

DE LA RECHERCHE À L'INDUSTRIE



Comparisons & Discussions on Adjustment trends from JEFF (CEA)

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Covariances Matrices methodologies: Cross Section “knowledge”, Evaluations and Integral Constraints

■ Experimentalist

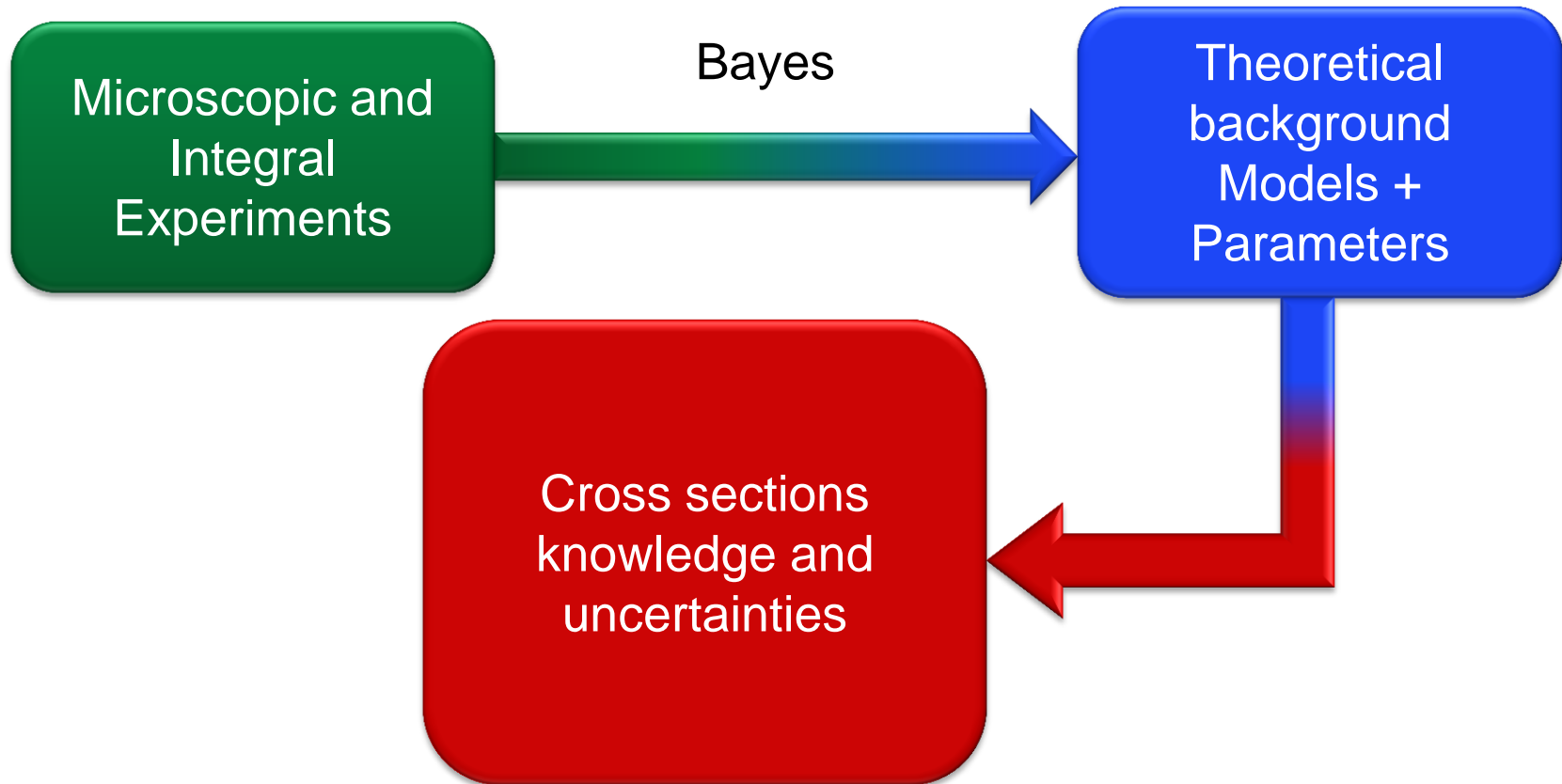
Knowledge of cross section  finest microscopic experiments and smartest integral experiments;

Calibration; Systematical uncertainties...

■ Theoretician

Knowledge of cross section  knowledge of models parameters and/or nuclear reaction models (resonance parameters, optical models, fission barrier, average width, ...);

Systematics; Model defects



Issues:

- Systematic experimental uncertainties
- Phenomenological Nuclear reaction model theories & Parameters
- Integral experiment assimilation

Bayesian inference (probability density):

$$p(\vec{x} | M, \vec{y}, U) = \frac{p(\vec{x} | M, U) \cdot p(\vec{y} | M, \vec{x}, U)}{\int d\vec{x} \cdot p(\vec{x} | M, U) \cdot p(\vec{y} | M, \vec{x}, U)}$$

Model parameters New measurements *a priori* information

Formulation:

posterior [$p(\vec{x} | \vec{y}, U)$] \propto prior [$p(\vec{x} | U)$]. likelihood [$p(\vec{y} | \vec{x}, U)$]

Estimation of the first two moments
of the *a posteriori* distribution

Bayesian inference (probability density):

Maximum Entropy Principle

Laplace approximation
(Sammy, Refit, Conrad, SOK...)

Monte-Carlo
(UMC, Forward-Backward...)

Estimation of a cost function
(Generalized Chi-square)

$$\chi_{GSL}^2 = (\vec{x} - \vec{x}_m)^T M_x^{-1} (\vec{x} - \vec{x}_m) + (\vec{y} - \vec{t}(\vec{x}))^T M_y^{-1} (\vec{y} - \vec{t}(\vec{x}))$$

- Estimation 1st two moments of $p(\vec{x}/M, \vec{y}, U)$ with Monte-Carlo
- Sample of $p(\vec{x} | M, U) \rightarrow \vec{x}_k$
- For each \vec{x}_k calculation of Likelihood $\ell_k [p(\vec{y}/M, \vec{x}_k, U)]$

Bayesian inference (probability density):

■ Description of \vec{x} and M :

■ Resonance range:

- R-Matrix (resonance parameters)
- Average models (average resonance parameters)

$$\vec{x} = \{\gamma_{a\lambda}, E_\lambda, a_c, R'\}$$

$$\vec{x} = \{\langle \Gamma_a \rangle, a_c, R^\infty, D_0, S_a\}$$

■ Continuum:

- Optical models (potentials parameters),
- Fission (barrier penetrabilities models)...
- Level densities...

$$\vec{x} = \{\beta_2, a_c, d_c, V, W, \dots\}$$

■ Multigroup

- Cross sections
- Spectra, nu-bar

$$\vec{x} = \sigma_g^r, \chi_g, \nu \dots$$

■ Description of \vec{y}

- Microscopic experiments (transmission, capture yields, fission ...)
- Integral experiments dedicated to nuclear data (ICSBEP...)

■ Description of $\vec{t}(M, \vec{x}, \vec{\theta})$

■ To simulate experiments:

- $\vec{t} \rightarrow$ need of a functional \rightarrow link between models and measurements
- $\vec{\theta} \rightarrow$ Experimental parameters \rightarrow systematic uncertainties
- Data reduction description \rightarrow from counts to \vec{t}

Data Assimilation framework for evaluation using integral experiments

$$\chi_{GSL}^2 = (\vec{x} - \vec{x}_m)^T M_x^{-1} (\vec{x} - \vec{x}_m) + (\vec{E} - \vec{C}(\sigma(\vec{x})))^T M_E^{-1} (\vec{E} - \vec{C}(\sigma(\vec{x})))$$

$$\vec{y} \rightarrow \vec{E}$$

→ Integral Exp.

$$\vec{x} \rightarrow$$

$$\vec{x} = \{\gamma_{a\lambda}, E_\lambda, a_c, R'\}$$

$$\vec{x} = \{\Gamma_a, a_c, R^\infty, D_0, S_a\}$$

$$\vec{x} = \{\beta_2, a_c, d_c, V, W, \dots\}$$

$$\vec{x} = \sigma_g^r, \chi_g, \nu \dots$$

$$\vec{G} = \frac{\partial \vec{C}}{\partial \vec{x}} = \frac{\partial \vec{C}}{\partial \vec{\sigma}} \otimes \frac{\partial \vec{\sigma}}{\partial \vec{x}}$$

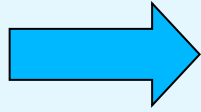
Conrad

Sammy,
Refit,
TALYS...

APOLLO2/CRONOS2, ERANOS/PARIS,
APOLLO3, MCNP, Tripoli-4

ND Treatment

Validation and/or
Data Assimilation



$$\vec{x} = \{\gamma_{a\lambda}, E_{\lambda}, a_c, R', OMP, \dots\}$$

+BIASES

and/or

$$\sigma_g^r \text{ and } \chi_g, \nu \dots$$

+ TRENDS

“Public” Integral Experiments

- Mini-Inca (ILL)
- ICSBEP / IRPHe
- ...

Used as validation for evaluation $\rightarrow C/E \sim 1$

Using benchmark in relative to focus on some reaction : $^{238}\text{U} (n, n')$

Take care of experimental correlation between ICSBEP series

Additional Integral Experiments

- Irradiation Exp.
PROFIL/MANTRA
- Oscillation Exp.
MINERVE/DIMPLE
- ...

High Precision (Oscillation : 1-3% ; PROFIL : ~2%)

Flexibility in terms of neutronic spectrum

\rightarrow Deconvolution of energy domain

Best Knowledge coming from

- Microscopic Measurements
- Nuclear Reaction Models

“Public” Integral Experiments

- Mini-Inca (ILL)
- ICSBEP
- ...

Breakthrough

- Covariances [0eV;20MeV]
- Evaluation methodologies
- Understanding of discrepancies
- Covariance methodologies
- Reduction of Uncertainties

Additional Integral Experiments

- Minerve
- PROFIL
- ...

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Covariances Matrices evaluation on ^{239}Pu Determination of



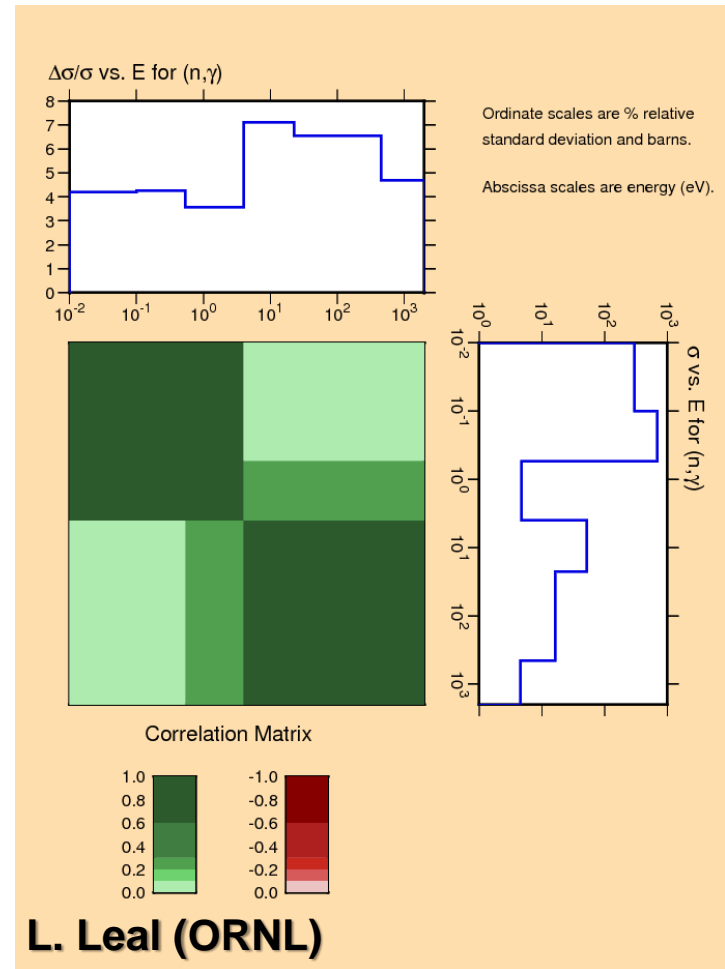
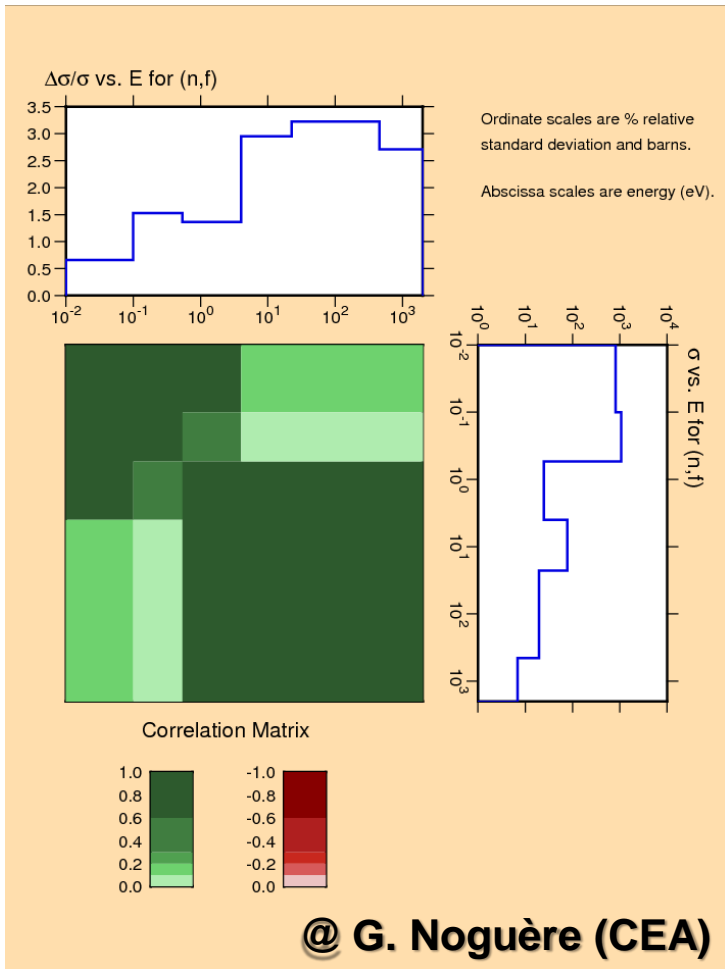
Matrices



²³⁹PU COVARIANCE MATRICES (MICROSCOPIC KNOWLEDGE)

Resolved Resonance Range (SG34 and JEFF-3.2)

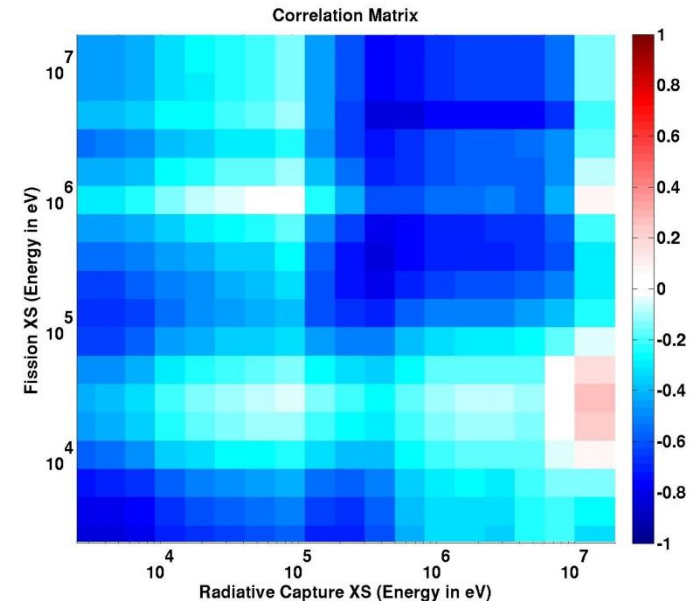
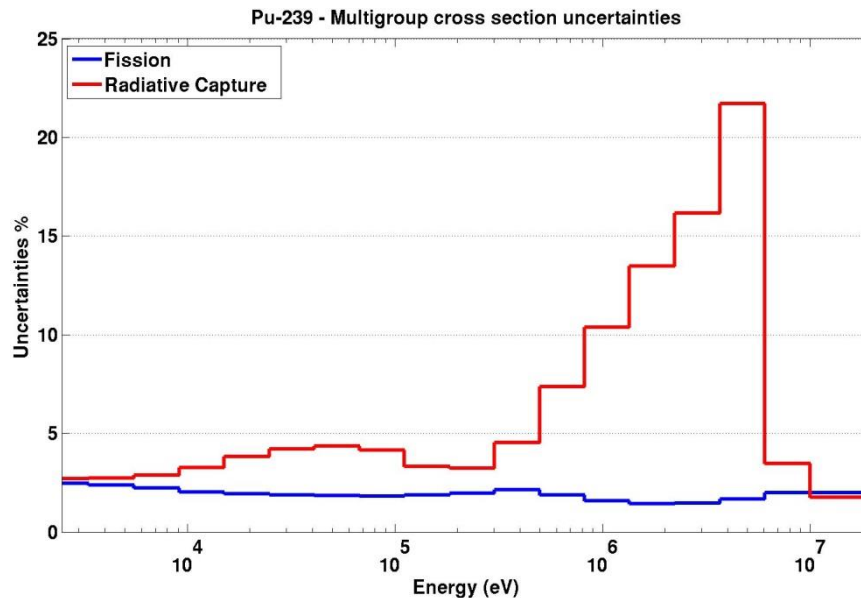
- Final uncertainties dominated by normalization accuracy introduced in the Marginalization procedure (0.5-3% for the fission cross section and 4-9% for the capture cross section)





Covariances in the continuum (COMAC-V0.1)

- Construction of an a-priori based on JEFF-3.2 cross sections
- Systematic uncertainties on fission and capture XS, based on “International Evaluation of Neutron Cross Section Standards” by Carlson *et al.* (CRP Report)



- Same conclusions : a few % of uncertainties with high correlations



²³⁹Pu COVARIANCE MATRICES (MICROSCOPIC KNOWLEDGE)

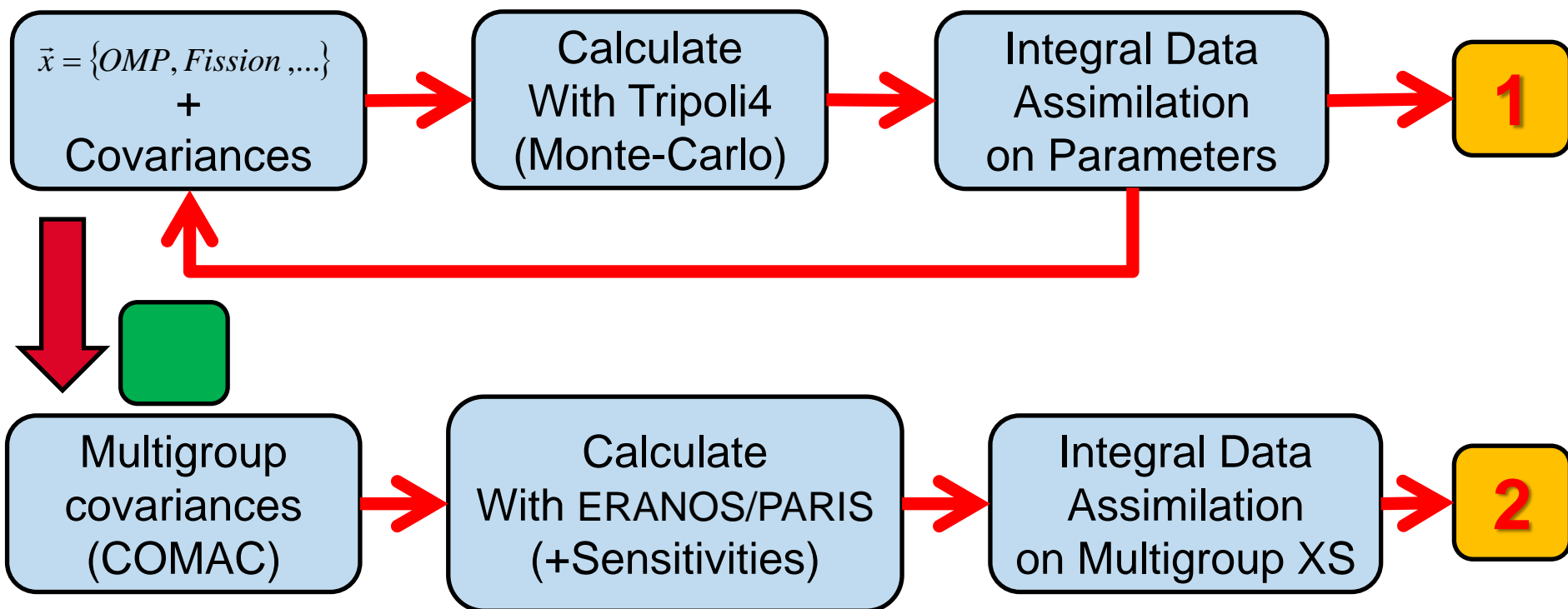
- Covariances on Nuclear model parameters and related Cross sections
- High influence of systematic uncertainties
 - High and long range correlations
 - Uncertainties around 0.5-10 % (²³⁹Pu Capture high even in thermal range)
- RRR/URR/OM treated separately
 - Importance of cross-correlations between reactions / energy ranges

Still important uncertainties
→ Needs for integral constraints

- Short term → Add integral information + Additional energy ranges constraints
- Long term → New microscopic/integral experiments even for well-known isotopes (Normalization/background issues, URR, angular distributions, ...)
- Long term → More microscopic ingredients (less “free” parameters)



■ JEZEBEL → define a consistent benchmark



- A. Only Cross sections and related model parameters
- B. Investigate results
- C. Add other nuclear data (PFNS, nu, etc...)
- D. Propagate to a Fast Reactor

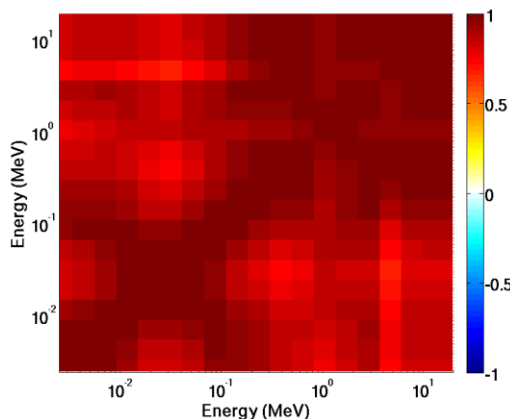


^{239}Pu COVARIANCE MATRICES (PUBLIC INTEGRAL EXPERIMENTS)

“Public” Integral Experiments

☐ ICSBEP (JEZEBEL)

Prior Correlation on Fission

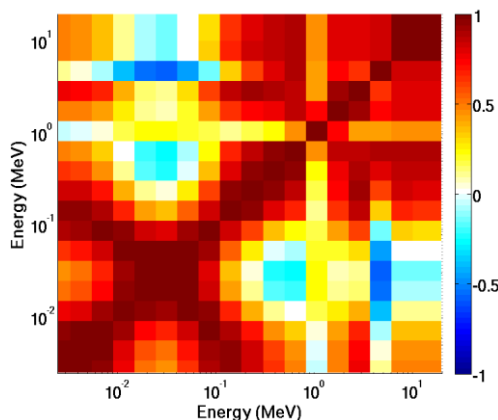


Nuclear model parameters Data Assimilation

Multigroup cross section Data Assimilation

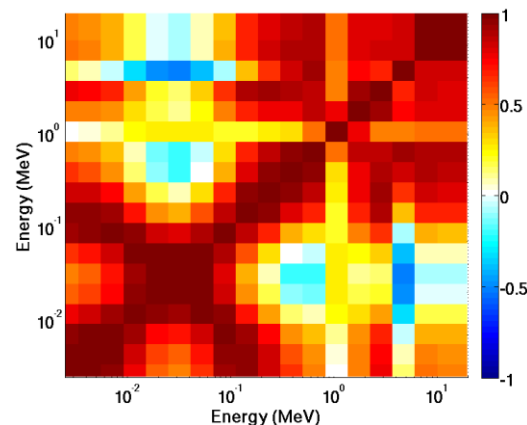
$$\vec{x} = \{OMP, Fission, \dots\}$$

Post Correlation on Fission with Feedback on Parameters



$$\sigma_g^r$$

Post Correlation on Fission with Feedback on MultiGroup XS



Correlation Matrices are almost equivalent:

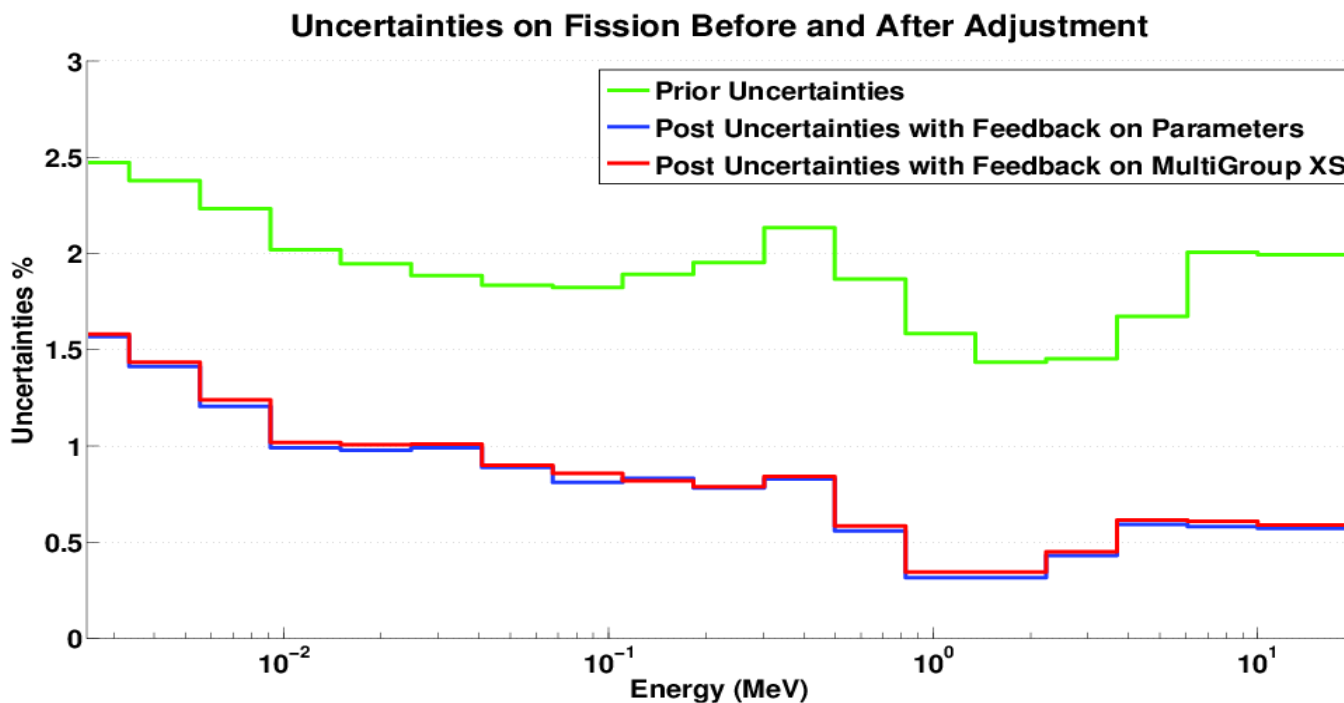
$$|C(\text{param} \rightarrow \sigma_g) - C(\sigma_g)|_{\max} \sim 0.1$$



²³⁹Pu COVARIANCE MATRICES (PUBLIC INTEGRAL EXPERIMENTS)

“Public” Integral Experiments

☐ ICSBEP (JEZEBEL)



Data Assimilations using multigroup cross sections or nuclear reaction model parameters seem to be very consistent



239PU COVARIANCE MATRICES (PUBLIC INTEGRAL EXPERIMENTS)

Effect on a Fast Reactor (large size core)

Uncertainties on Keff :

With COMAC-V0.1 :

| Isotope | FISSION | CAPTURE | ELASTIC | INELASTIC | NXN | NU | DISTRIBUTION | TOTAL |
|---------|---------|---------|---------|-----------|--------|--------|--------------|---------|
| Pu239 | 782.45 | 234.45 | -14.24 | 67.63 | -12.39 | 109.76 | 199.06 | 850.35 |
| TOTAL | 955.27 | 598.58 | 30.30 | 449.18 | -43.25 | 157.94 | 253.96 | 1249.44 |

With COMAC-V0.1 + JEZEBEL :

| Isotope | FISSION | CAPTURE | ELASTIC | INELASTIC | NXN | NU | DISTRIBUTION | TOTAL |
|---------|---------|---------|---------|-----------|--------|--------|--------------|--------|
| Pu239 | 304.31 | 176.87 | -18.03 | 50.03 | -7.93 | 56.36 | 144.41 | 387.34 |
| TOTAL | 626.83 | 578.46 | 28.21 | 446.87 | -42.19 | 126.78 | 213.83 | 994.00 |

Major changes due to new ²³⁹Pu covariance

→ ²³⁸U next

→ Add dedicated integral experiments (PROFIL)

→ All usual suspects (Fe...)

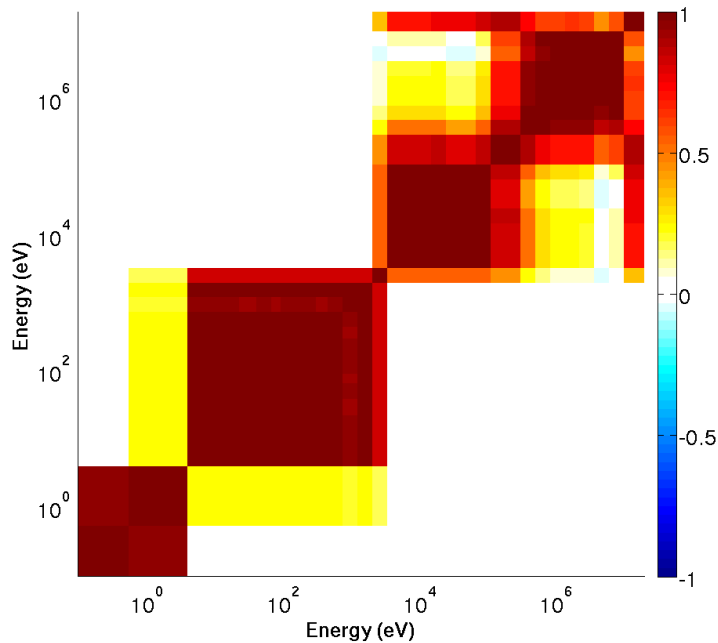


²³⁹Pu COVARIANCE MATRICES (ADDITIONAL INTEGRAL EXPERIMENTS)

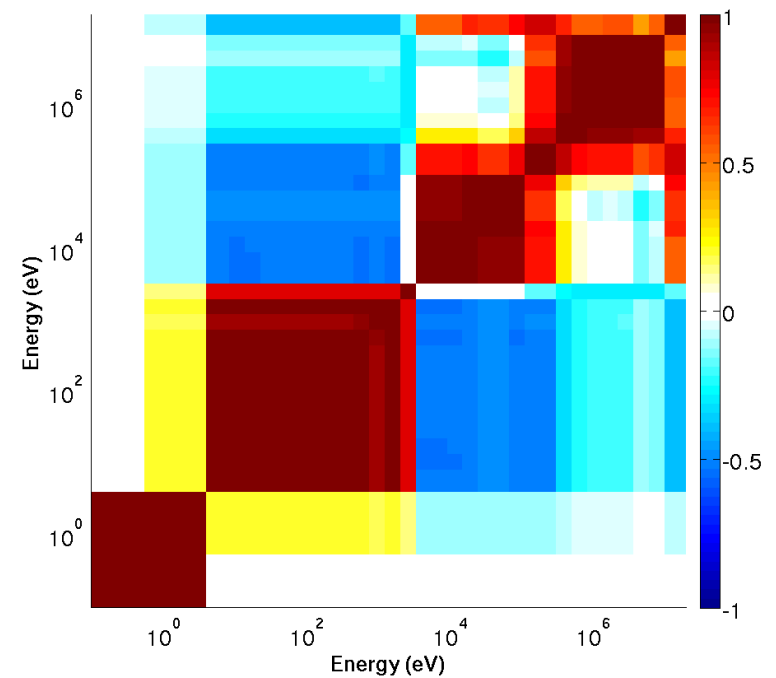
Additional Integral Experiments

□ PROFIL experiments (CEA Marcoule)

Correlation Before between CAPTURE(Pu239) and CAPTURE(Pu239)



Correlation After between CAPTURE(Pu239) and CAPTURE(Pu239)

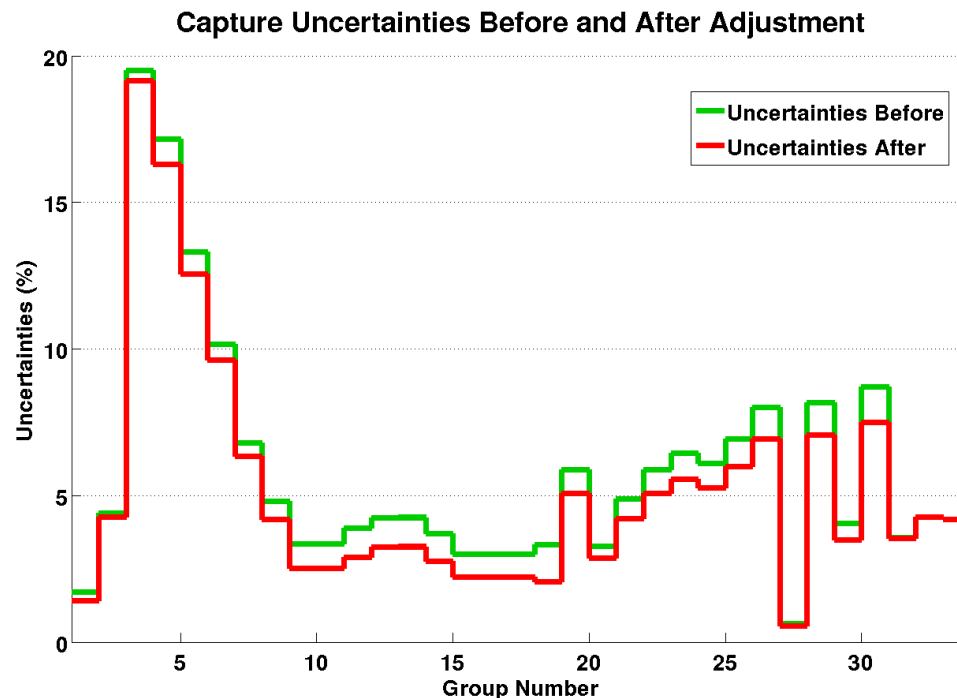




^{239}Pu COVARIANCE MATRICES (ADDITIONAL INTEGRAL EXPERIMENTS)

Additional Integral Experiments

□ PROFIL experiments (CEA Marcoule)



→ Slight reduction of the uncertainties but large anti-correlations appear between the keV and the MeV energy regions
 → Additional experiments are required for the thermal region

IMPOSING CONSTRAINTS ON MODELS INTEGRAL EXPERIMENTS

- Reduction of uncertainties with dedicated integral experiments is major (Factor 5-10)
- Work presented here on multigroup cross sections and nuclear reaction model parameters
- Choice of integral experiments is crucial to disentangle nuclear data sensitivities
 - Use integral experiments sensitive to different reactions or parameters
 - Relative integral experiments (reflector effect instead of reactivity...)
- Difficulty arises if :
 - Parameters are not well chosen or forgotten (PFNS, angular distributions ...etc...)
 - Spurious Integral experiment (as for microscopic ones) with hidden error
 - Correlation between experiments are neglected (ICSBEP series ...)
- Traditional questions arises → “old” experiments, effect is diluted on several ND,.. etc
- JEZEBEL is quite unique...
- Investigate cases with bad C/E or if two different evaluations are giving same C/E



**Sometimes true but
CIELO and SG39 could give answers**

- Several kind of Nuclear Data
- Several kind of Nuclear Reaction Models
- Several kind of Experiments
- Several kind of Covariance Matrices

- Progress on Methodologies needed:
 - Data assimilation techniques
 - Adding physical constraints (On several models)

- Progress on Experiments needed:
 - Reduction of systematic uncertainties for microscopic measurements
 - Integral experiments to target limited energy domain / reactions / isotopes

- Progress on Nuclear models needed:
 - Microscopic models
 - Avoid compensations

- Needs to define Covariance estimation benchmarks:**
 - Fixed experiments
 - Fixed a priori (on parameters and/or cross section & uncertainties)
 - Incremental complexity
 - Compare covariance evaluation methodologies

