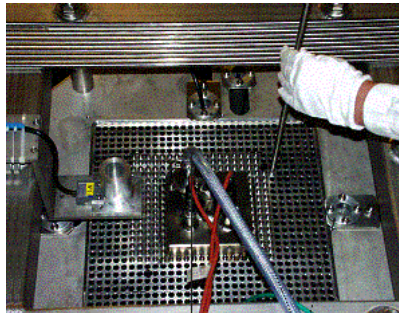
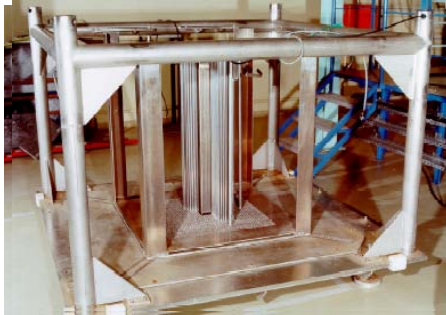
October 28, 2009 Cordoba, Spain

# Outline

- French Fission Product (FP) Experimental Program
- Modification to the adjustment technique to establish bias and bias uncertainty due to FPs
- FP credit validation for application systems of the present and future fuel cycle
- Summary

# French FP Experimental Program

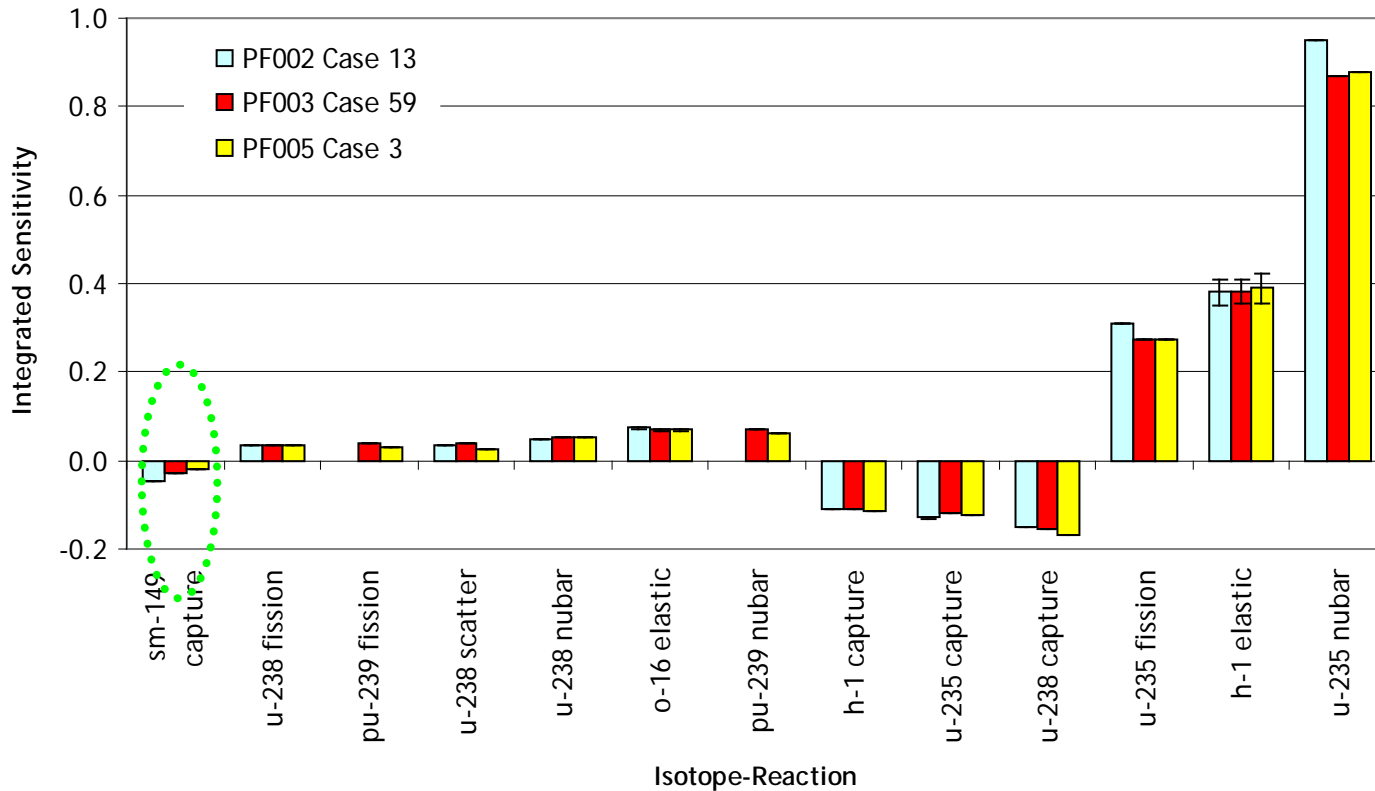
Series of 145 critical experiments referred to as the FP Experimental Program was performed in the Valduc facility (CEA, France) in 1998-2004 [Ref.] with **Cs-133, Sm-149, Sm-152, Gd-155, Ph-103, and Nd-143** in solutions



a) “Physical”    b) “Elementary Dissolution”    c) “Global Dissolution”

[Ref.] N. Leclaire et al., “Fission Products Experimental Programme: Validation and Computational Analysis”, *Nucl. Sci. Eng.*, **161**, 2, pp. 188-215 (2009)

# Sensitivity Comparison: an Example



$k_{\text{eff}}$  sensitivity\* to FP are significantly smaller than sensitivities for major actinides and moderator materials

\*Sensitivity coefficients calculated by TSUNAMI-3D code/ 44-group ENDF/B-V based library

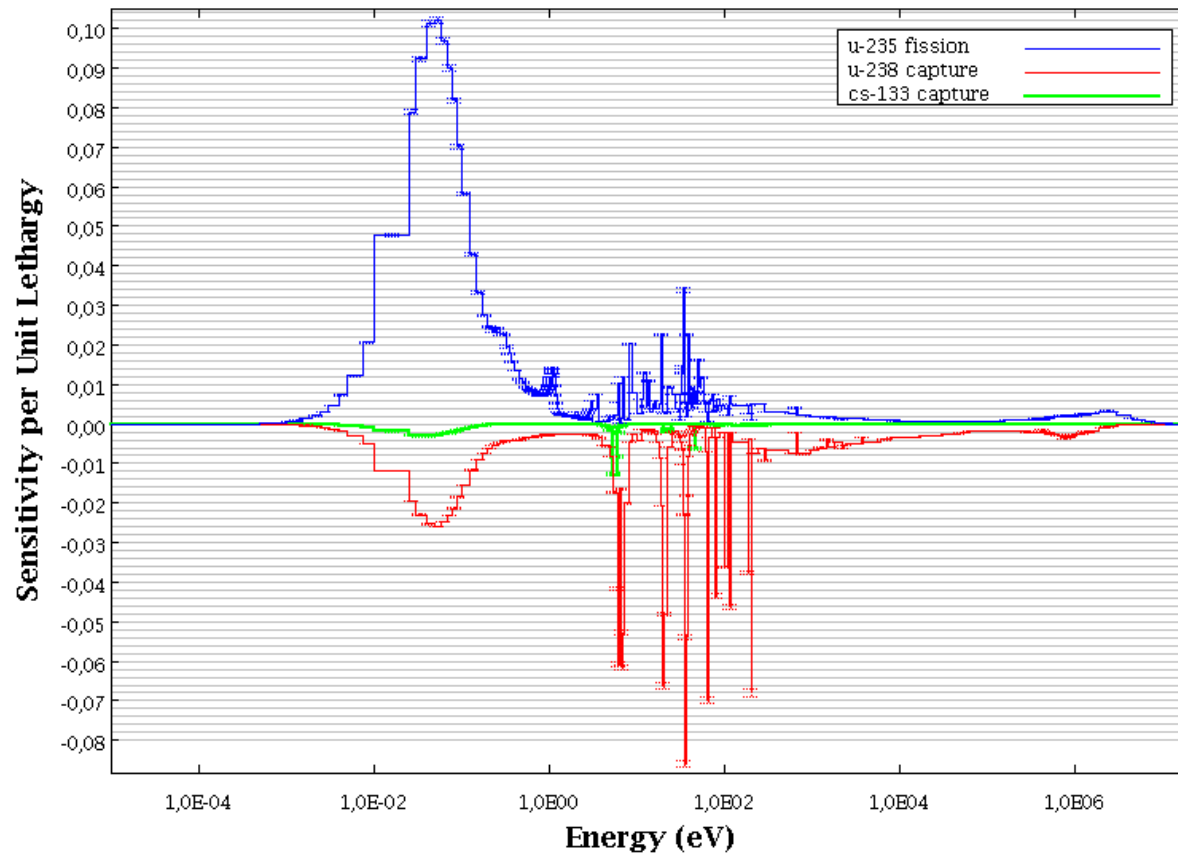
# Analysis of the FP Experiments: an Example (1/3)

## Some Physical Type Configurations

| Exp. | No. | FP                | C(FP) g/l | r (g/cm <sup>3</sup> ) | H <sup>+</sup> (N) | Array    | Number of rods | Number of rods removed | °C   | Hc (mm) |
|------|-----|-------------------|-----------|------------------------|--------------------|----------|----------------|------------------------|------|---------|
| 2834 | 2   | <sup>103</sup> Rh | 40        | 1.0916                 | 0.97               | 25x25-25 | 600            | 0                      | 19.9 | 600     |
| 2835 | 3   | <sup>103</sup> Rh | 20        | 1.0454                 | 0.49               | 25x25-25 | 600            | 0                      | 20.3 | 530     |
| 2811 | 8   | <sup>133</sup> Cs | 130       | 1.1383                 | 0.014              | 25x25-25 | 600            | 0                      | 20   | 540     |
| 2809 | 11  | <sup>133</sup> Cs | 80        | 1.0809                 | 0.014              | 25x25-25 | 600            | 0                      | 20   | 520     |
| 2812 | 13  | <sup>133</sup> Cs | 80        | 1.1483                 | 2.04               | 25x25-25 | 600            | 0                      | 19.5 | 521     |
| 2817 | 14  | <sup>133</sup> Cs | 78        | 1.1463                 | 2                  | 25x25-25 | 600            | 0                      | 19   | 521     |
| 2821 | 16  | Ndnat             | 120       | 1.2224                 | 0.023              | 25x25-25 | 600            | 0                      | 19   | 540     |
| 2823 | 18  | <sup>152</sup> Sm | 50        | 1.088                  | 0.011              | 25x25-25 | 600            | 0                      | 19   | 700     |
| 2844 | 28  | Mixt.             |           | 1.0989                 | 0.21               | 25x25-25 | 600            | 0                      | 20   | 600     |
| 2803 | 35  | Water             |           | 0.9986                 | 0.014              | 25x25-25 | 600            | 0                      | 19.4 | 460     |
| 2813 | 37  | Water             |           | 0.9986                 | 0.014              | 25x25-25 | 600            | 0                      | 19.4 | 460     |

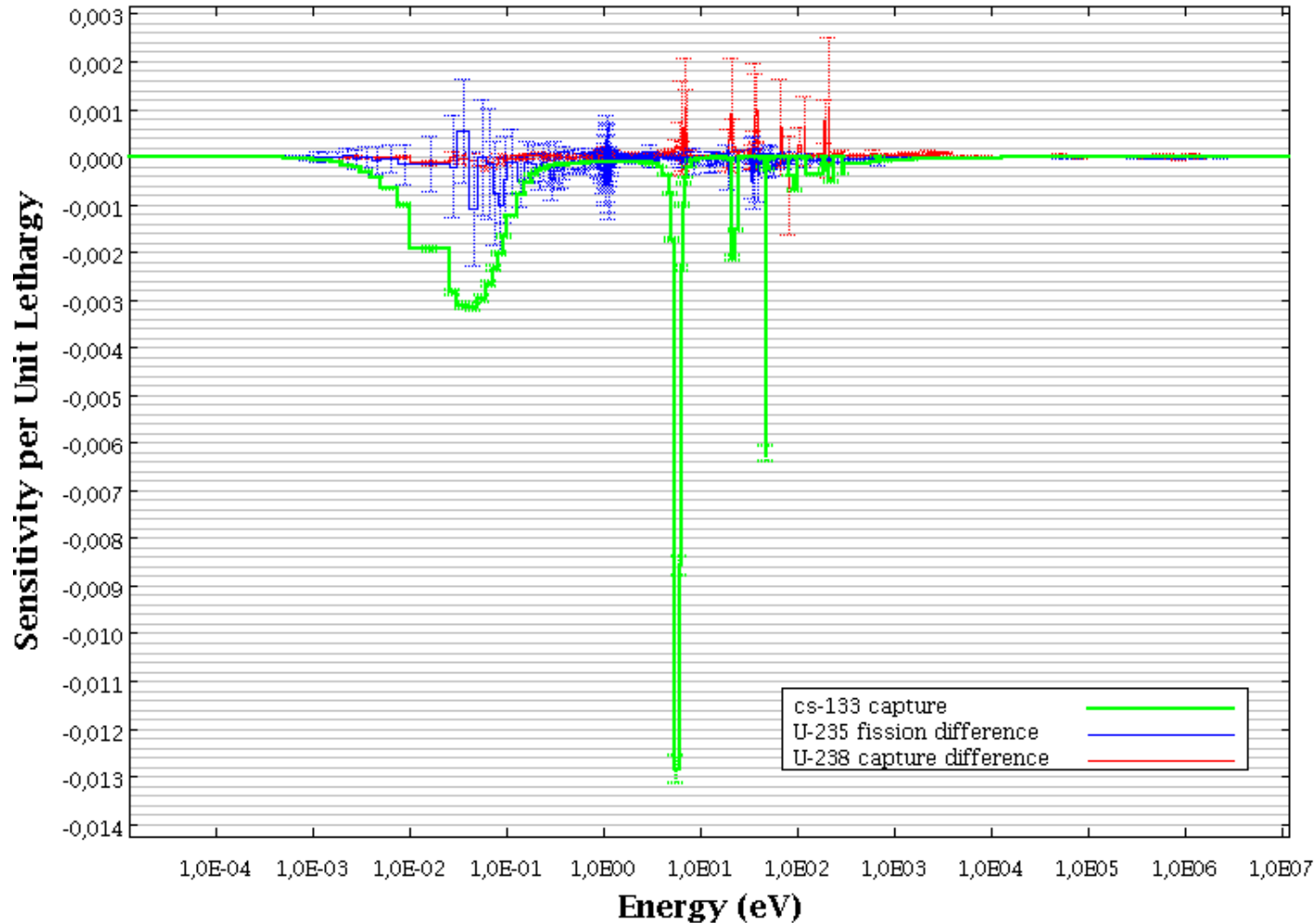
# Analysis of the FP Experiments: an Example (2/3)

Some  $k_{eff}$  sensitivity profiles for configuration #2809 with  $^{133}\text{Cs}$



# Analysis of the FP Experiments: an Example (3/3)

Some  $k_{eff}$  difference sensitivity for configurations with (#2809) and without (#2803)  $^{133}\text{Cs}$



## Basic Equations for the “Adjustment” Method

$$\mathbf{S}^2 = \mathbf{P}^t \mathbf{W}^{-1} \mathbf{P} + (\Delta \mathbf{k} - \mathbf{H} \mathbf{P})^t \mathbf{U}^{-1} (\Delta \mathbf{k} - \mathbf{H} \mathbf{P})$$

$$\mathbf{P} = (\mathbf{W}^{-1} + \mathbf{H}^t \mathbf{U}^{-1} \mathbf{H})^{-1} \mathbf{H}^t \mathbf{U}^{-1} \Delta \mathbf{k}$$

$$\mathbf{W}' = (\mathbf{W}^{-1} + \mathbf{H}^t \mathbf{U}^{-1} \mathbf{H})^{-1}$$

**Bias for Application System =  $\mathbf{D} \mathbf{P}$**

**Bias Uncertainty for Application System =  $\mathbf{D} \mathbf{W}' \mathbf{D}^t$**

W - ND covariances

U - Experimental uncertainty correlation

H -  $k_{\text{eff}}$  Sensitivities for experiments

D -  $k_{\text{eff}}$  Sensitivities for application systems

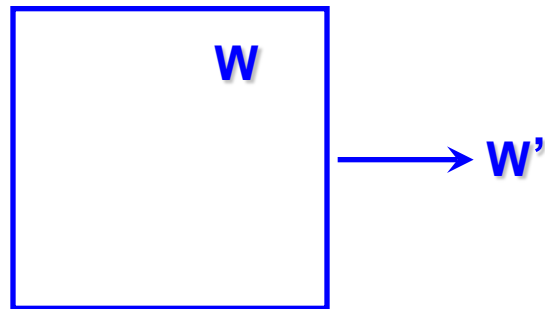
P - vector of corrections to cross sections

$\Delta K = k_c - k_e$



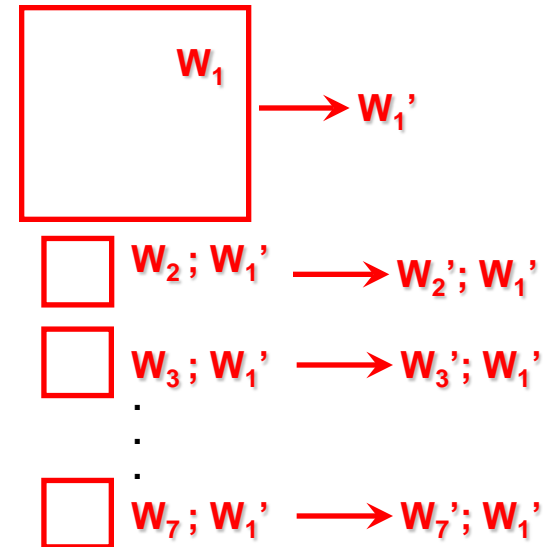
# Modification to the “Adjustment” Method

## Standard Approach



$W$ : covariance data for  
U-235, U-238, H, O, FPs

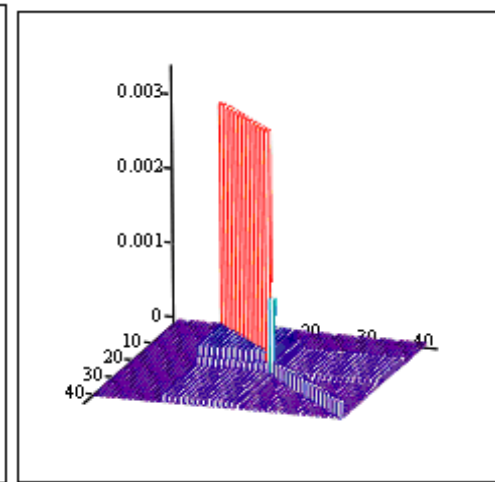
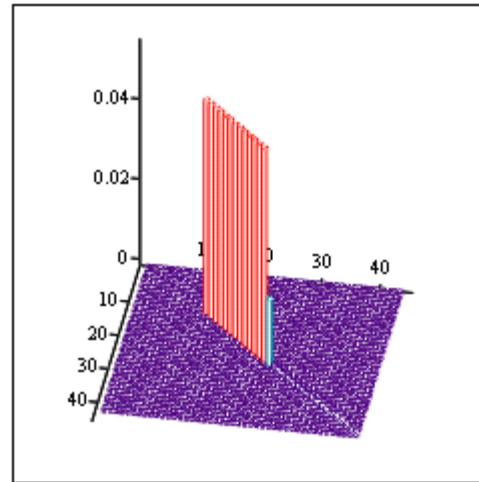
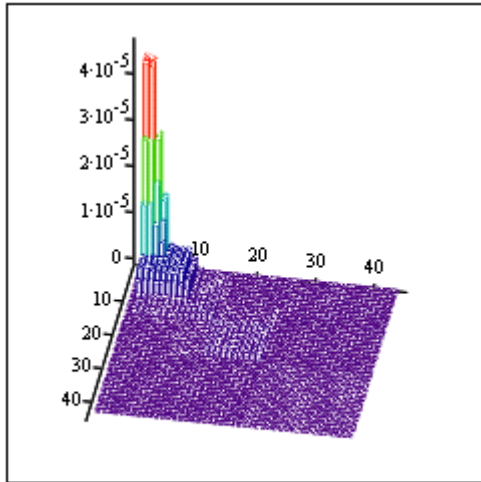
## Modified Approach



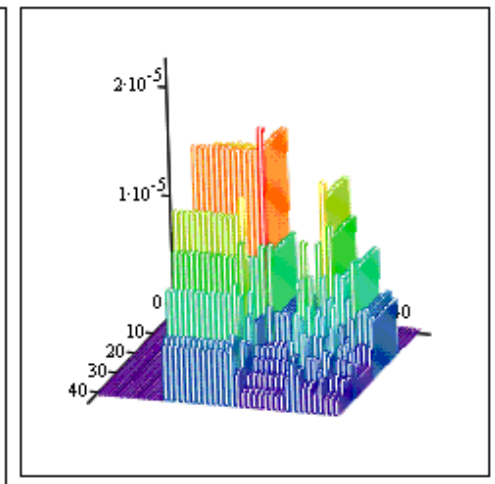
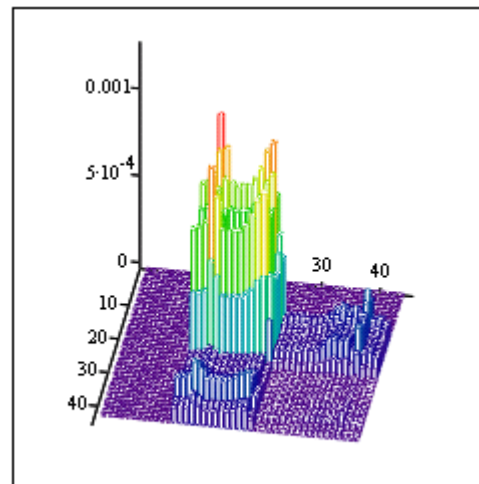
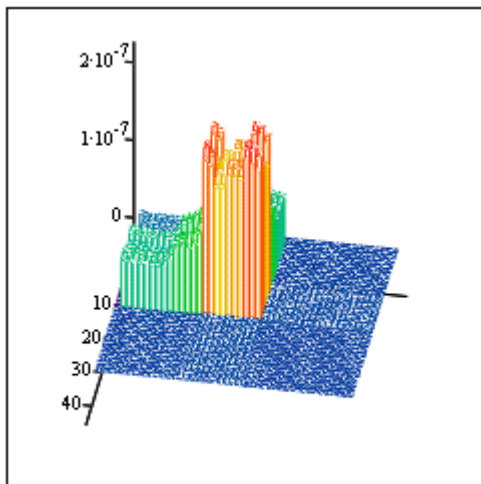
$W_1$ : covariance data for  
U-235, U-238, H, O  
 $W_2$ : covariance data for FP-1,  
 $W_3$ : covariance data for FP-2...

# Some ND Covariance Before/After the “Adjustment”

Before



After



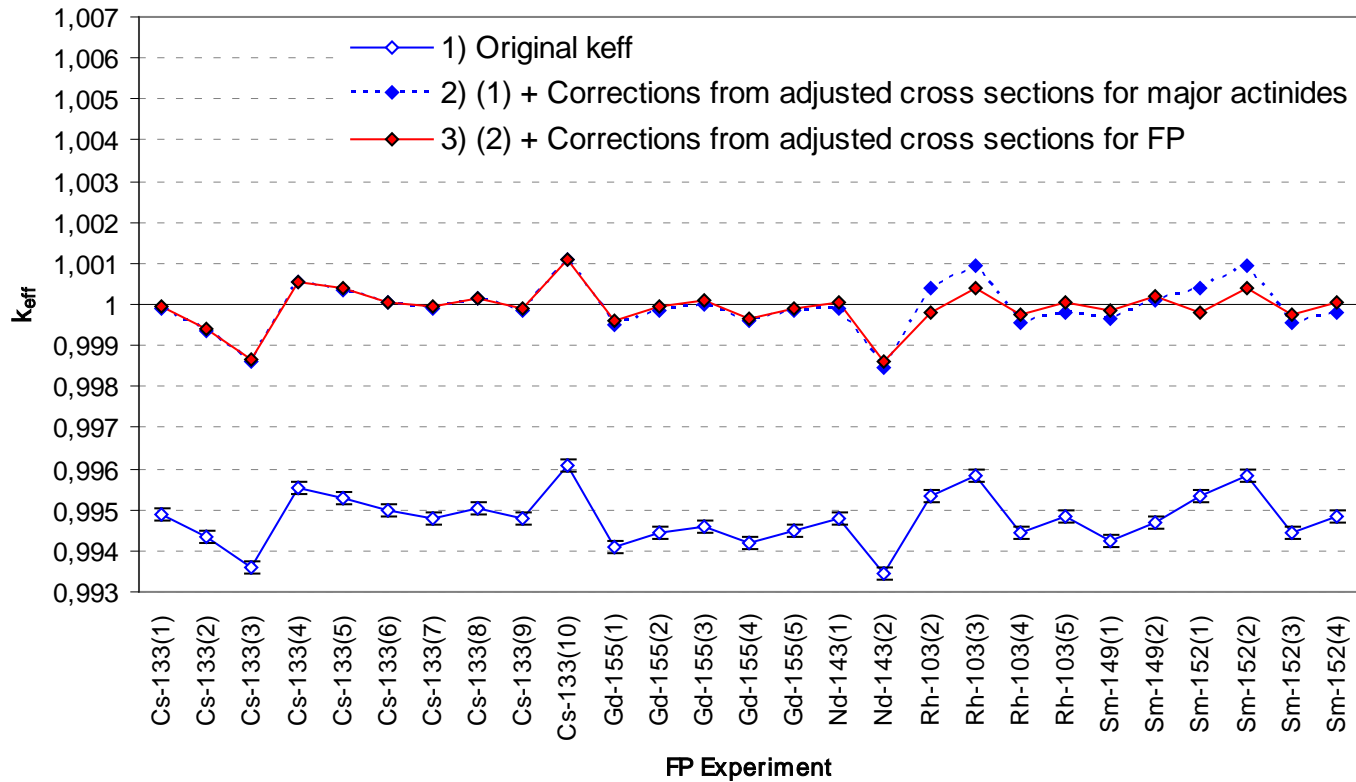
U-238 Capture

Nd-143 Capture

Rh-103 Capture

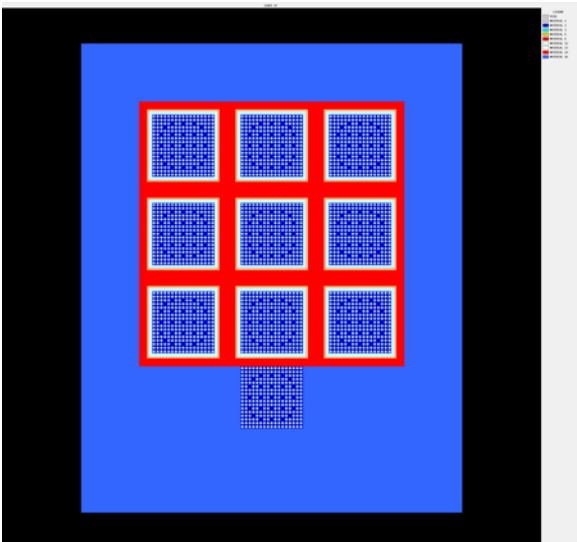
44-group ND covariance data for Cs-133, Sm-149, Sm-152, Gd-155, Ph-103, Nd-143 from ENDF/B-V.rec (SCALE5.1)

# $k_{\text{eff}}$ Bias for the FP Configurations

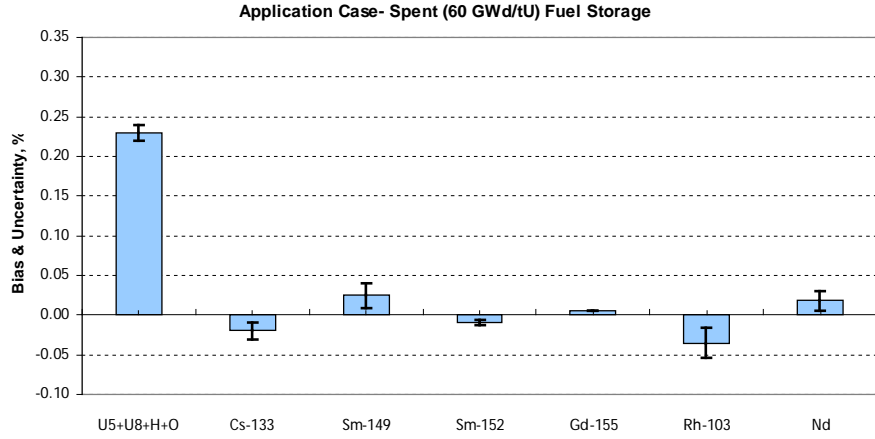
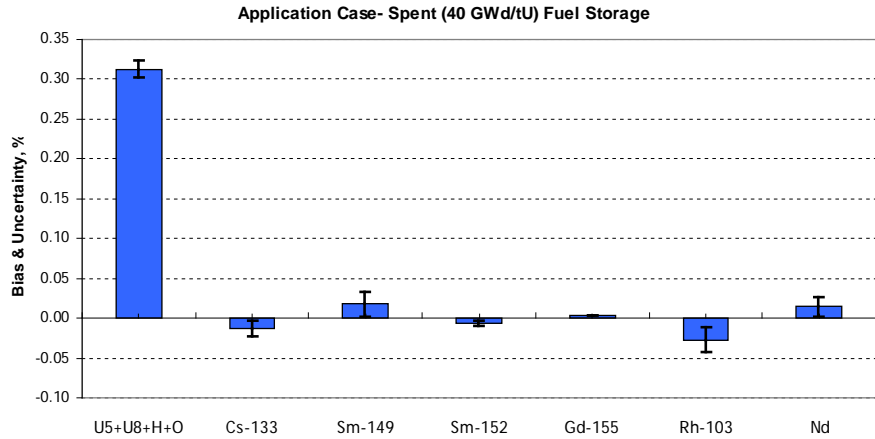


# Uncertainty Assessment for Typical Application System

Simplified models of storage in accidental condition for  $UO_2$  fuel with initial enrichment of 5% burned to 40 GWd/MTU and 60 GWd/MTU

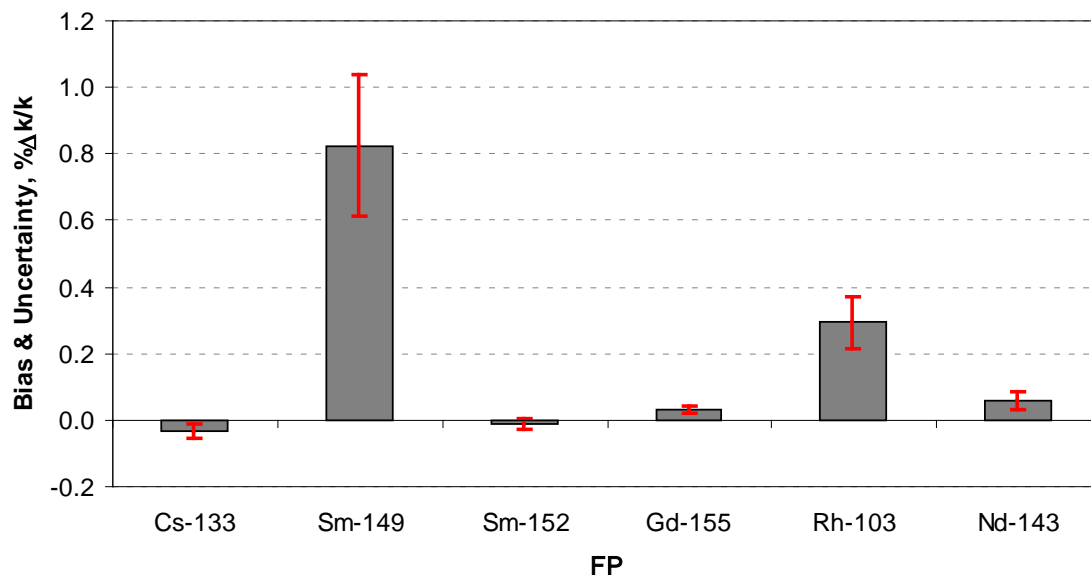
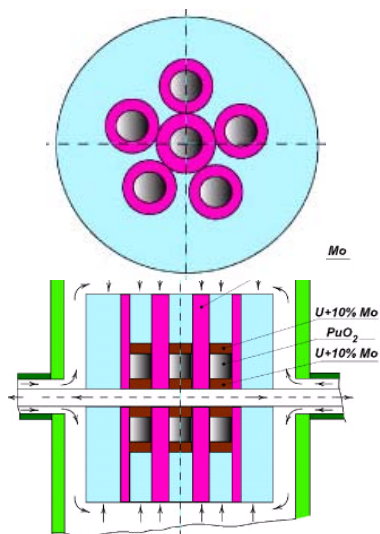


The composition of the spent fuel was calculated by CESAR4 code



# Uncertainty Assessment for Future Application System

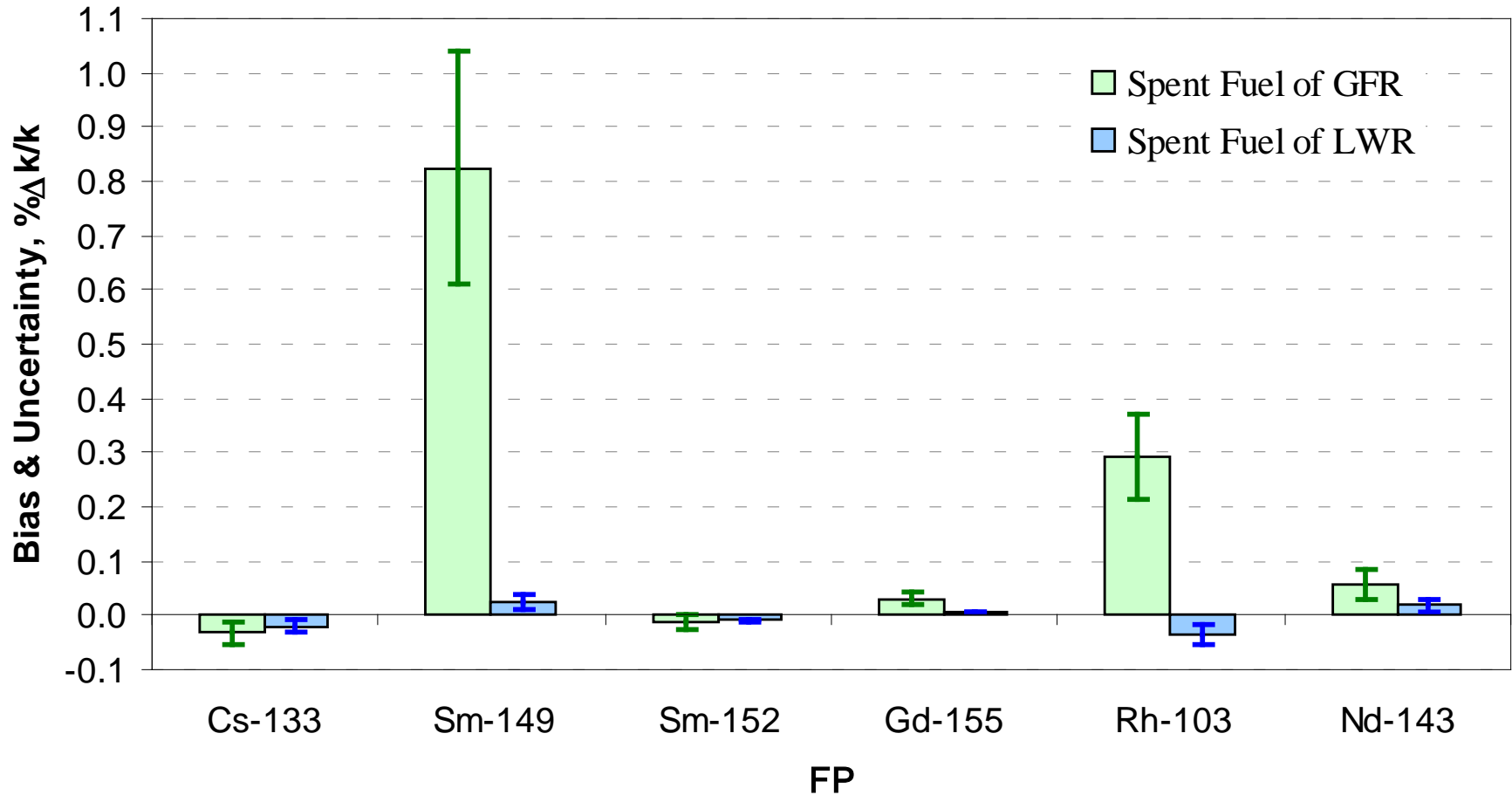
Simplified model of MOX fuel for GFR burned to  $\sim 120$  GWd/MTU and flooded by water [Ref.]



The composition of the spent fuel was calculated by ORIGEN code

[Ref.] P. N. Alekseev et al., Nuclear facility with the gas cooled fast reactor BGR-1000 using coated particles and technologies of light water reactors, Proc. of International Congress on Advances in Nuclear Power Plants (ICAPP 2007) "The Nuclear Renaissance at Work", Volume 3, pp.1657-1663 (2008)

# From Present to Future Fuel Cycle Applications



# Summary

- The methodology is proposed and tested to establish bias and bias uncertainty for FPs;
- FP validation study is performed for typical and innovative application systems;
- For the present test application the FP biases are small, as expected, and comparable with the bias uncertainties;
- The significant bias for Sm-149 is established for the innovative (FR) application system;
- The presented results show that the proposed method is useful in design and safety studies for innovative systems;
- The FP experiments provide valuable information to assess FP credit for configurations containing fuel of both the present LWR and the future FR.