

*International Workshop on Advances in Applications of Burnup Credit
for Spent Fuel Storage, Transport, Reprocessing, and Disposition*

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Peak Reactivity Characterization and Isotopic Inventory Calculations for BWR Criticality Applications

C. Casado, J. Sabater, J. F. Serrano

Core Engineering Department

ENUSA Industrias Avanzadas, SA

Fuel Characterization for BWR Criticality

1. Introduction (1)

- For BWR criticality calculations supporting spent fuel storage racks design, the most reactive fuel assembly to be stored, at its maximum reactivity point (reactivity peak), must be considered.
- Determination of the most reactive fuel assembly needs to consider the distribution (as a function of burnup) of the fissile content, burnable absorbers and fission product inventories within the fuel assembly.

Fuel Characterization for BWR Criticality

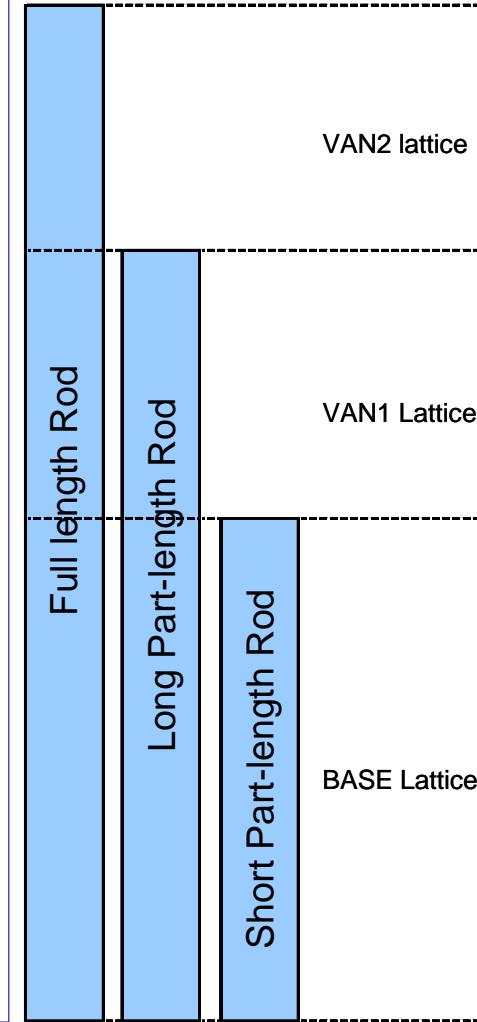
1. Introduction (2)

- BWR fuel designs and operating conditions are highly heterogeneous:
 - ✓ Different lattice geometries in the same bundle (part-length rods)
 - ✓ Radial and axial distribution of enrichment and gadolinium inside the bundle.
 - ✓ Burnup dependent local operating conditions: void fractions and control rod insertion
- BWR fuel characterization for criticality analysis is not so straight as desirable.
- The scope of this work is to develop a simple and conservative (production) model for BWR criticality analysis.
- Production model derived from a series of sensitivity analysis to the relevant characteristics of the real model:
 - ✓ K-infinite and isotopic calculations performed with the lattice TGBLA code.
 - ✓ In-rack K-effective calculations performed with CSAS25 (SCALE5.1).

Fuel Characterization for BWR Criticality

1. Introduction (3)

- The examples and results included in this presentation are for GNF fuel designs.
- Fuel lattices named as BASE, VAN1 or VAN2 depending on the existence and type of partial length rods.
- The conclusions of the study judged to be easily extrapolated to other vendors designs.



Fuel Characterization for BWR Criticality

2. Evolution of fuel reactivity with burnup and operating conditions (1)

- BWR fuel reactivity increases, due to the presence of gadolinium rods, from its fresh fuel value up to a maximum obtained at a given burnup (reactivity peak)
- For a given lattice design the reactivity peak will depend on void fraction and control rod insertion.

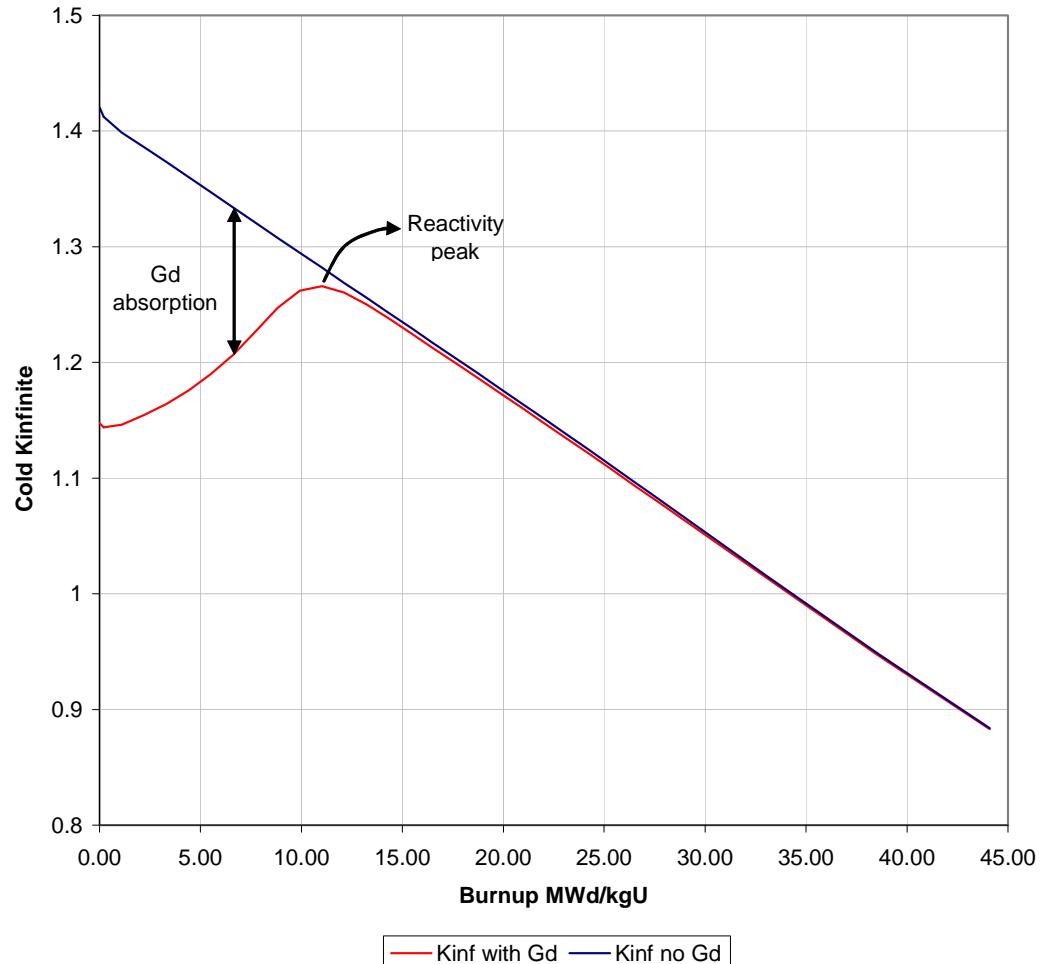


Figure: Cold K-infinite vs Burnup

Fuel Characterization for BWR Criticality

2. Evolution of fuel reactivity with burnup and operating conditions (2)

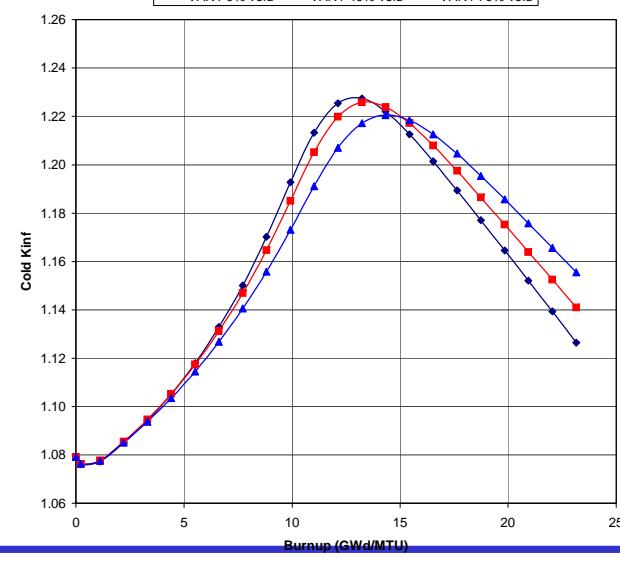
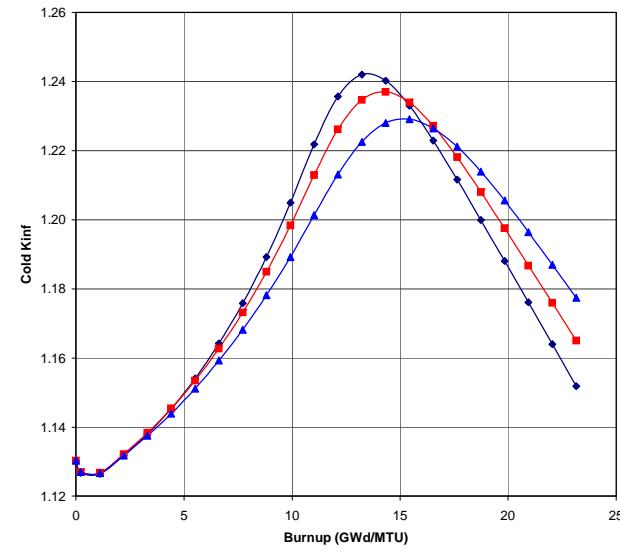
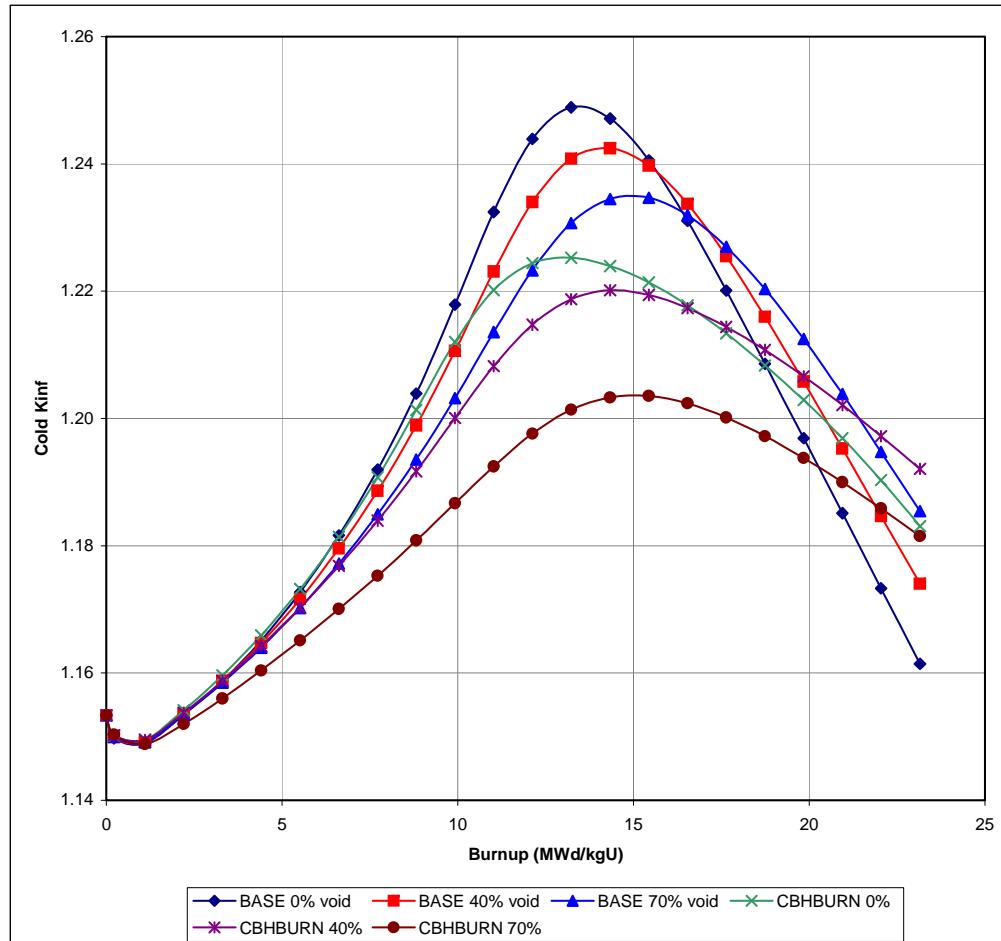
- First step towards simplified model consists on determining the core conditions that lead to the highest cold K-infinite value.
- Burnup calculations at several void fractions were performed for a fuel with 12 Gd rods at 5% in Gd_2O_3 .
- Control blade insertion was also analyzed for the BASE lattice.
- For all lattices, the highest cold K-infinite was reached for the uncontrolled case at 0.0 voids.
- For the BASE lattice, the highest K-infinite corresponds to the uncontrolled case

	A	B	C	D	E	F	G	H	I	J
1	1.60	2.80	3.60	4.40	4.40	4.40	4.40	3.60	2.80	2.00
2	2.80	4.00	4.40 5.00	4.95	4.40 5.00	4.95	4.95	4.40 5.00	4.95	3.20
3	3.60	4.40 5.00	4.95	4.95	4.95	4.95	4.95	4.95	4.40 5.00	4.40
4	4.40	4.95	4.95	4.95	4.95	WR		4.95	4.95	4.95
5	4.40 5.00	4.40 5.00	4.95	4.95	4.95	-	-	4.95	4.95	4.95
6	4.40	4.95	4.95	WR		4.95	4.95	4.95	4.40 5.00	4.95
7	4.40	4.95	4.95	-	-	4.95	4.95	4.95	4.95	4.95
8	3.60	4.40 5.00	4.95	4.95	4.95	4.95	4.95	4.95	4.95 5.00	4.95
9	2.80	4.95	4.40 5.00	4.95	4.95	4.40 5.00	4.95	4.95 5.00	4.95	3.20
10	2.00	3.20	4.40	4.95	4.95	4.95	4.95	4.95	3.20	2.80

Figure: BASE lattice with 12 Gd5% rods.

Fuel Characterization for BWR Criticality

2. Evolution of BWR fuel reactivity with burnup and operating conditions (3)



K-infinite vs. void fraction and control rod insertion

Fuel Characterization for BWR Criticality

3. Evolution of fuel reactivity with axial burnup and voids shapes (1)

- Next step towards simplified model is related to the axial distribution of burnup and void fraction.
- In the figure it is represented the axial burnup shape at two different locations of a particular equilibrium cycle design.
- The average burnup of those bundles being similar to that of the reactivity peak (slide 7).

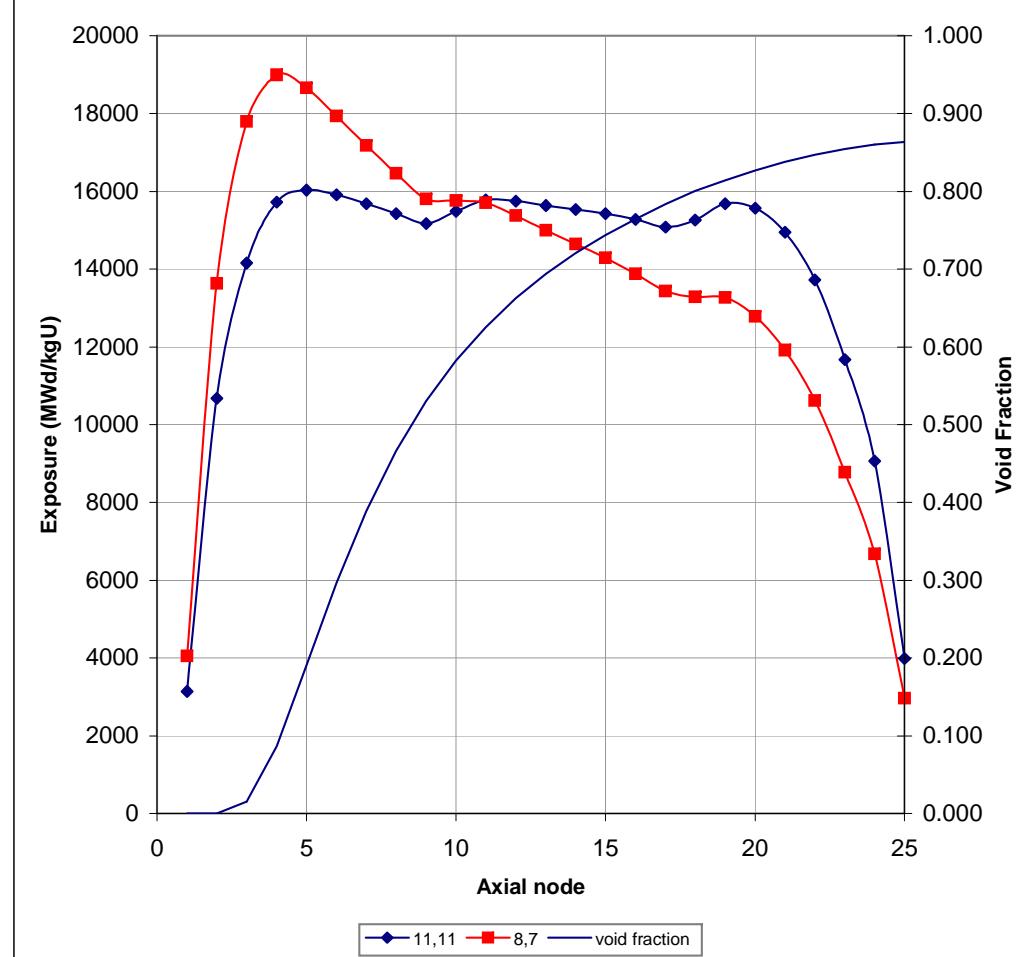
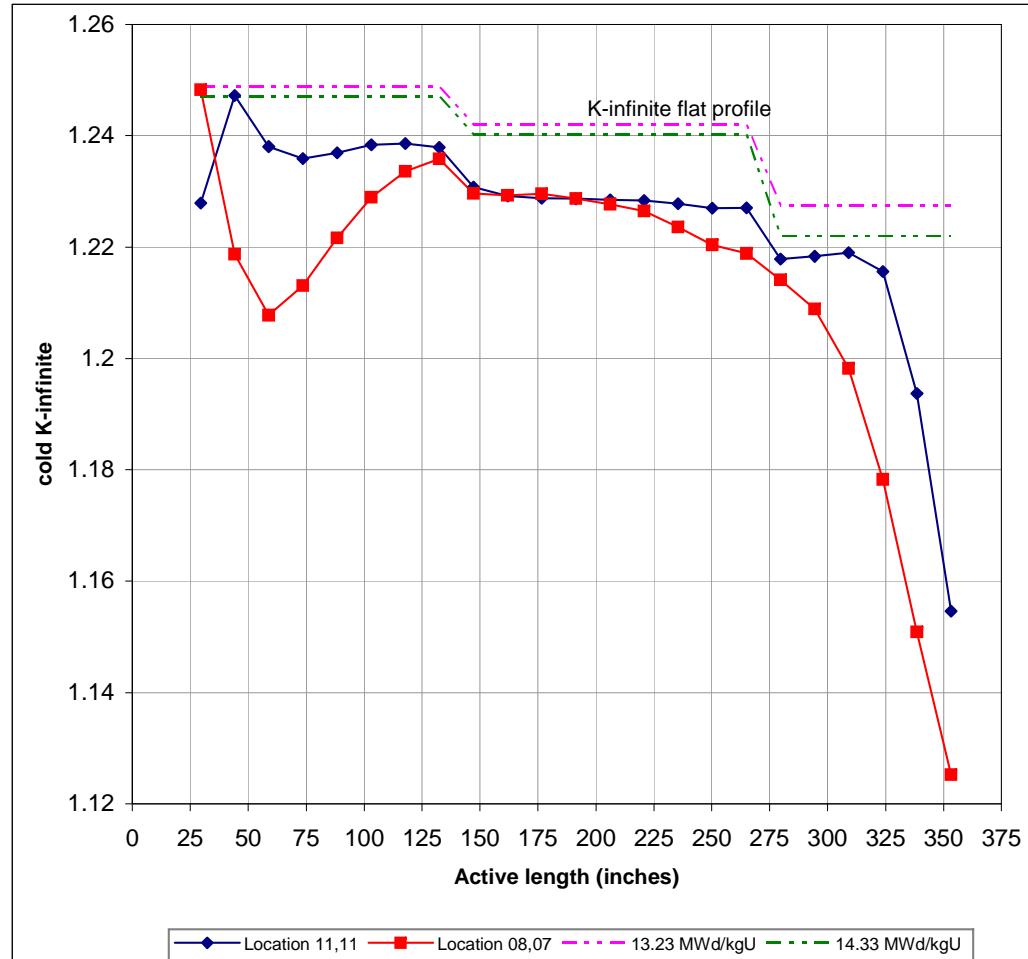


Figure: Burnup and void fraction vs. axial height

Fuel Characterization for BWR Criticality

3. Evolution of fuel reactivity with axial burnup and voids shapes (2)

- Node by node cold K-infinite values, calculated from local node burnup and void fraction values, for the two bundles.
- Cold K-infinite calculated for each lattice at two burnups around the peak reactivity burnup point.
- Lattice cold K-infinite values calculated at the peak reactivity 1%-2% higher than local (node wise) values.
- The shown excess in reactivity is due to differences in the isotopic evolution of the fuel, which, in turn, produce differences in the in-rack K-effective of the fuel



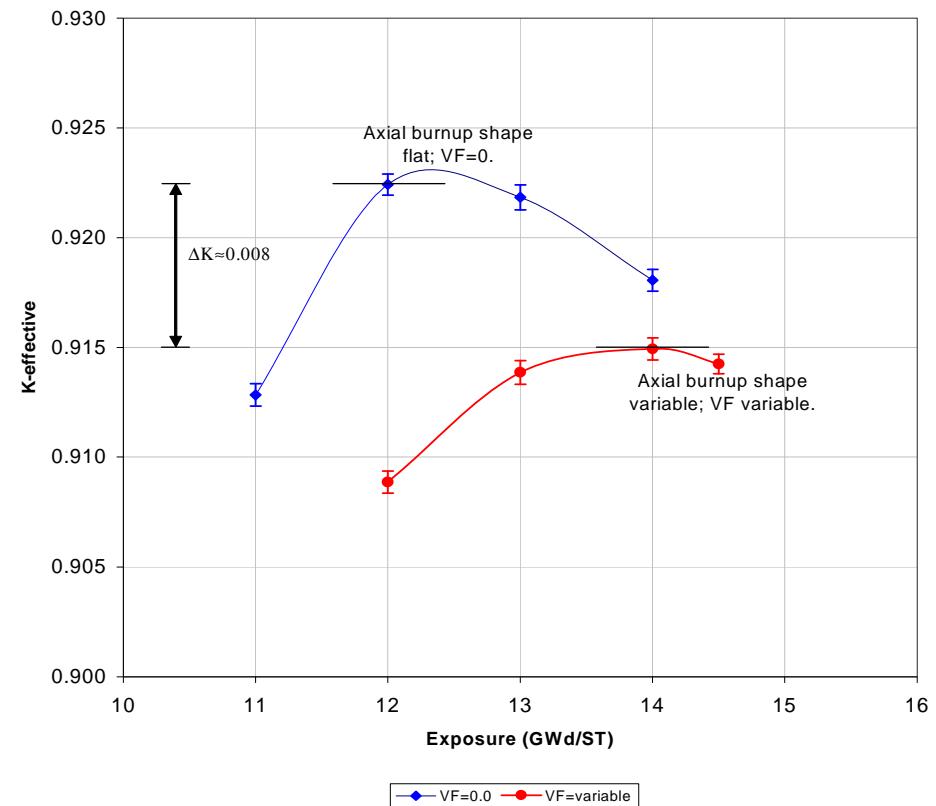
K-infinite vs. axial height

Fuel Characterization for BWR Criticality

3. Evolution of fuel reactivity with axial burnup and voids shapes (3)

- Comparisons have been made with CSAS25 (SCALE5.1) between homogeneous and heterogeneous axial shapes.
- As for the K-infinite, homogeneous case produces conservative results also for the in-rack K-effective.

Burnup(norm.)	void fraction		burnup	void fraction
14.72				
29.44	0.725	0.000	0.725	0
44.16	0.961	0.016	0.961	0
58.88	1.068	0.087		
73.6	1.089	0.191	1.079	0.191
88.32	1.081	0.297		
103.04	1.065	0.389		
117.76	1.048	0.466		
132.48	1.030	0.530		
147.2	1.052	0.582		
161.92	1.071	0.625	1.057	0.564
176.64	1.069	0.663		
191.36	1.062	0.694		
206.08	1.055	0.721		
220.8	1.048	0.744		
235.52	1.038	0.764		
250.24	1.024	0.784	1.046	0.779
264.96	1.036	0.801		
279.68	1.065	0.815		
294.4	1.057	0.827		
309.12	1.015	0.838	1.015	
323.84	0.932	0.847	0.932	0.850
338.56	0.793	0.855	0.793	
353.28	0.616	0.860	0.616	
368				



Fuel Characterization for BWR Criticality

4. Evolution of fuel reactivity with gadolinium rods configuration (1)

Configuration "a"

	A	B	C	D	E	F	G	H	I	J
1	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60
2	3.60	3.60	3.60 4.00	3.60	3.60	3.60	3.60	3.60	3.60 4.00	3.60
3	3.60	3.60 4.00	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60
4	3.60	3.60	3.60	3.60	3.60	WR	-	3.60	3.60	3.60
5	3.60	3.60	3.60	3.60	3.60		-	3.60	3.60	3.60
6	3.60	3.60	3.60	WR	-	3.60	3.60	3.60	3.60	3.60
7	3.60	3.60	3.60		-	3.60	3.60	3.60	3.60	3.60
8	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60 4.00	3.60
9	3.60 4.00	3.60	3.60	3.60	3.60	3.60	3.60	3.60 4.00	3.60	3.60
10	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60

Configuration "b"

	A	B	C	D	E	F	G	H	I	J
1	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60
2	3.60	3.60	3.60 4.00	3.60	3.60 4.00	3.60	3.60	3.60	3.60	3.60
3	3.60 4.00	3.60	3.60	4.00	3.60	3.60	3.60	3.60	3.60	3.60
4	3.60	3.60	3.60 4.00	3.60	3.60	WR	-	3.60	3.60	3.60
5	3.60 4.00	3.60	3.60	3.60	3.60		-	3.60	3.60	3.60
6	3.60	3.60	3.60	WR	-	3.60	3.60	3.60	3.60	3.60
7	3.60	3.60	3.60		-	3.60	3.60	3.60	3.60	3.60
8	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60
9	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60
10	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60	3.60

3.60 UO₂ rod
3.60
4.00 UO₂+Gd rod

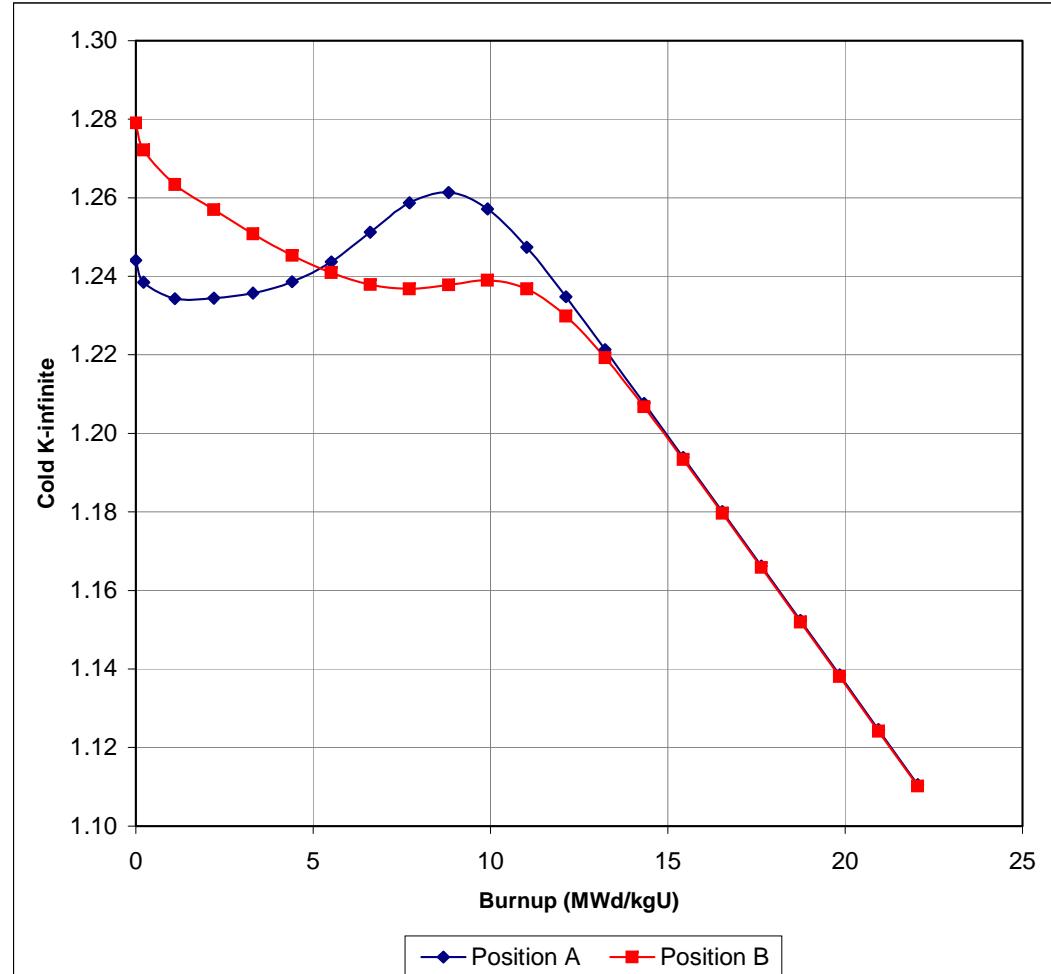


Figure: Gad rods configurations analyzed for 6Gd4% lattice

Fuel Characterization for BWR Criticality

4. Evolution of fuel reactivity with gadolinium rods configuration (2)

Configuration "a"

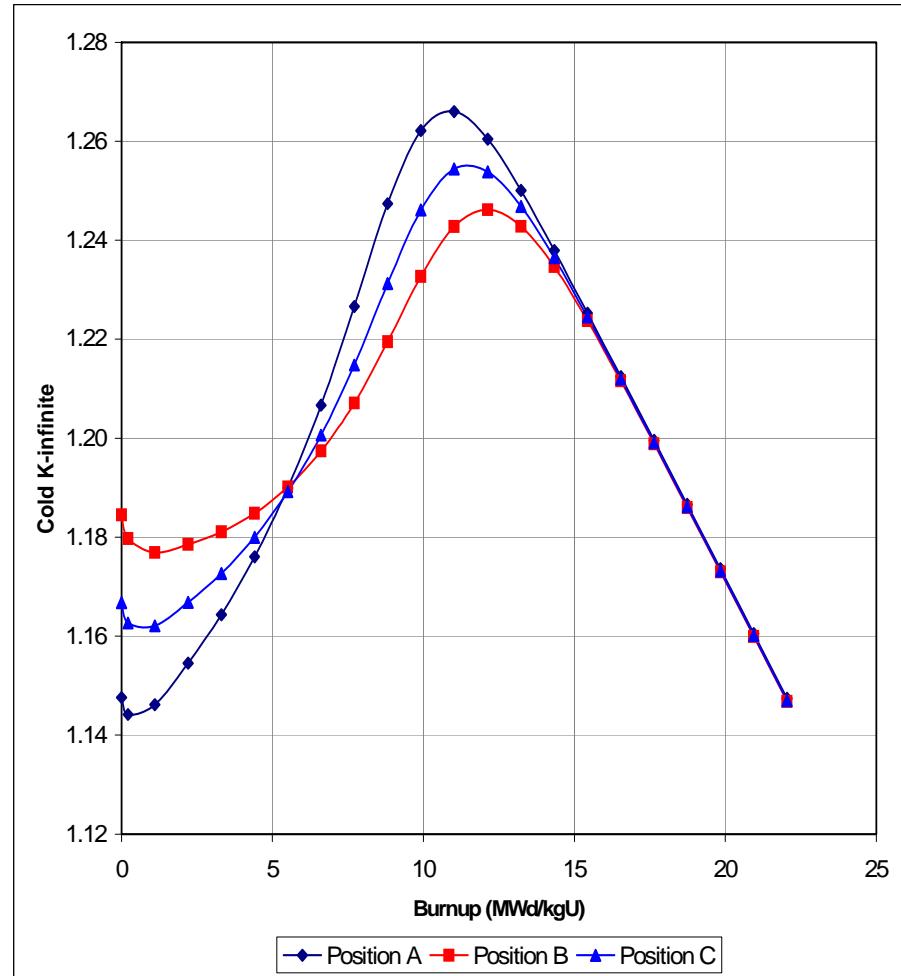
	A	B	C	D	E	F	G	H	I	J
1	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98
2	3.98	3.98	4.00	3.98	3.98	4.00	3.98	3.98	3.98	3.98
3	3.98	3.98	4.00	3.98	3.98	3.98	3.98	3.98	3.98	3.98
4	3.98	3.98	3.98	3.98	3.98	WR		3.98	3.98	3.98
5	3.98	3.98	4.00	3.98	3.98	-	-	3.98	3.98	3.98
6	3.98	3.98	3.98	WR	-	3.98	3.98	3.98	3.98	3.98
7	3.98	3.98	3.98	-		3.98	3.98	3.98	3.98	3.98
8	3.98	3.98	4.00	3.98	3.98	3.98	3.98	3.98	3.98	3.98
9	3.98	3.98	4.00	3.98	3.98	3.98	4.00	3.98	3.98	3.98
10	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98

Configuration "b"

	A	B	C	D	E	F	G	H	I	J
1	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98
2	3.98	3.98	4.00	3.98	3.98	4.00	3.98	3.98	3.98	3.98
3	3.98	3.98	4.00	3.98	3.98	3.98	3.98	3.98	3.98	3.98
4	3.98	3.98	4.00	3.98	3.98	WR		3.98	3.98	3.98
5	3.98	3.98	4.00	3.98	3.98	-	-	3.98	3.98	3.98
6	3.98	3.98	3.98	WR	-	3.98	3.98	3.98	3.98	3.98
7	3.98	3.98	3.98	-		3.98	3.98	3.98	3.98	3.98
8	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98
9	3.98	3.98	3.98	3.98	3.98	3.98	4.00	3.98	3.98	3.98
10	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98

Configuration "c"

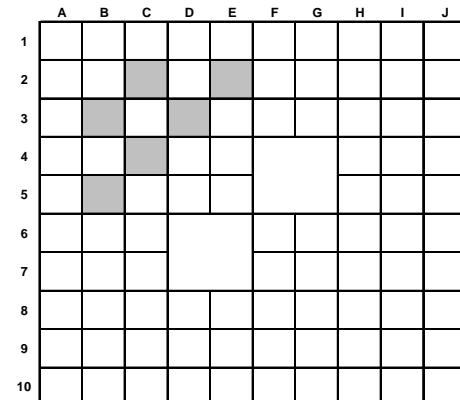
	A	B	C	D	E	F	G	H	I	J
1	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98
2	3.98	3.98	3.98	4.00	3.98	3.98	3.98	3.98	3.98	3.98
3	3.98	3.98	3.98	4.00	3.98	3.98	3.98	3.98	3.98	3.98
4	3.98	3.98	3.98	4.00	3.98	WR		3.98	3.98	3.98
5	3.98	3.98	3.98	3.98	-		3.98	3.98	3.98	3.98
6	3.98	3.98	3.98	WR	-	3.98	3.98	3.98	3.98	3.98
7	3.98	3.98	3.98	-		3.98	3.98	3.98	3.98	3.98
8	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98
9	3.98	3.98	3.98	4.00	3.98	3.98	4.00	3.98	3.98	3.98
10	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98	3.98



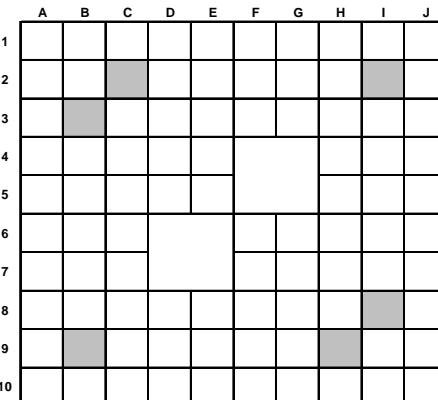
Fuel Characterization for BWR Criticality

4. Evolution of fuel reactivity with gadolinium rods configuration (3)

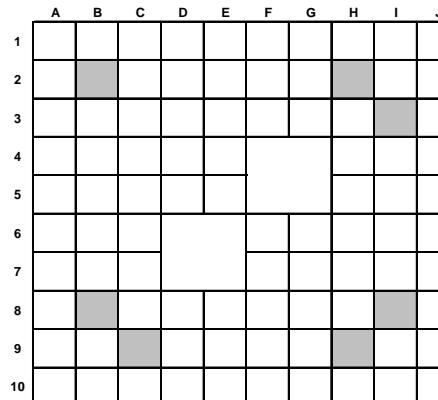
a) Configuration for 6 Gd rods (BOL calculations)



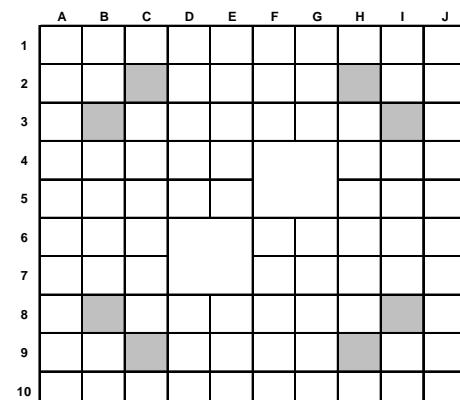
b) Configurations for 6 Gd rods (Burned fuel calculations)



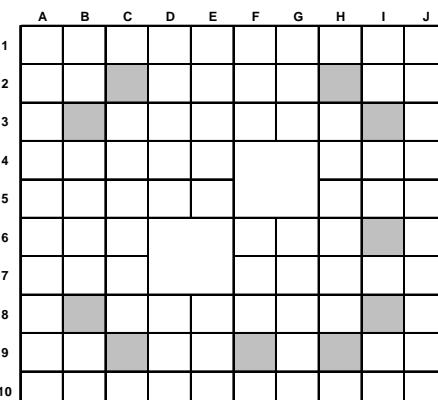
c) Configuration for 7 Gd rods



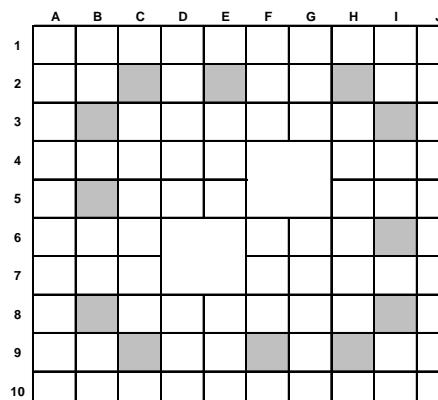
d) Configuration for 8 Gd rods



e) Configuration for 10 Gd rods



f) Configuration for 12 Gd rods



□ UO₂ rod □ UO₂+Gd rod

Figure: Conservative Gd rods configurations for Criticality Analysis

Fuel Characterization for BWR Criticality

4. Evolution of fuel reactivity with gadolinium rods configuration (4)

- In conclusion:

- ✓ Limiting gadolinium configurations can be different for fresh and burned fuel.
- ✓ For given fuel design and gadolinium needs, it is possible to establish limiting configurations of gadolinium rods, based on a reduced number of K-infinite lattice calculations.

Fuel Characterization for BWR Criticality

5. Initial enrichment distribution (1)

- Fresh fuel may be limiting only for ≤ 5 Gd rods, with all Gd rods closely packed (see figure in slide 11).
- Heterogeneous and homogeneous cases have been analyzed for a fuel with 3.735% average enrichment and 5Gd4% rods.

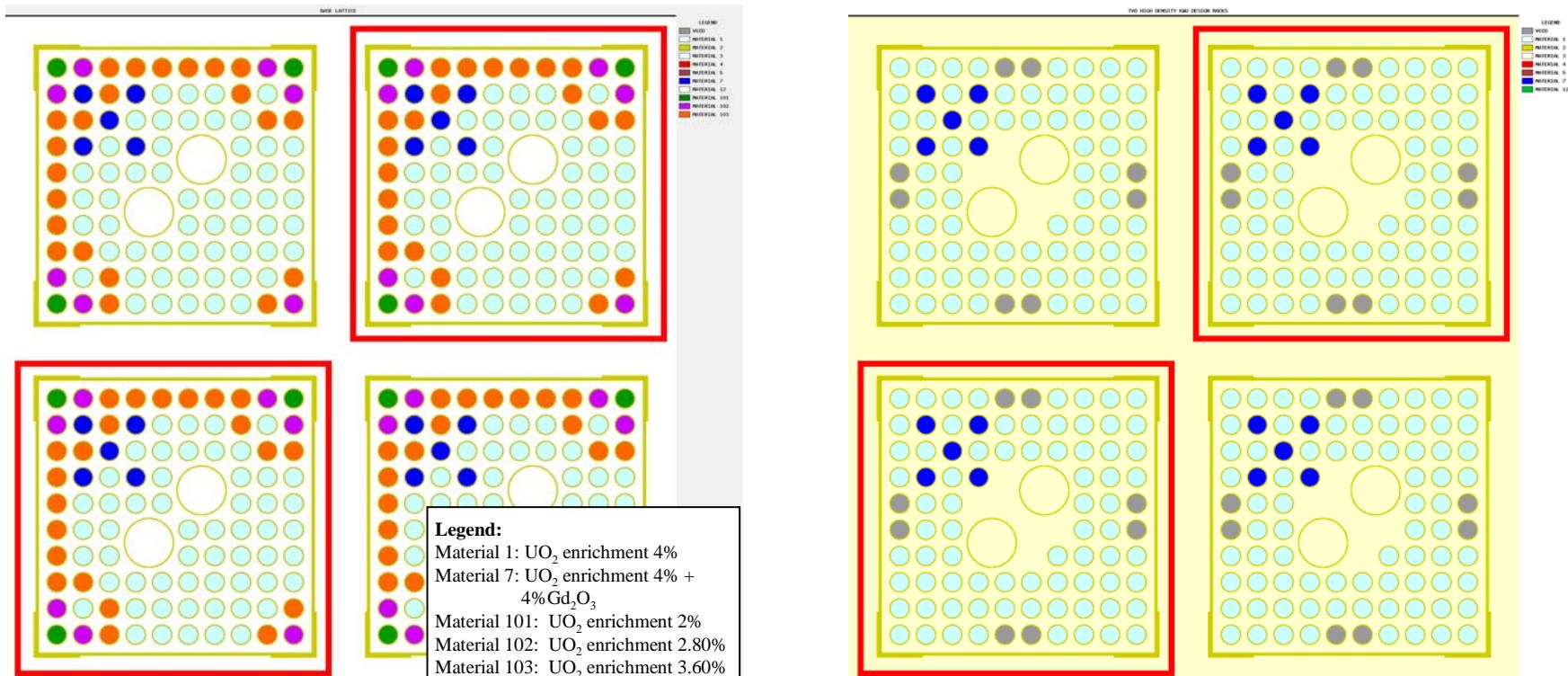


Figure: Heterogeneous and homogeneous initial enrichment distribution

Fuel Characterization for BWR Criticality

5. Initial enrichment distribution (2)

- Results for CSAS25 simulations:

Enrichment model	K-effective	σ
Homogeneous	0.92564	0.00048
Heterogeneous	0.91766	0.00051

- K-effective for the homogeneous radial model is almost 1% higher than that of the (real) heterogeneous model. Thus, the homogeneous (radial) enrichment model is conservative for fresh fuel criticality analysis.

Fuel Characterization for BWR Criticality

6. Radial Isotopic distribution (1)

- Now, we examine the radial rod-by-rod isotopic distribution.
- For burned fuel, the isotopic content is different in each rod, due to differences in their initial enrichment and because their power histories are also different.

RELATIVE POWER DISTRIBUTION

0.7741	0.9091	1.0043	1.2055	0.0000	0.0000	1.2105	1.0074	0.9031	0.8544
0.9091	0.9161	0.8663	0.9691	1.0054	1.0832	0.9869	0.8719	1.0220	0.9543
1.0043	0.8663	0.8539	0.9113	1.0609	1.0931	1.0127	0.8942	0.8451	1.0953
1.2055	0.9691	0.9113	1.1416	0.0000	0.0000	0.0000	1.0097	0.9686	1.2639
0.0000	1.0054	1.0609	0.0000	0.0000	0.0000	0.0000	1.0926	1.0745	0.0000
0.0000	1.0832	1.0931	0.0000	0.0000	0.0000	0.0000	1.0592	0.9902	0.0000
1.2105	0.9869	1.0127	0.0000	0.0000	0.0000	1.1421	0.9001	0.9347	1.2509
1.0074	0.8719	0.8942	1.0097	1.0926	1.0592	0.9001	0.8164	0.8125	1.1475
0.9031	1.0220	0.8451	0.9686	1.0745	0.9902	0.9347	0.8125	0.9618	0.9276
0.8544	0.9543	1.0953	1.2639	0.0000	0.0000	1.2509	1.1475	0.9276	0.9984

RELATIVE EXPOSURE DISTRIBUTION

0.7922	0.9795	1.0624	1.2770	0.0000	0.0000	1.2931	1.0570	0.9502	0.8711
0.9795	0.9654	0.6546	0.9910	0.7595	1.1307	1.0472	0.6608	1.0806	1.0077
1.0624	0.6546	0.8705	0.9649	1.0897	1.1483	1.0681	0.9096	0.6311	1.1443
1.2770	0.9910	0.9649	1.1868	0.0000	0.0000	0.0000	1.0558	1.0056	1.3147
0.0000	0.7595	1.0897	0.0000	0.0000	0.0000	0.0000	1.1306	1.0868	0.0000
0.0000	1.1307	1.1483	0.0000	0.0000	0.0000	0.0000	1.0660	0.7100	0.0000
1.2931	1.0472	1.0681	0.0000	0.0000	0.0000	1.1680	0.9305	0.9207	1.2620
1.0570	0.6608	0.9096	1.0558	1.1306	1.0660	0.9305	0.8133	0.6083	1.1761
0.9502	1.0806	0.6311	1.0056	1.0868	0.7100	0.9207	0.6083	0.9816	0.9368
0.8711	1.0077	1.1443	1.3147	0.0000	0.0000	1.2620	1.1761	0.9368	1.0027

Figure: Relative power and burnup distribution for a 4.41% heterogeneous lattice with 12Gd5% rods at 13.23 MWd/KgU burnup step.

Fuel Characterization for BWR Criticality

6. Radial Isotopic distribution (2)

- The heterogeneous (diagonal symmetric) CSAS25 model uses different fuel rods types, each one with its corresponding set of isotopic composition, for each of the axial segments being considered: BASE, VAN1 and VAN2.
- For the case being presented a total of $51+47+43= 141$ different isotopic sets for the CSAS25 model were used.
- In the homogeneous model only 6 different isotopic sets were used: one for the UO₂ rod and other for the UO₂+Gd₂O₃ rod, for each of the three axial lattices.

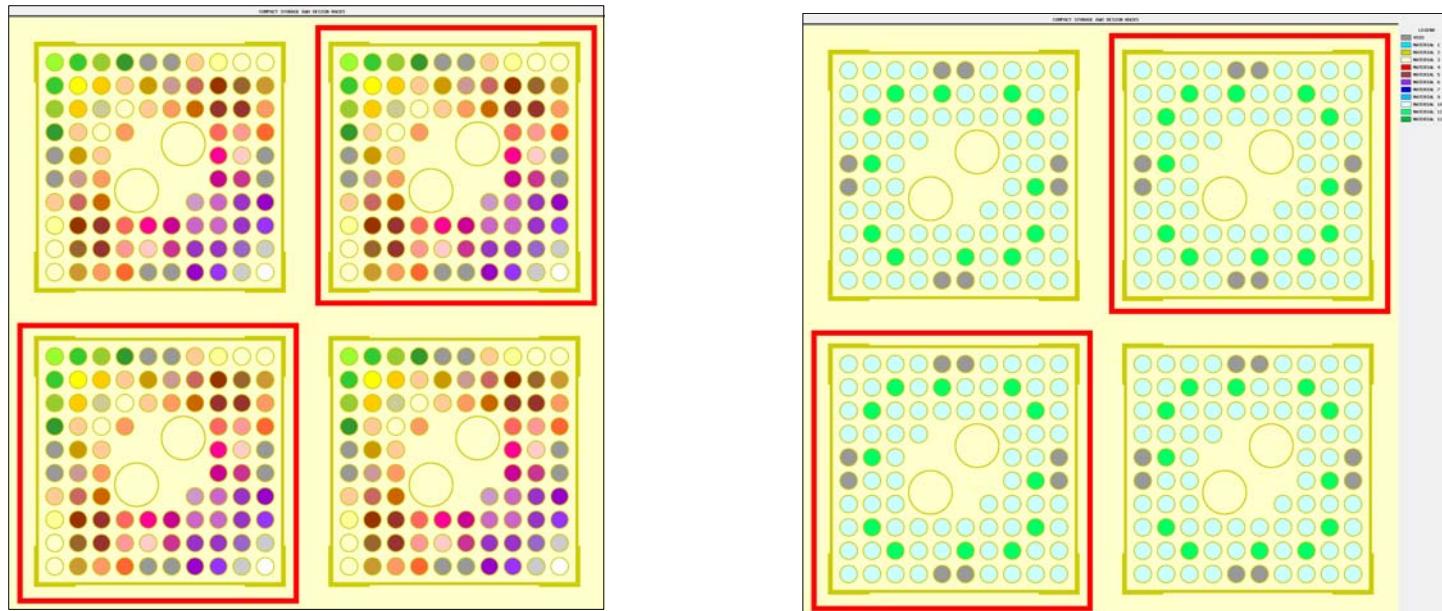


Figure: Heterogeneous and homogeneous radial model.

Fuel Characterization for BWR Criticality

6. Radial Isotopic distribution (3)

- Several pairs of (enrichment, gadolinium) were analyzed, for different racks geometries and fuel designs.
- In all cases the homogeneous model gave higher K-effective results than the corresponding heterogeneous case.
- Therefore, homogeneous radial isotopic model is conservative for burned fuel Criticality Analysis.

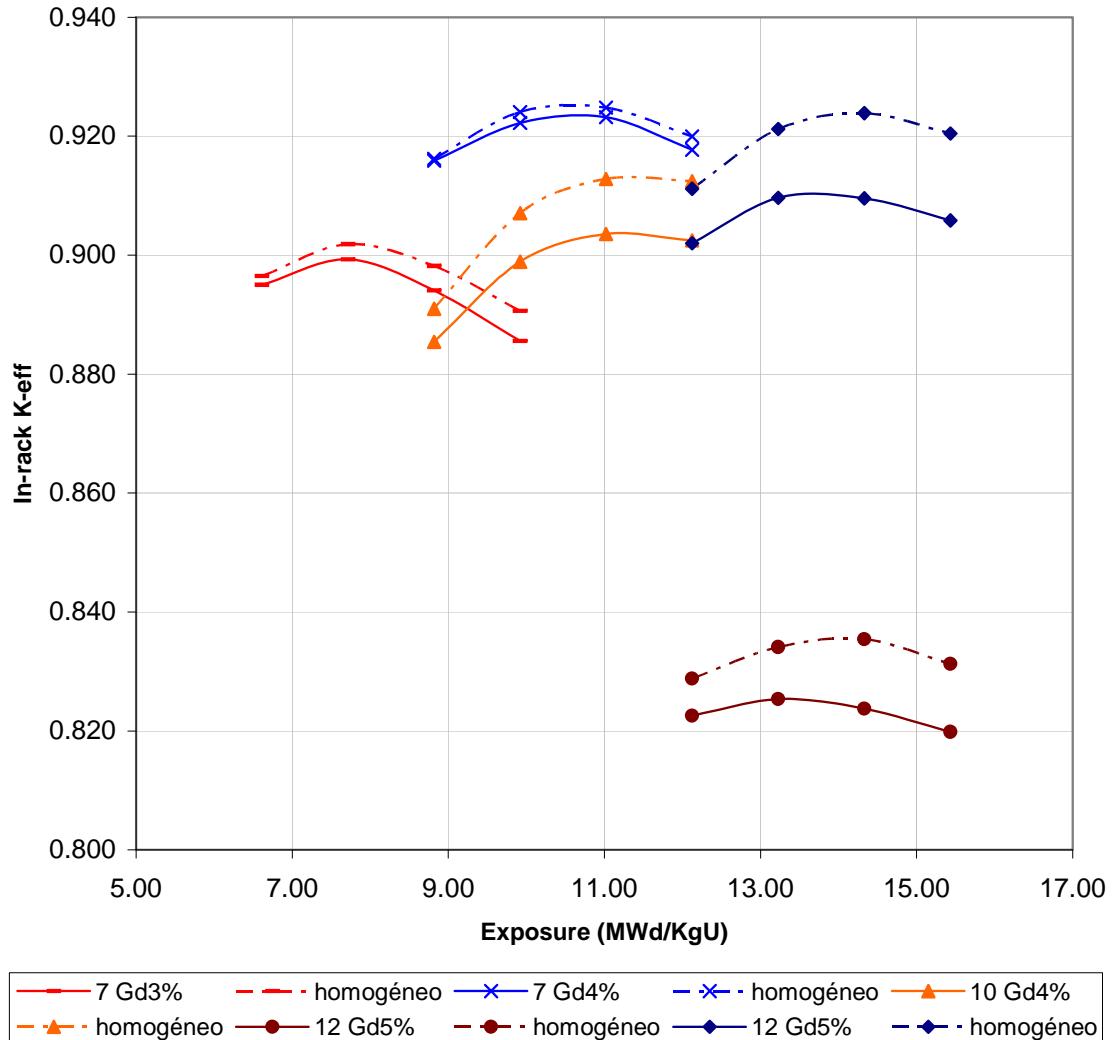


Figure: Heterogeneous vs homogeneous radial model K-eff.

Fuel Characterization for BWR Criticality

7. Summary and conclusions (1)

- BWR fuel designs and operating conditions are highly heterogeneous:
 - ✓ Different lattice geometries in the same bundle (part-length rods)
 - ✓ Radial and axial distribution of enrichment and gadolinium inside the bundle.
 - ✓ Burnup dependent local operating conditions: void fractions and control rod insertion
- A conservative 3D-model, useful for Criticality Analysis production work, has been developed.
- The production model is characterized by:
 - ✓ Different actual lattice geometries (Full length and Part-length fuel rods) are explicitly modeled.
 - ✓ Fuel isotopic content obtained from uncontrolled 0 void fraction burnup calculations, covering the peak reactivity range.
 - ✓ Flat axial burnup shape (i.e. all axial lattices at the same burnup) in the range of the peak reactivity.
 - ✓ Conservative locations of Gd rods.
 - ✓ Homogeneous initial enrichment in all rods (fresh fuel).
 - ✓ Homogeneous radial isotopic distribution for spent fuel (except for Gd isotopes) for each lattice.

Fuel Characterization for BWR Criticality

7. Summary and conclusions (2)

- This way, the BWR fuel can be characterized, for Criticality Analysis, by the Enrichment/Gadolinium content pair.
- The examples and conclusions presented here are for GNF fuel designs.
- Nevertheless, the conclusions of the study judged to be easily extrapolated to other vendors designs.