

DE LA RECHERCHE À L'INDUSTRIE



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**Investigation of  
Prompt Fission Neutron and Gamma Spectra  
with their covariance matrices.  
Application to  $^{239}\text{Pu}+n_{\text{th}}$ ,  $^{238}\text{U}+n_{1.8\text{MeV}}$ ,  $^{235}\text{U}+n_{\text{th}}$**

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NEMEA-7 / CIELO

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- Activities around PFNS
- PFNS and PFGS from Fission Fragment deexcitation
- Covariance matrices
- Conclusion, Outlook

## ■ Activities around PFNS

### 1. Model for spectra

Monte Carlo simulation of the fission fragment deexcitation  
(**Fifrelin code**)

→ *Allows to estimate fission observables (spectra, multiplicities, correlations, fission yields, ...)*

### 2. Model for quantification of covariances

Production of covariance matrices (**Conrad code**)

→ *Used for cross sections but also any kind of model (in this work: Maxwell, Watt, Madland-Nix, Fifrelin PFNS Models)*

■ PFNS and PFGS from Fission Fragment deexcitation

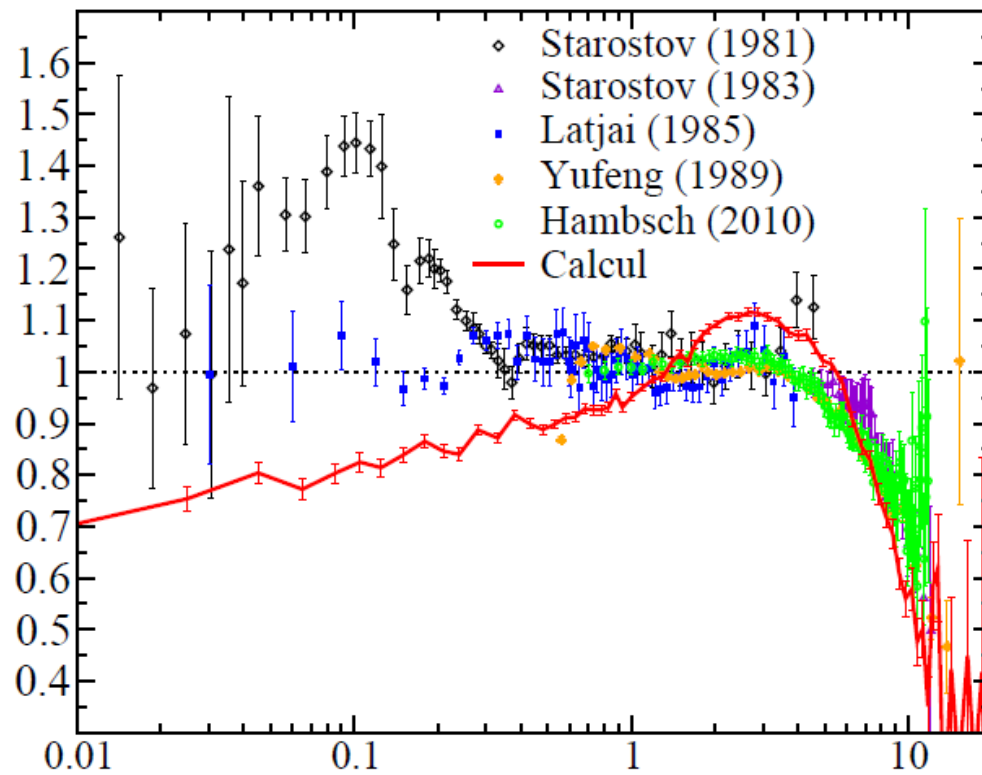
U235 / U238 / Pu239

## FIFRELIN: a Monte Carlo code simulating the fission fragment deexcitation

### *Review of the model:*

- ☯ Pre-neutron fission fragment mass sampling
- ☯ Pre-neutron fission fragment kinetic energy sampling
- ☯ Nuclear charge sampling
- ☯ Spin and parity sampling
- ☯ Excitation energy sharing after full acceleration ( $E^*=aT^2$ )
  - Ignatyuk's prescription for level density parameter ←
  - Mass dependent temperature ratio law ←
- ☯ Prompt particle (n/γ) emission (Weisskopf or Hauser-Feshbach model)

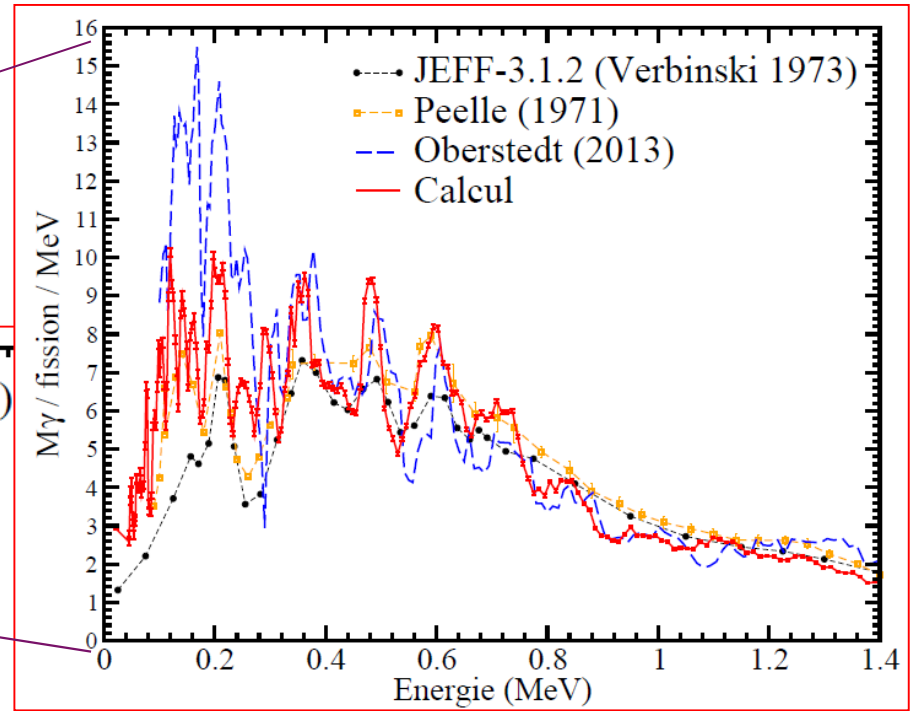
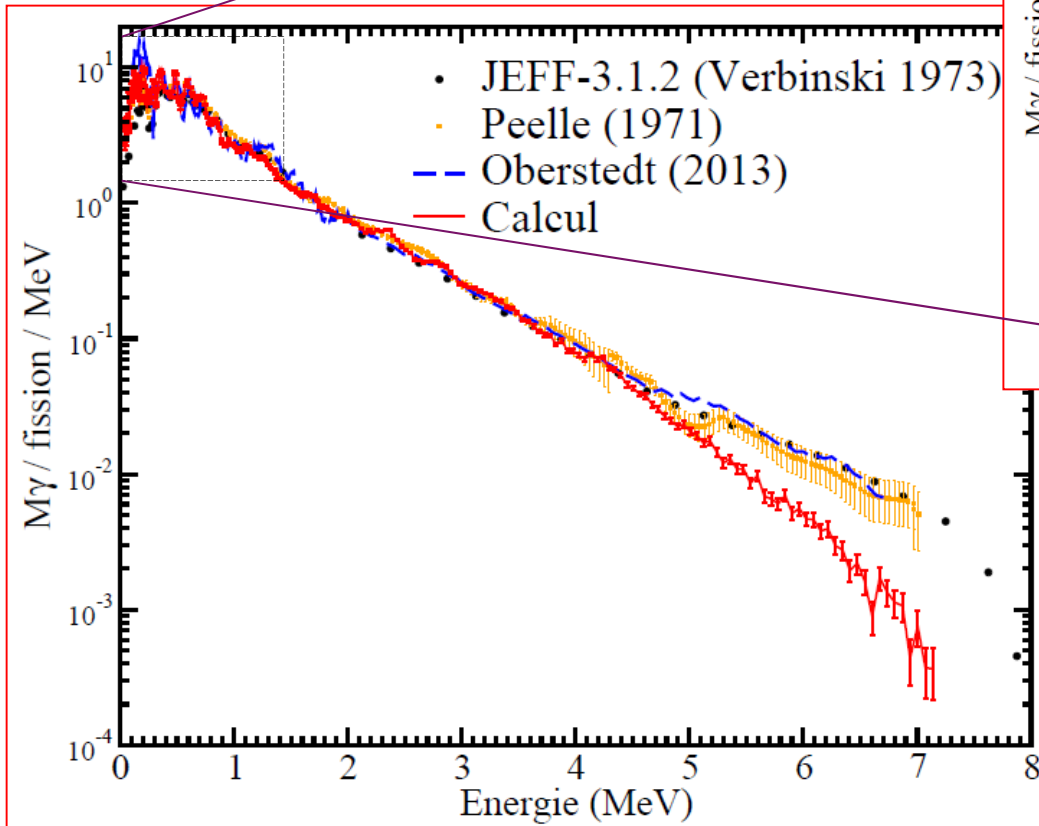
□ Thermal fission of U235 (Prompt Fission Neutron Spectrum)



D. Regnier phD (october 2013)

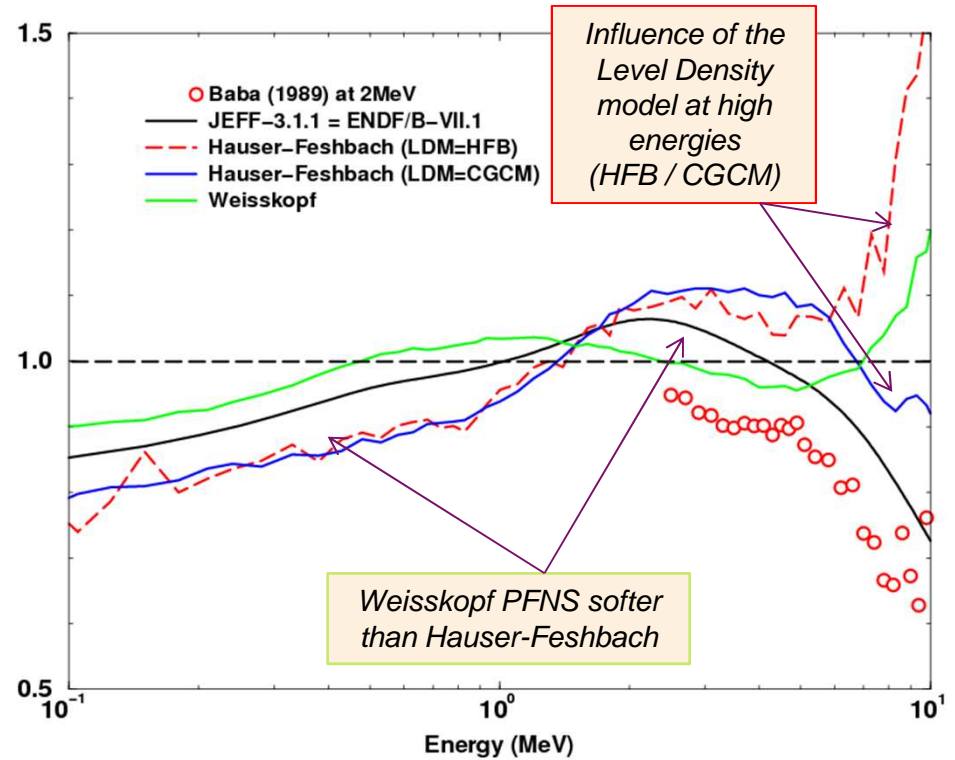
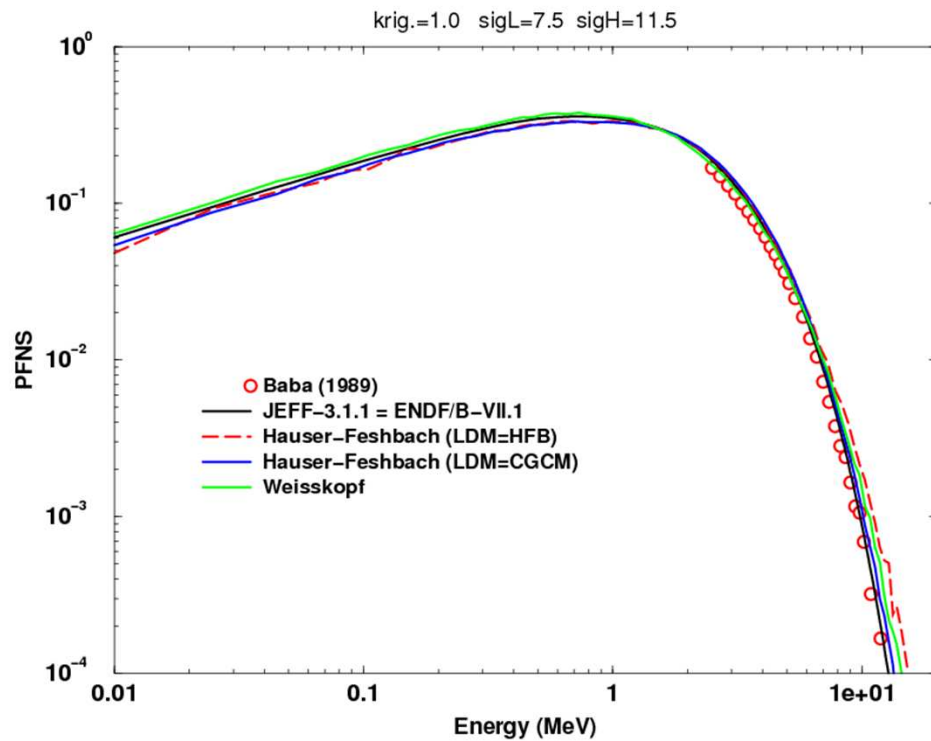
□ Thermal fission of U235 (Prompt Fission **Gamma** Spectrum)

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☐ U238 + n<sub>1.8MeV</sub> (Prompt Fission Neutron Spectrum)

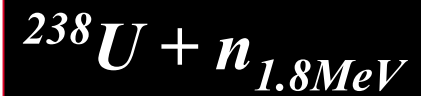
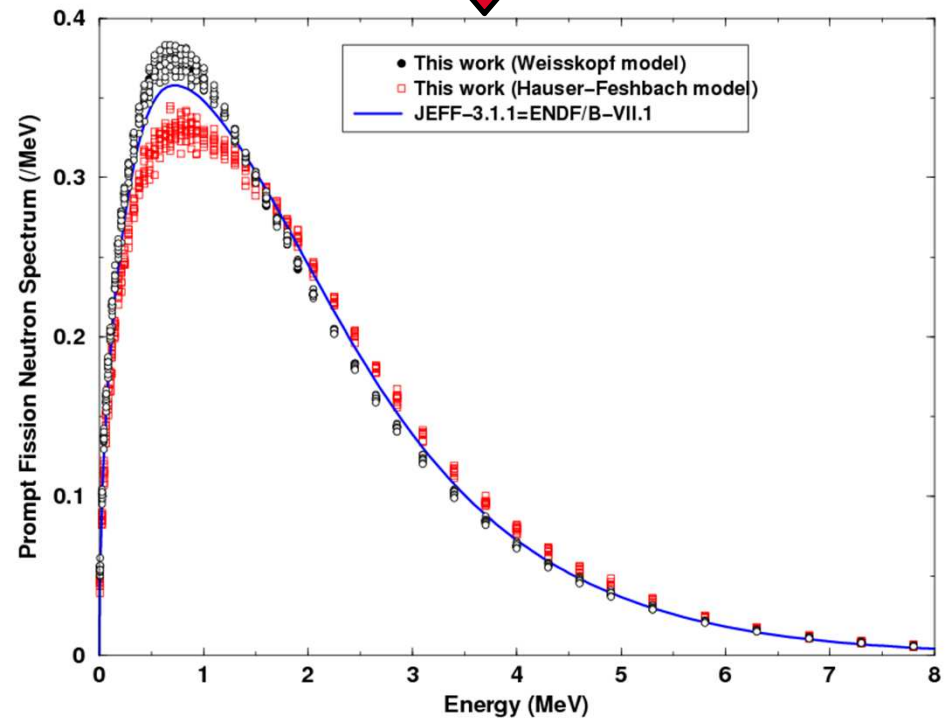
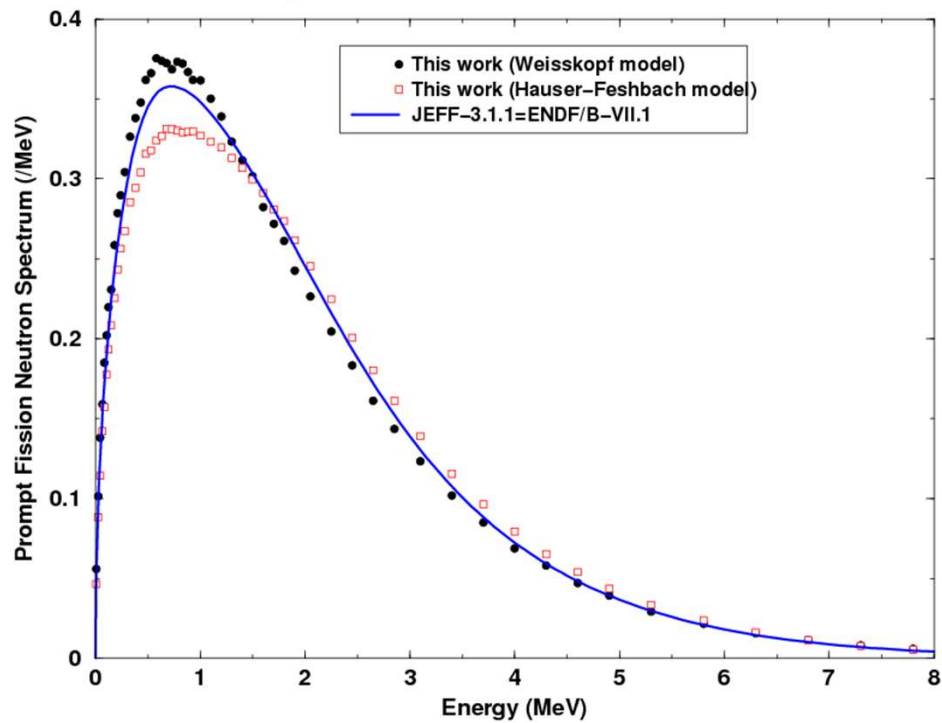
***<sup>238</sup>U + n<sub>1.8MeV</sub>***



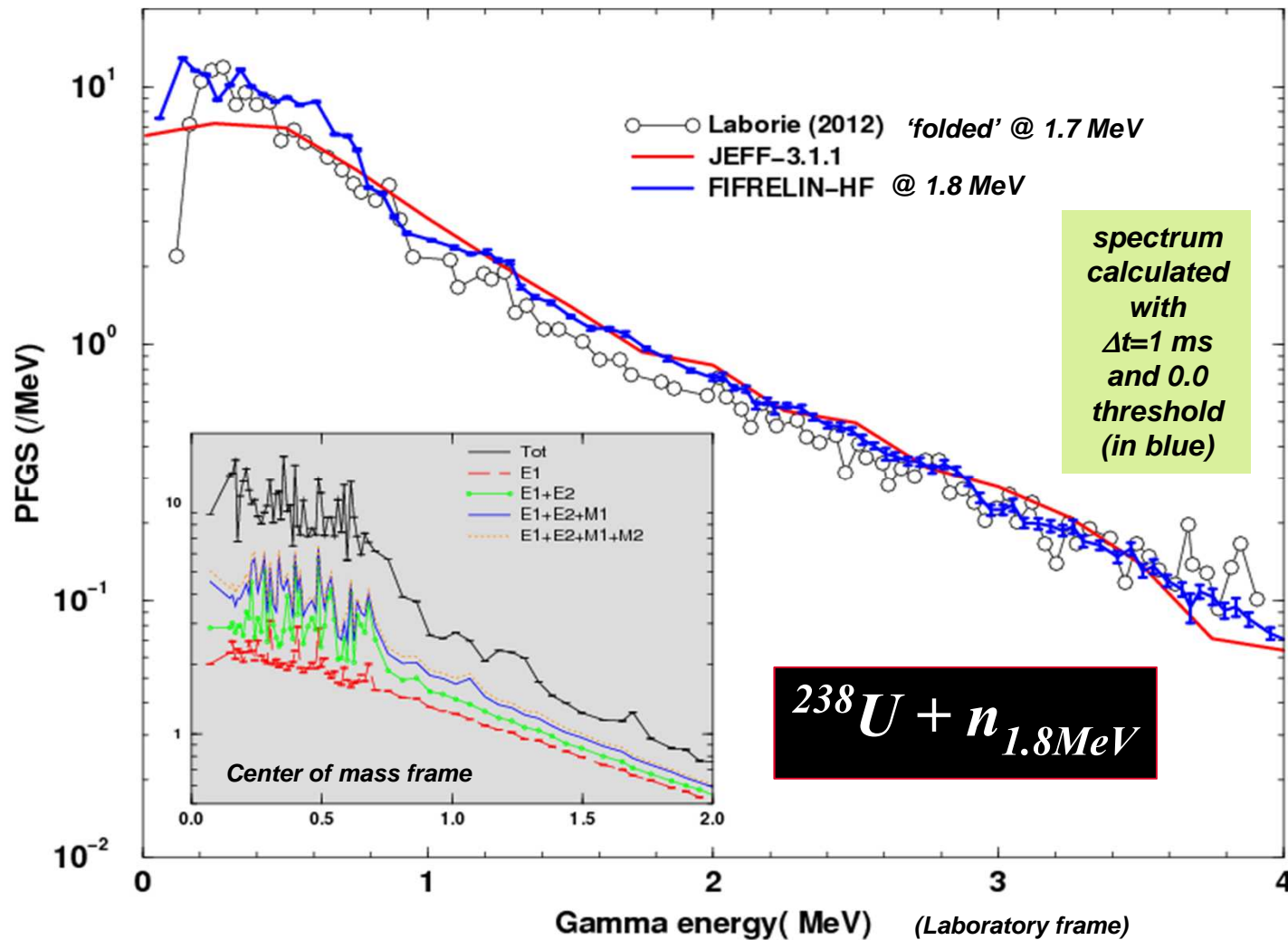


□  $U_{238} + n_{1.8MeV}$  (Prompt Fission Neutron Spectrum)

Same trend whatever the model parameters



□  $U_{238} + n_{1.8MeV}$  (Prompt Fission **Gamma** Spectrum)



□ **Prompt Fission Gamma Multiplicity (PFGM)**

- JEFF-3.1.1

$$\overline{M}_{\gamma} = 8.2$$

- FIFRELIN-HF

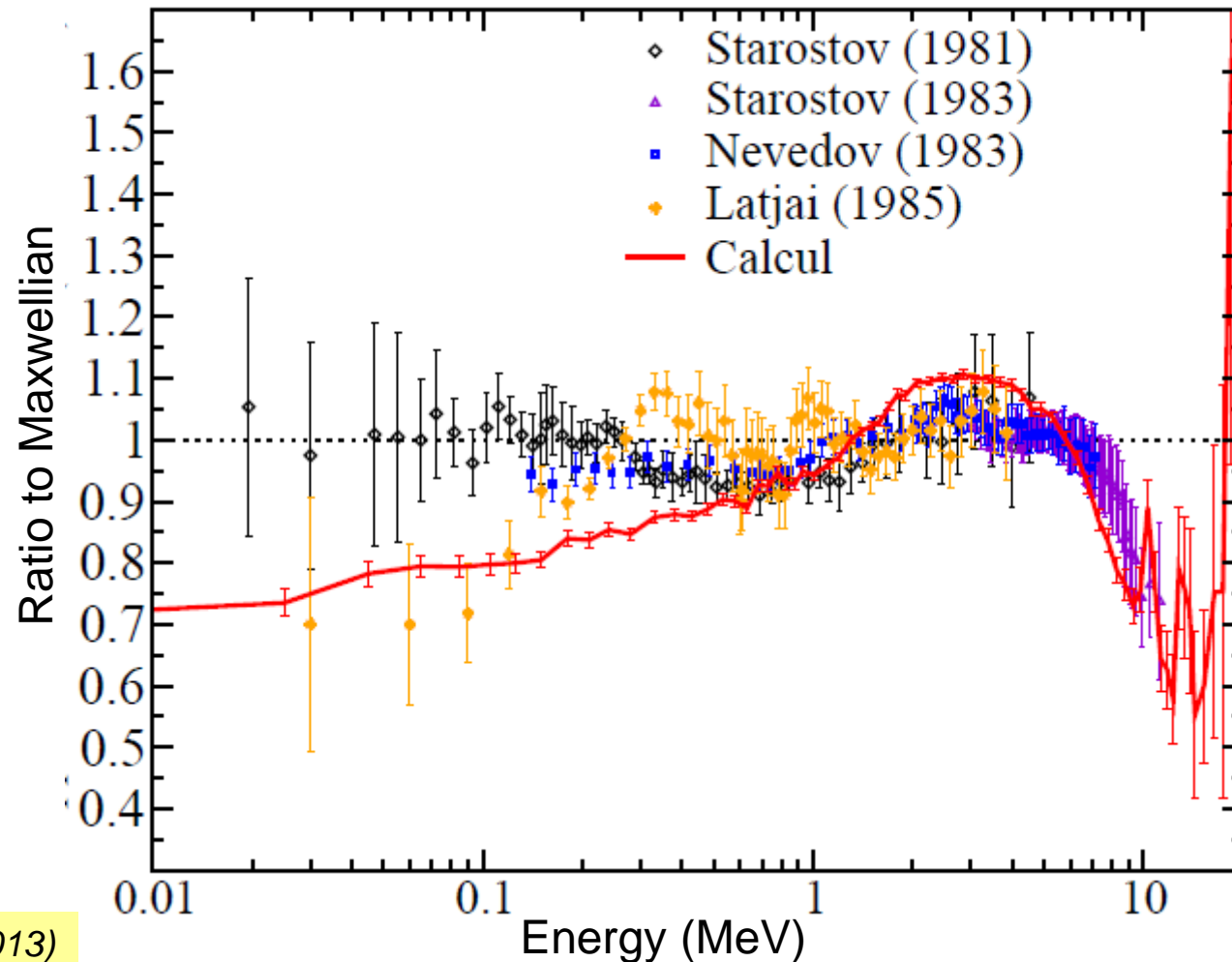
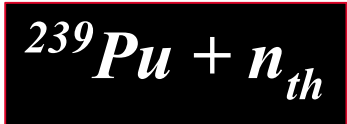
with threshold : 0,1 MeV  
time window : 10 ns

$$\overline{M}_{\gamma} \approx 9.0$$

$$\langle E_{\gamma}^{tot} \rangle \approx 7.04$$

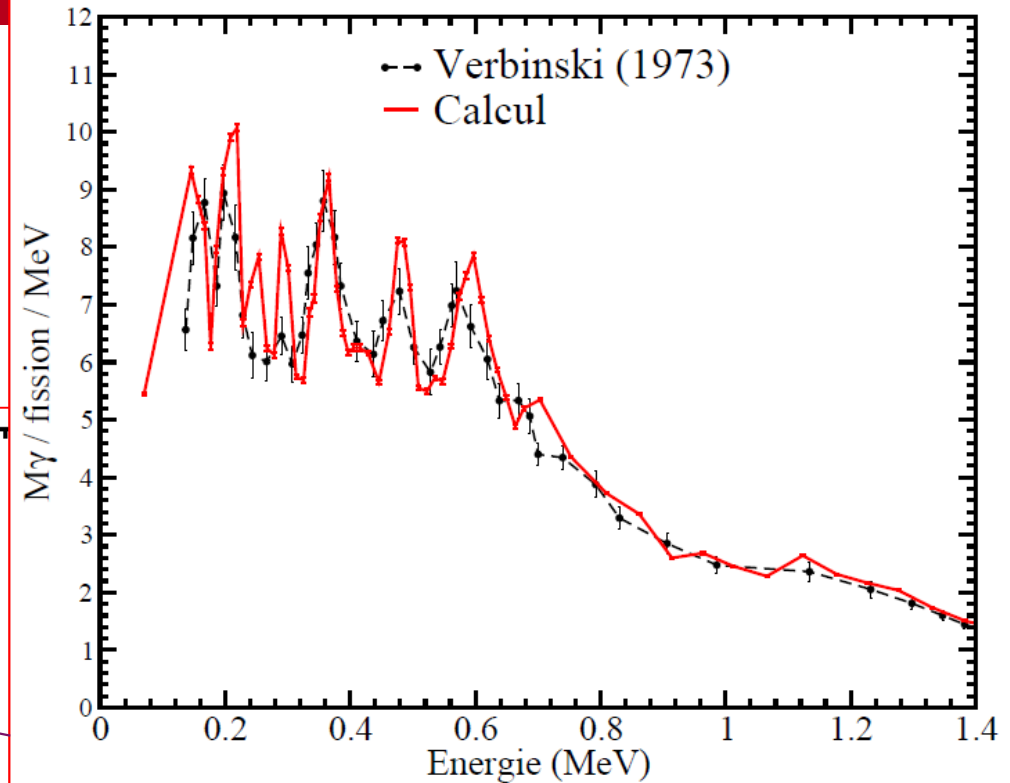
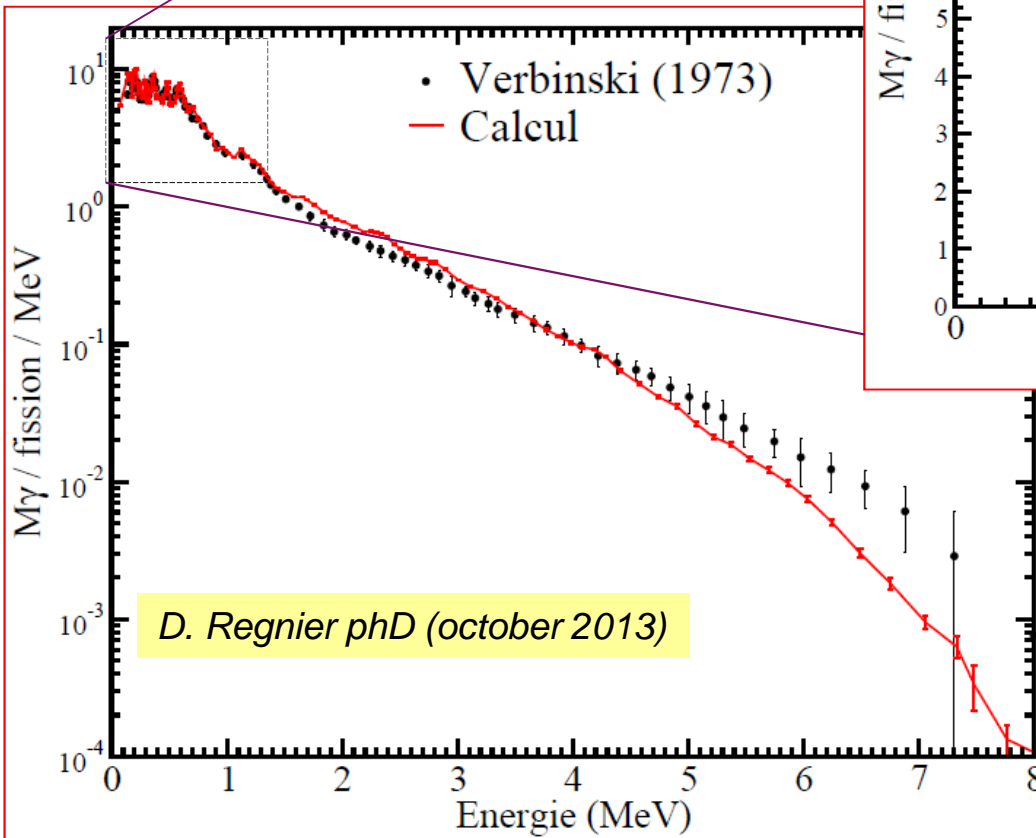
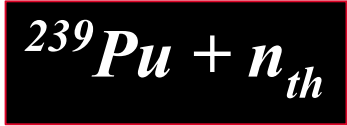
$$\langle \varepsilon_{\gamma} \rangle \approx 0.78$$

□ Thermal fission of Pu239  
(Prompt Fission Neutron Spectrum : ratio to Maxwellian T=1.38 MeV)



D. Regnier phD (october 2013)

□ Thermal fission of Pu239 (Prompt Fission **Gamma** Spectrum)



	$M_\gamma$ [ $\gamma/f$ ]	$E_{\gamma,tot}$ [MeV]	$\epsilon_\gamma$ [MeV]
Verbinski	7.23	6.81±0.3	0.94
FIRELIN	7.23	6.83	0.94

## ■ Covariance matrices (U235)

□ Model parameter adjustment in Conrad code

- *Experimental statistical uncertainty associated to the spectrum at each energy point*
- *Experimental systematic uncertainty due to normalization, detection efficiency, ...*

$$M_x^{marg} = M_x^{stat} + (G_x^T \cdot G_x)^{-1} \cdot G_x^T \cdot G_\theta \cdot M_\theta \cdot G_\theta^T \cdot G_x \cdot (G_x^T \cdot G_x)^{-1}$$

❑ Thermal fission of U235  
(Correlation matrix for Prompt Fission Neutron Spectrum)



Model	parameters	Prior (MeV)	Posterior (MeV)
Maxwell	T	1.32 ± 10%	1.32 ± 0.2% ± 2.3%
Watt	T <sub>w</sub>	0.90 ± 10%	1.06 ± 1.0% ± 15.1%
	E <sub>w</sub>	0.78 ± 10%	0.38 ± 4.2% ± 44.7%
Madland-Nix	T	1.01 ± 10%	0.96 ± 2.3% ± 15.4%
	E <sub>f</sub> <sup>L</sup>	1.07 ± 10%	1.16 ± 4.8% ± 14.9%
	E <sub>f</sub> <sup>H</sup>	0.50 ± 10%	0.25 ± 3.3% ± 36.1%

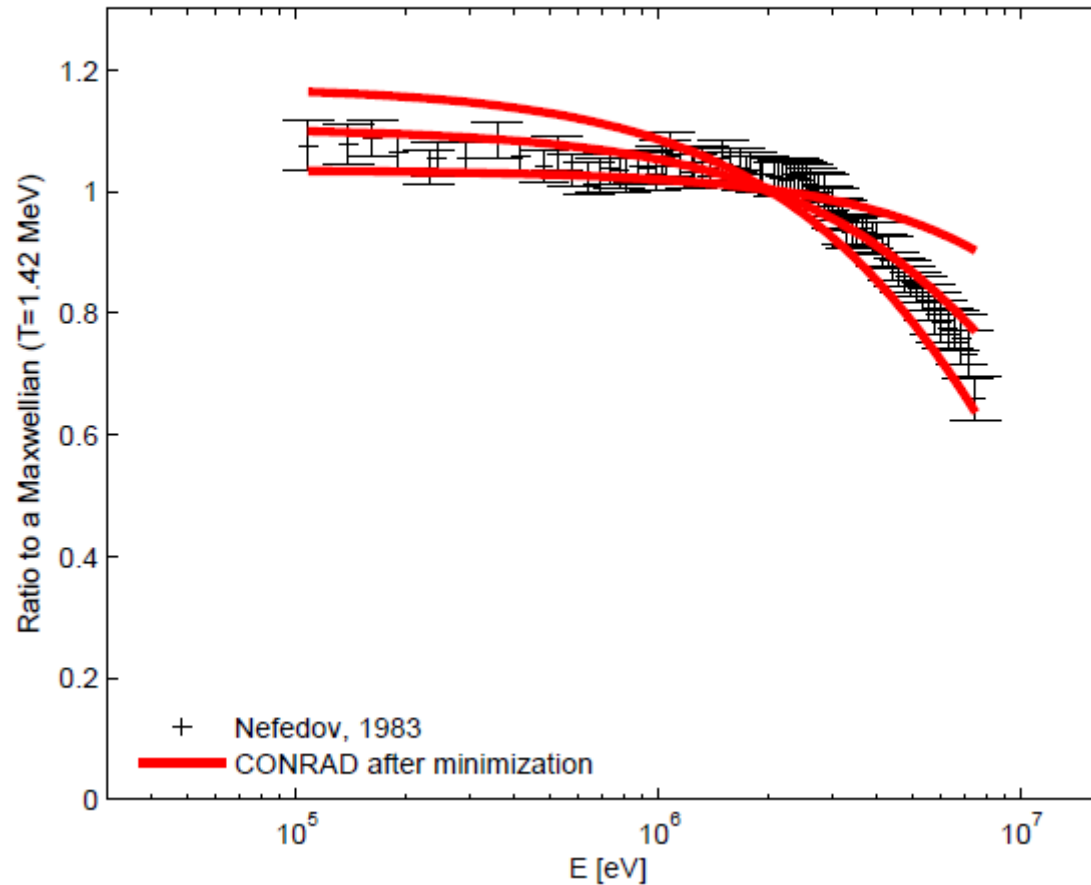
Fit based on 5 experiences

Statistical uncertainties

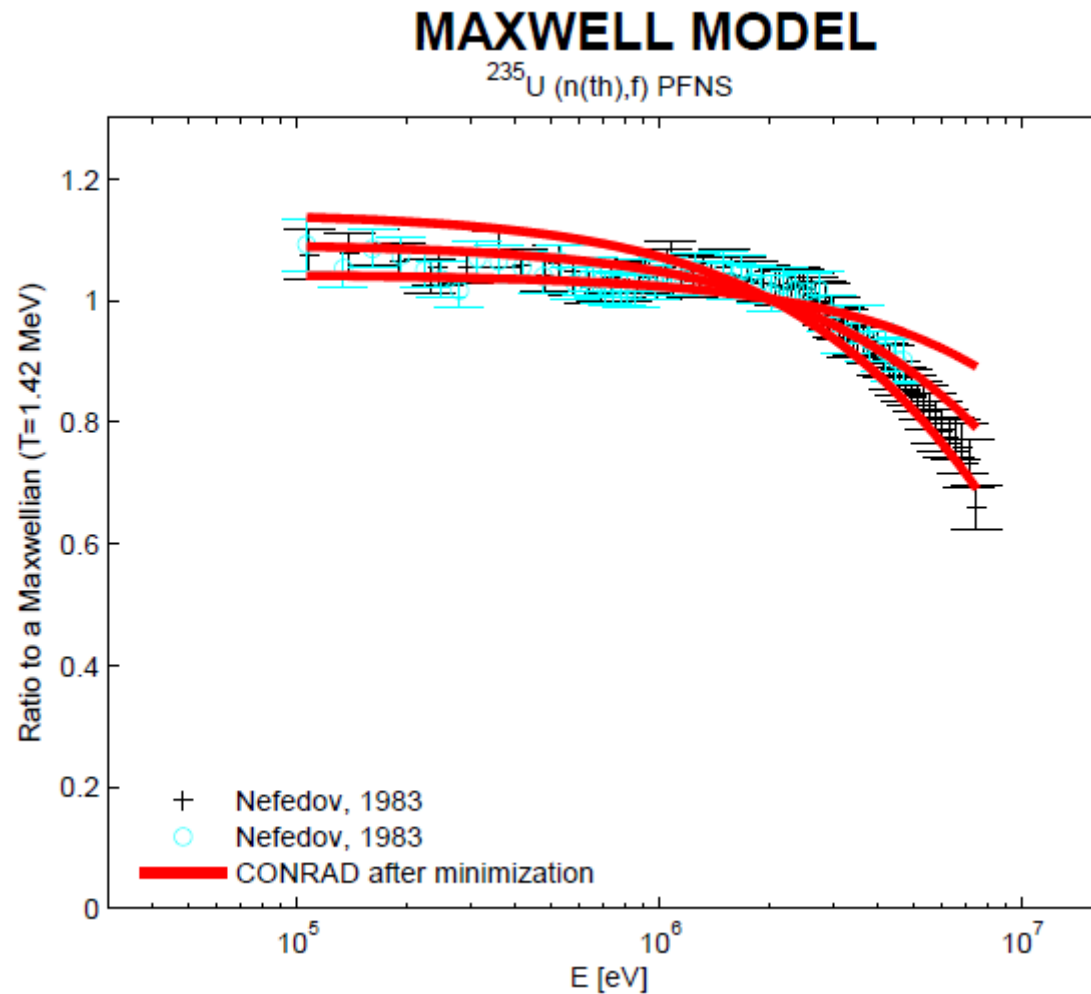
Systematic uncertainty (normalization)  
± 5%

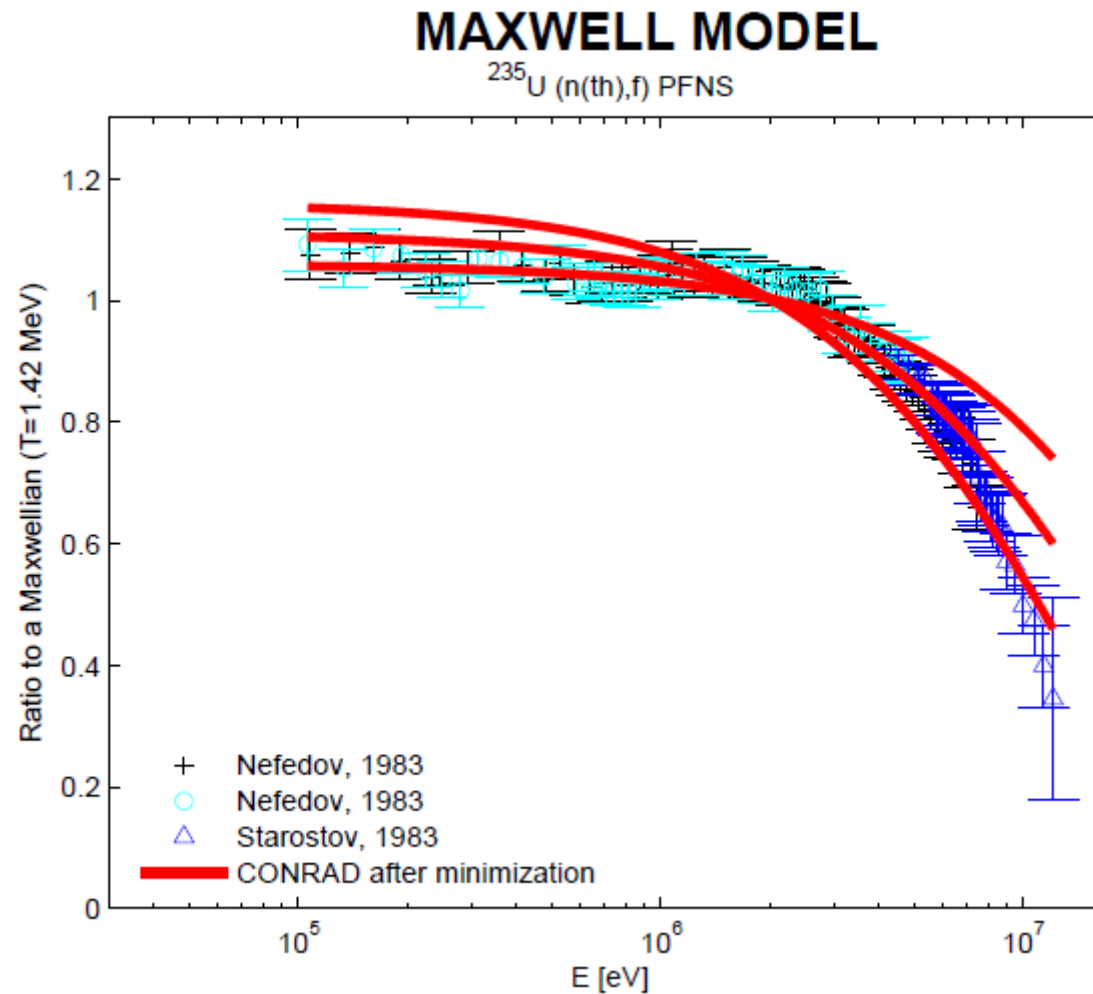
## MAXWELL MODEL

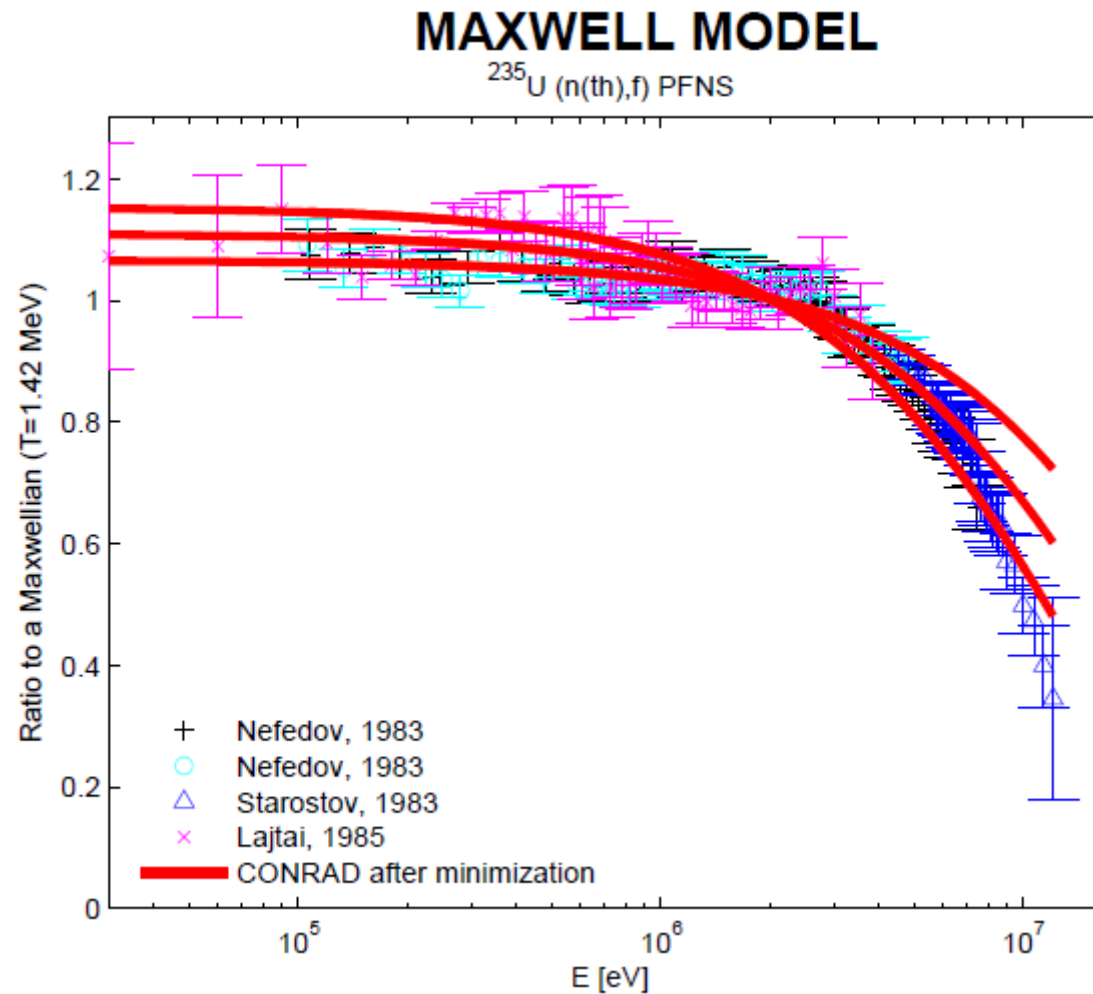
$^{235}\text{U}$  (n(th),f) PFNS



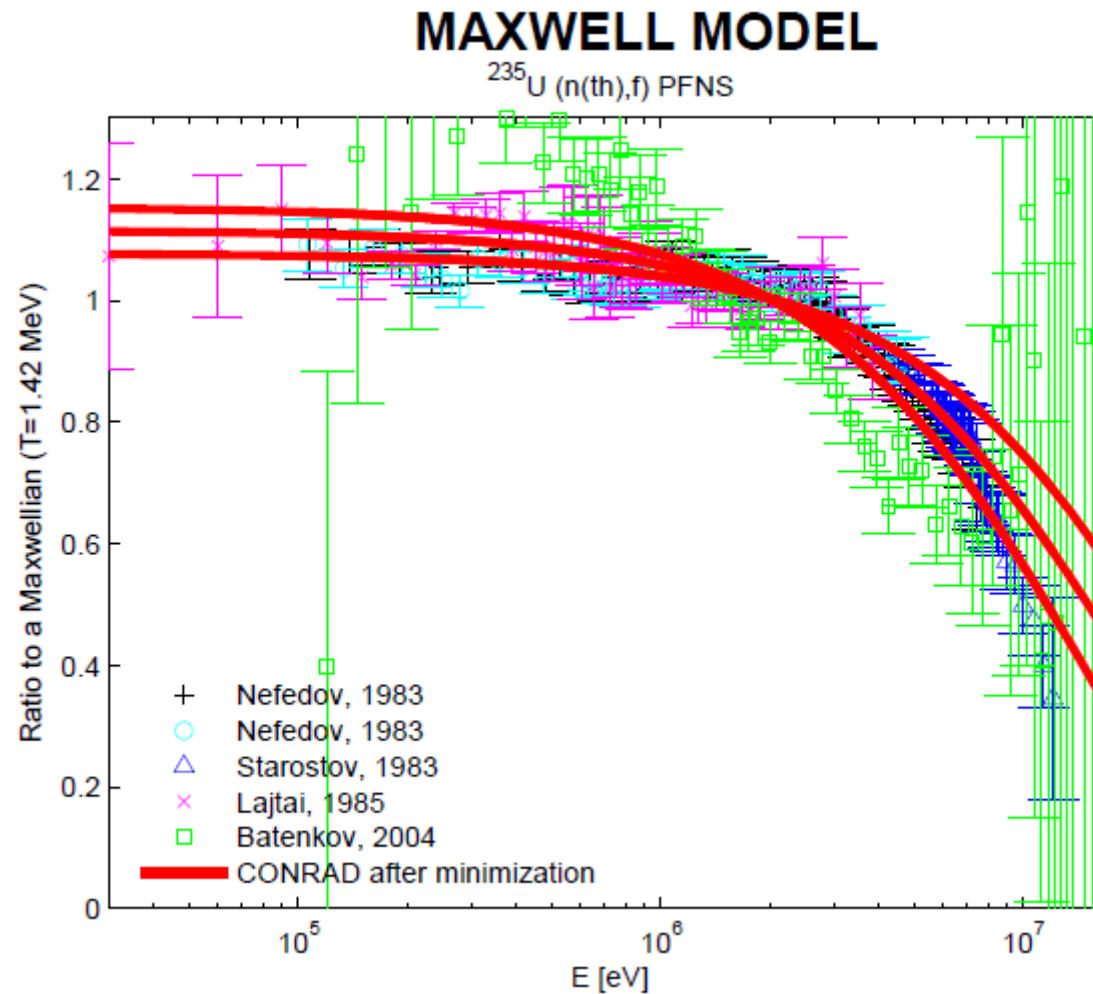




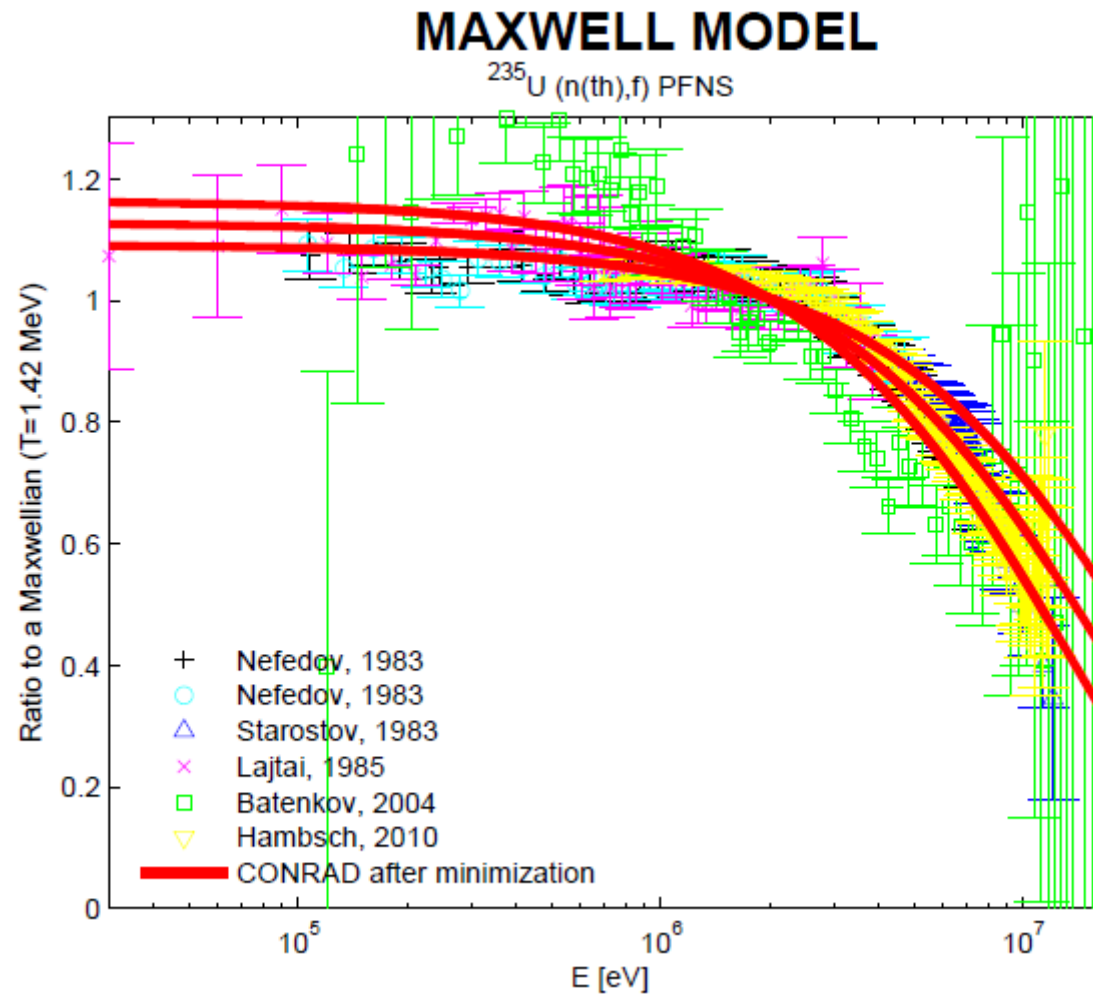


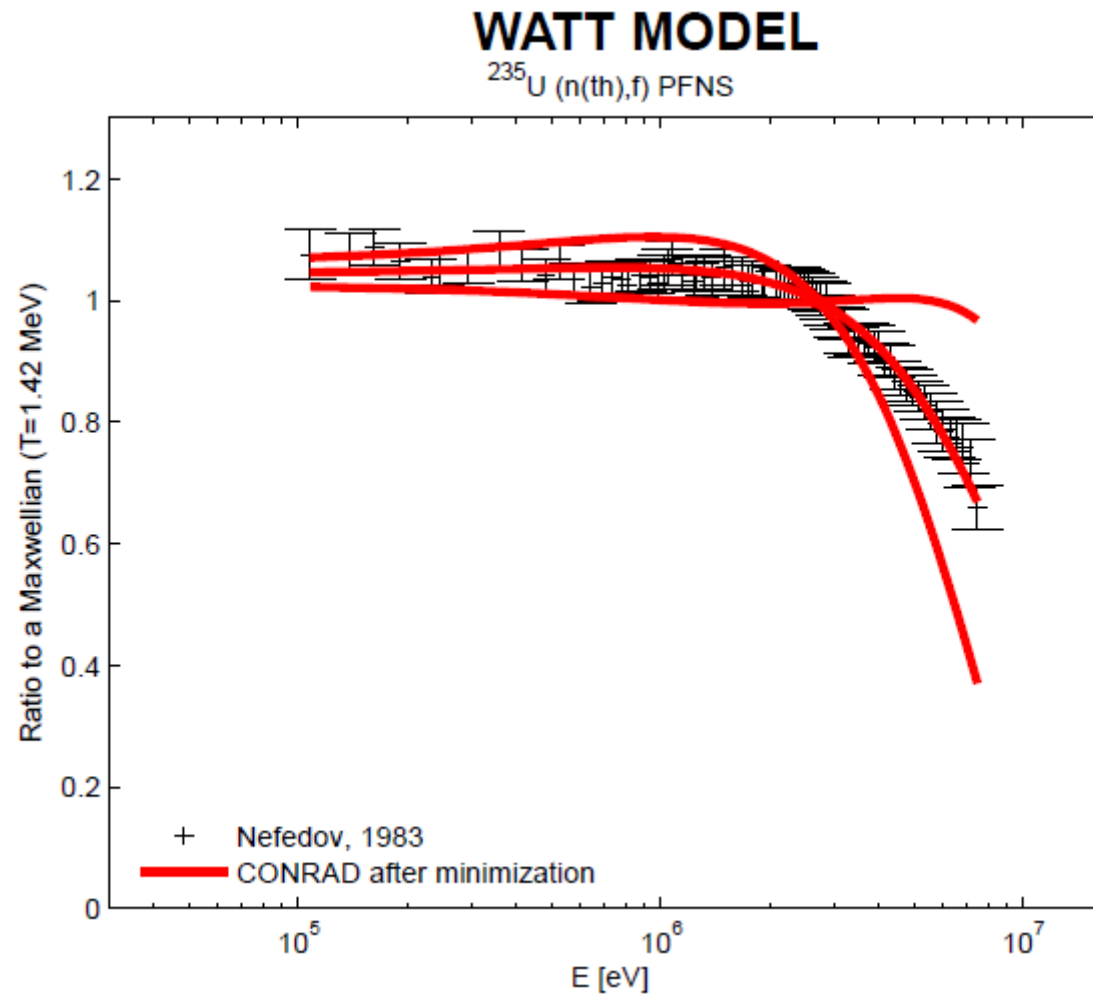


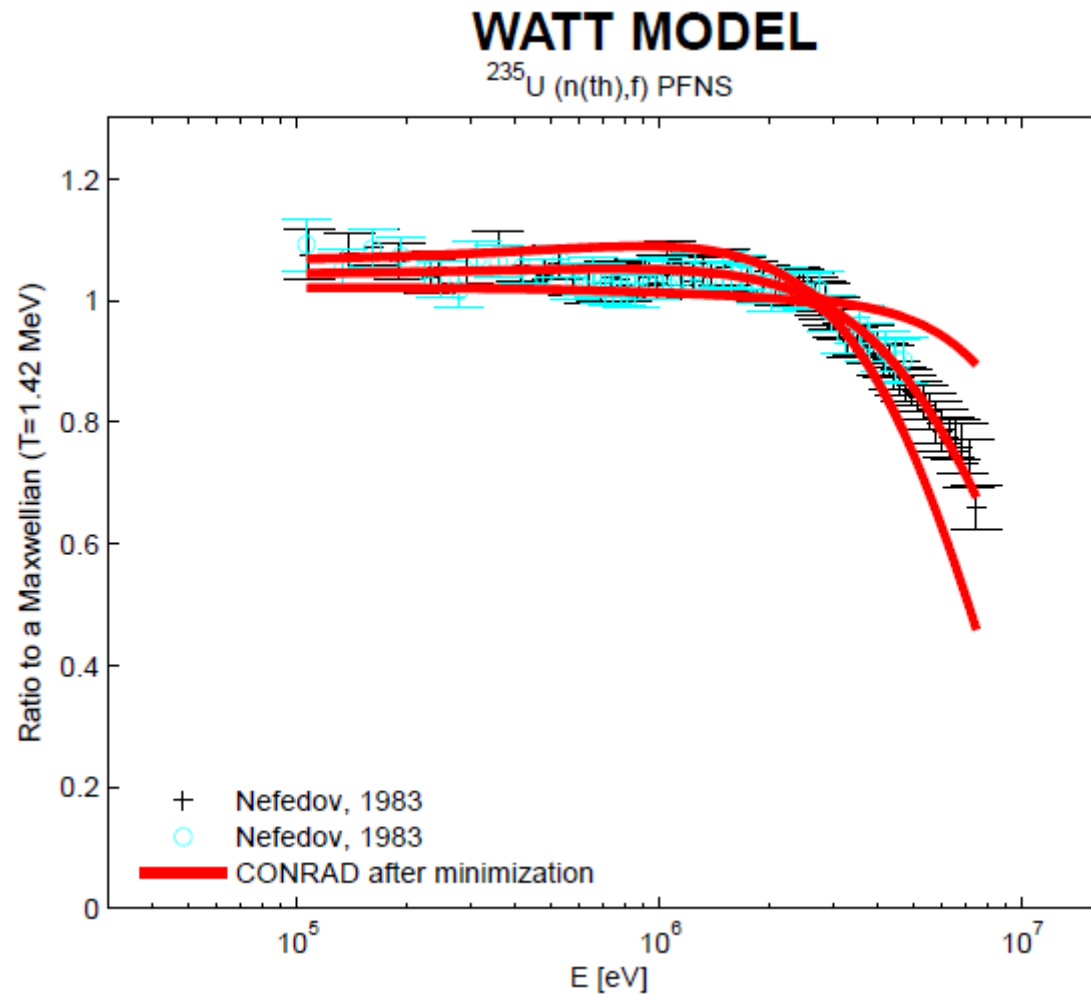
☐ Thermal fission of U235  
(Correlation matrix for Prompt Fission Neutron Spectrum)

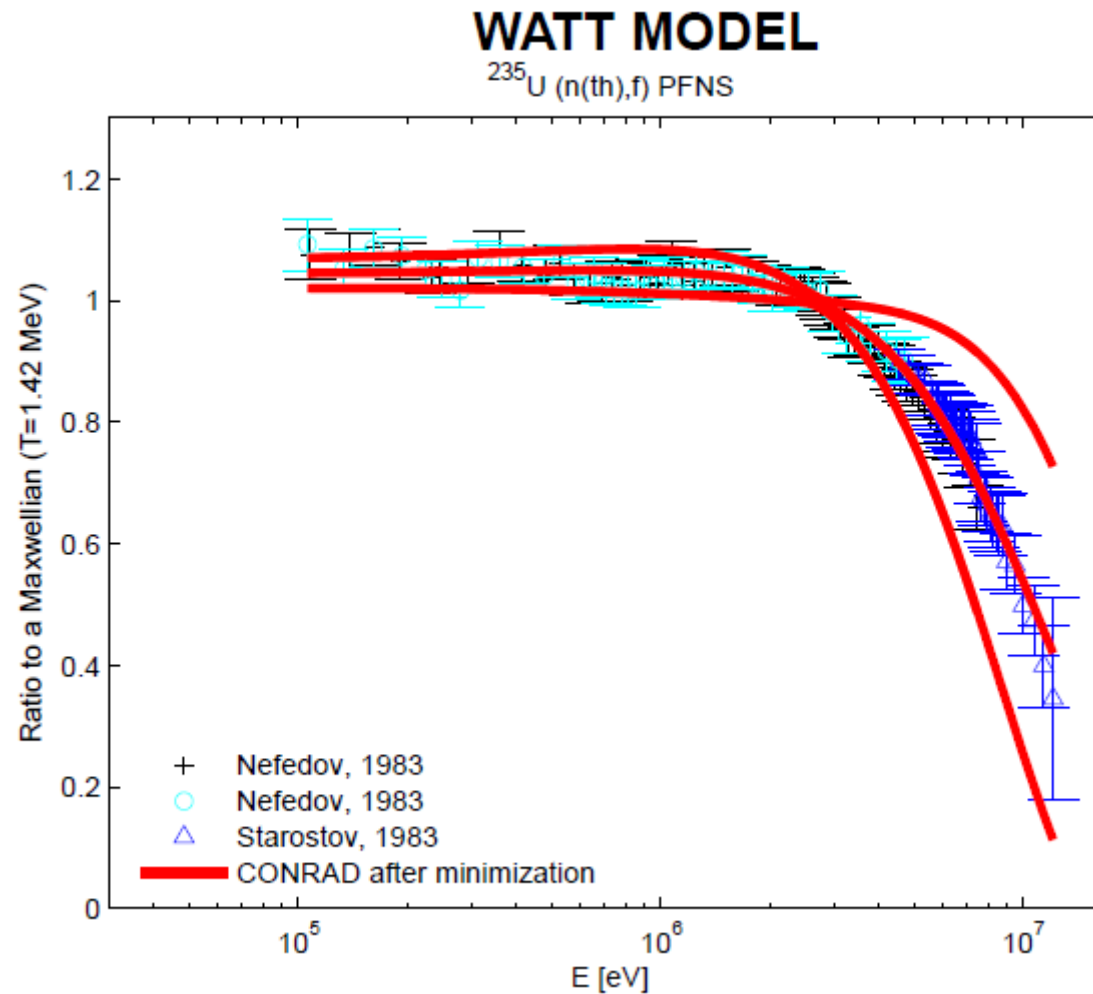


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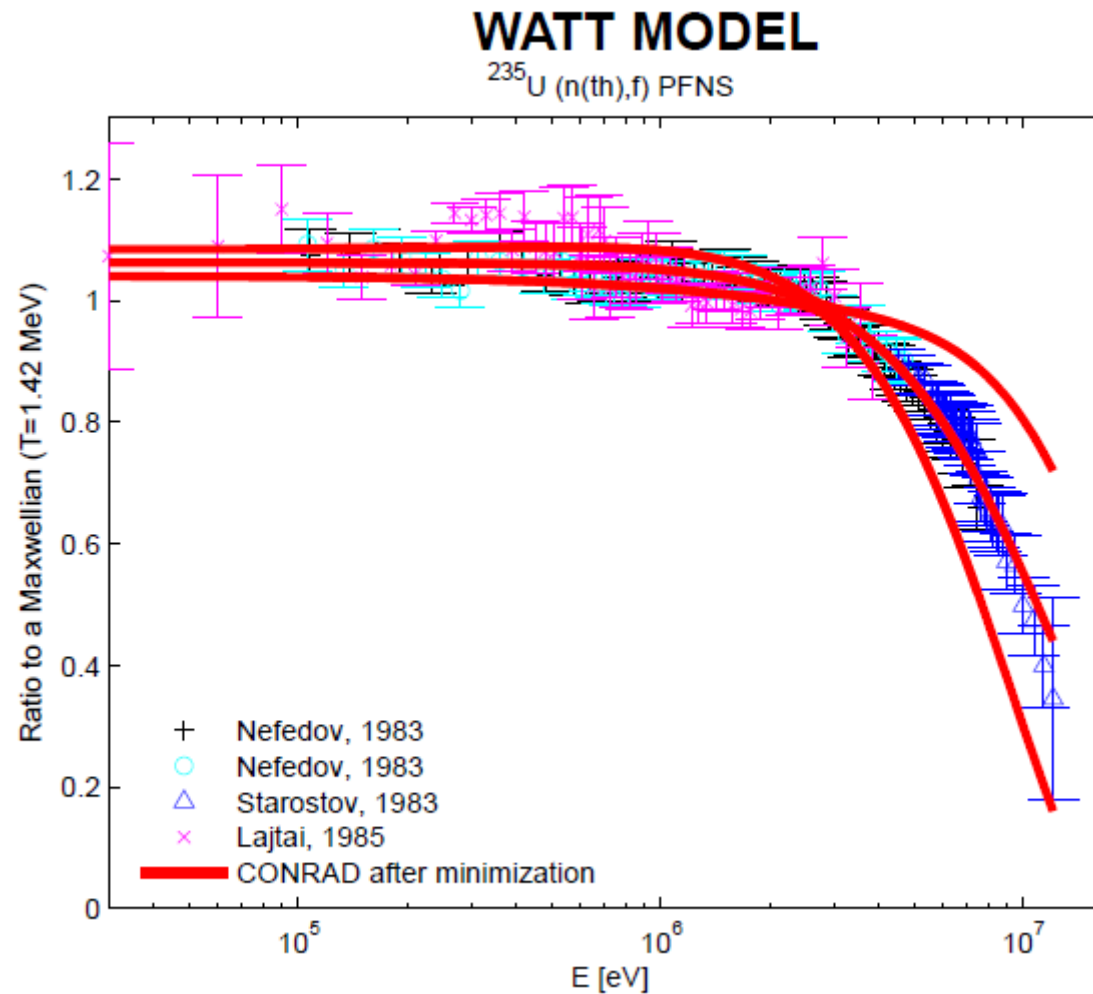




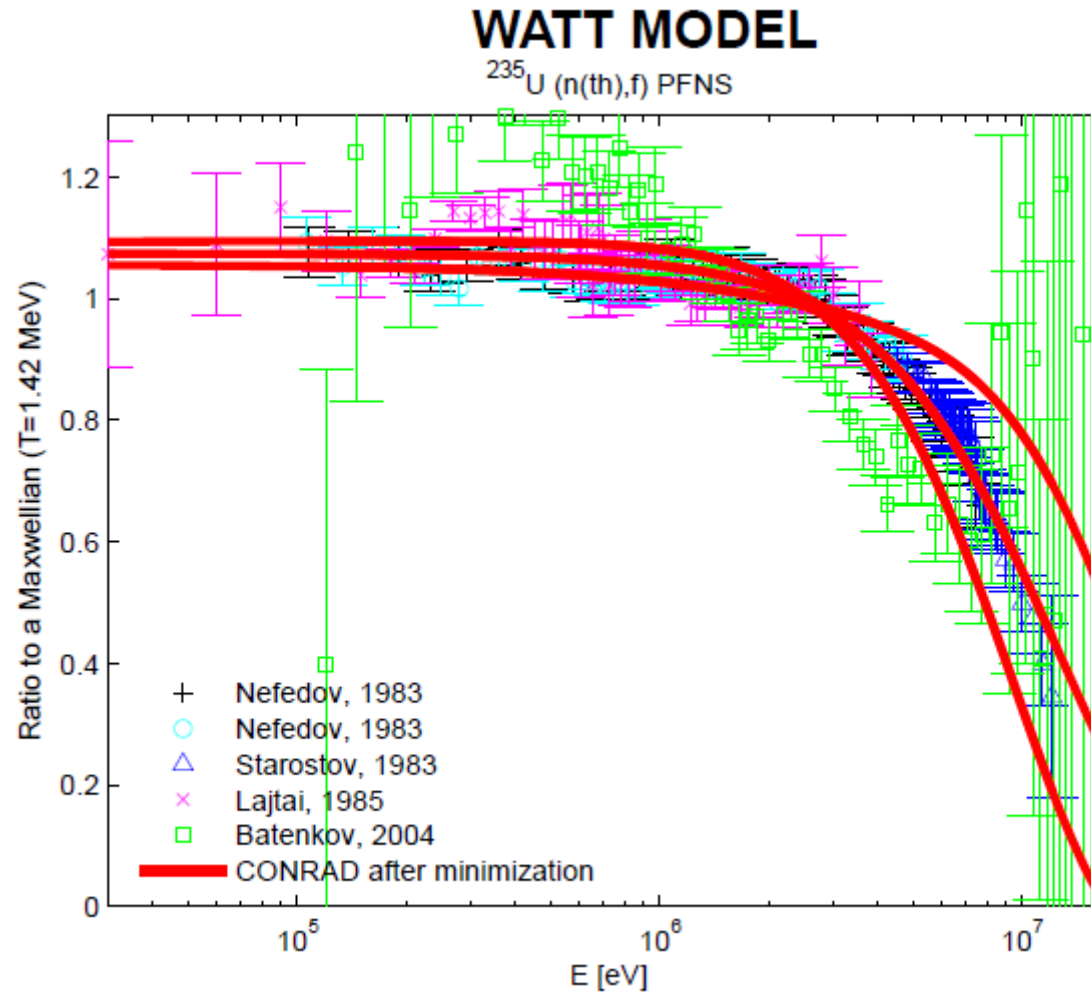






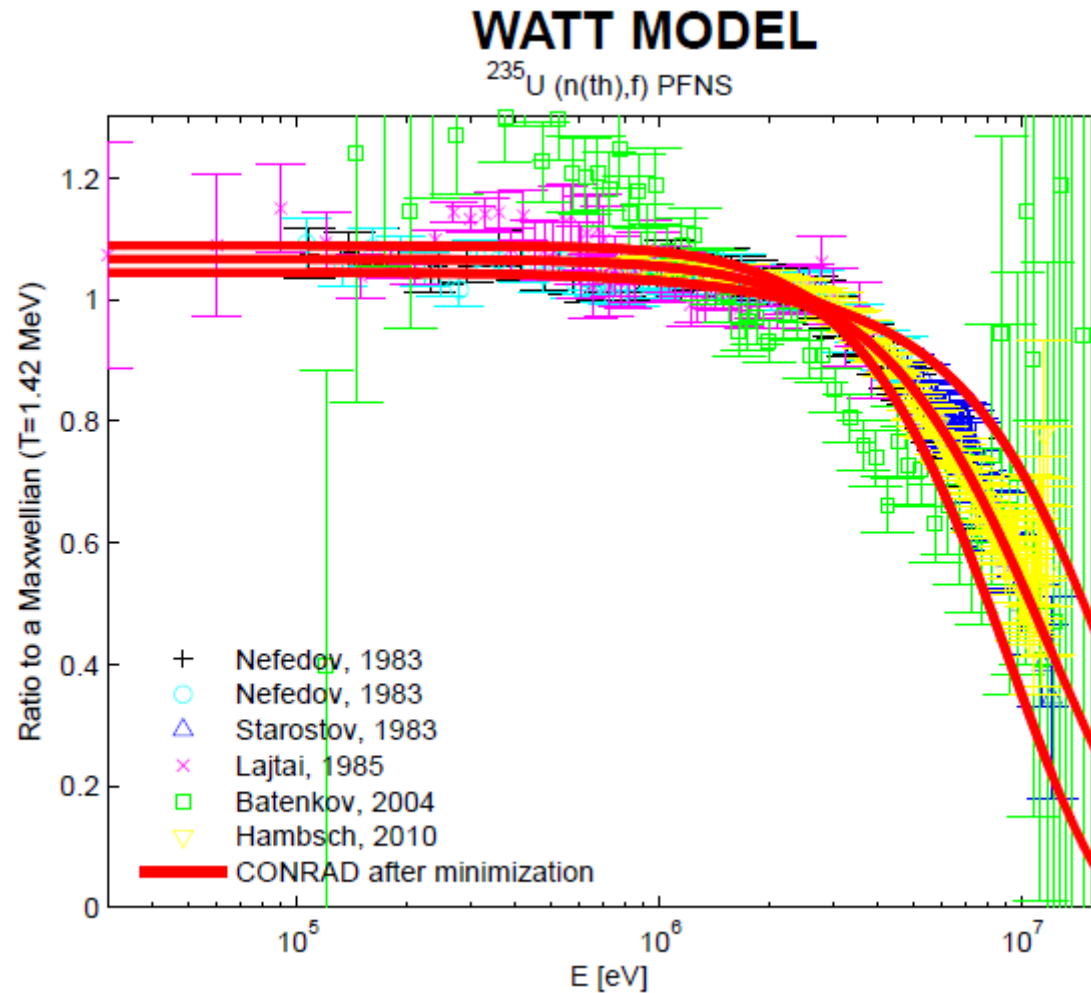


☐ Thermal fission of U235  
(Correlation matrix for Prompt Fission Neutron Spectrum)

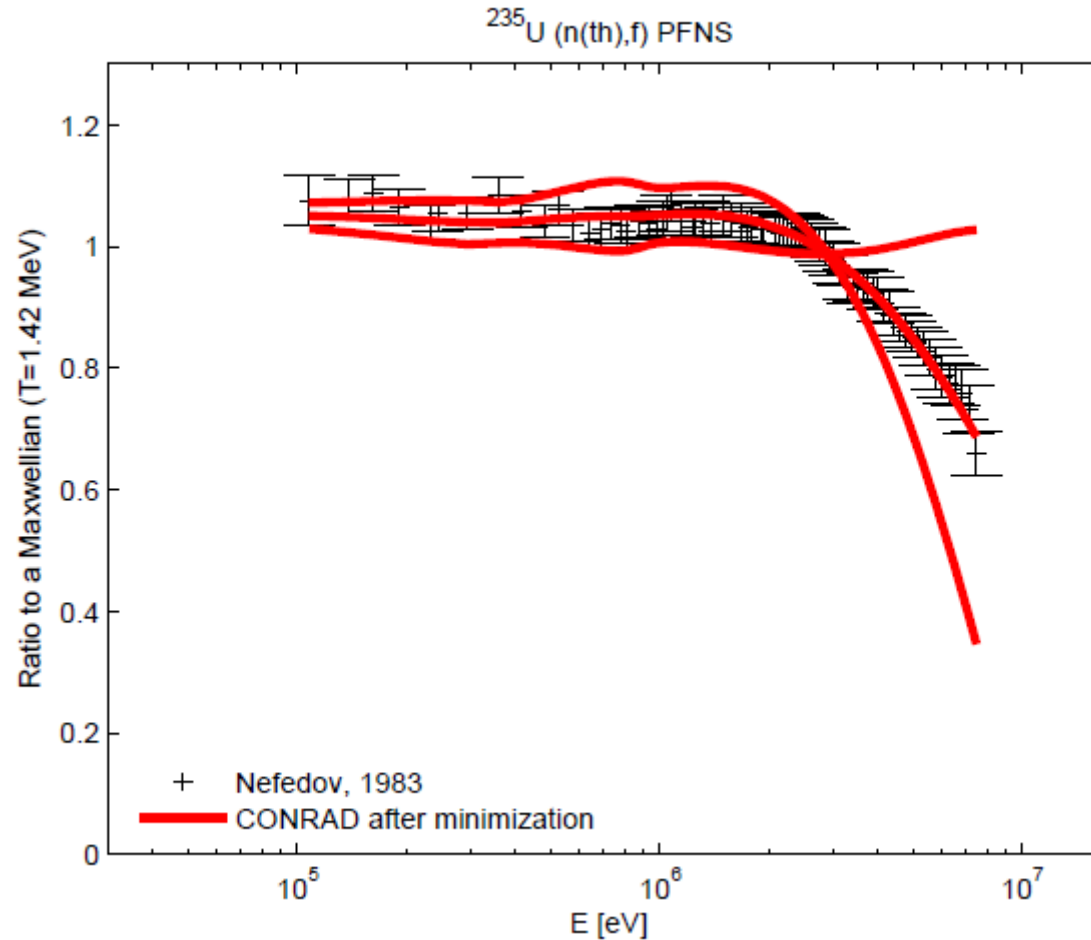


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☐ Thermal fission of U235  
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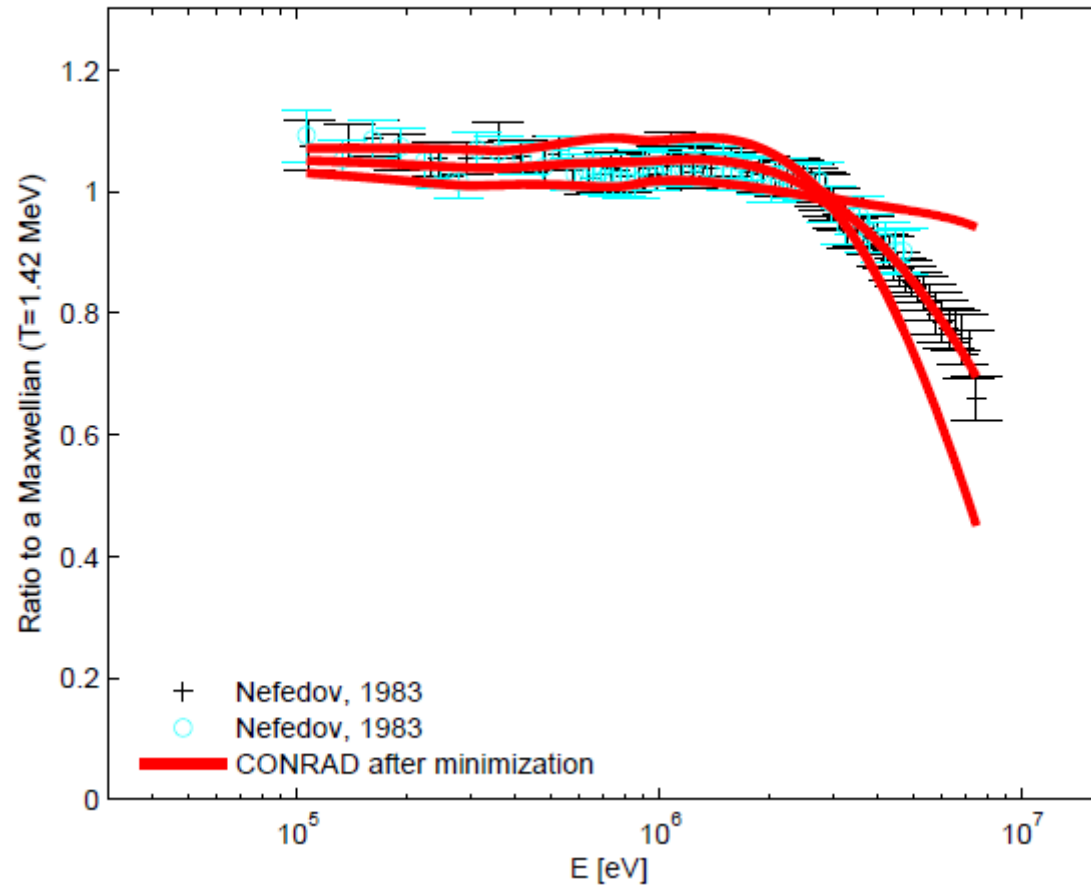


## MADLAND-NIX MODEL



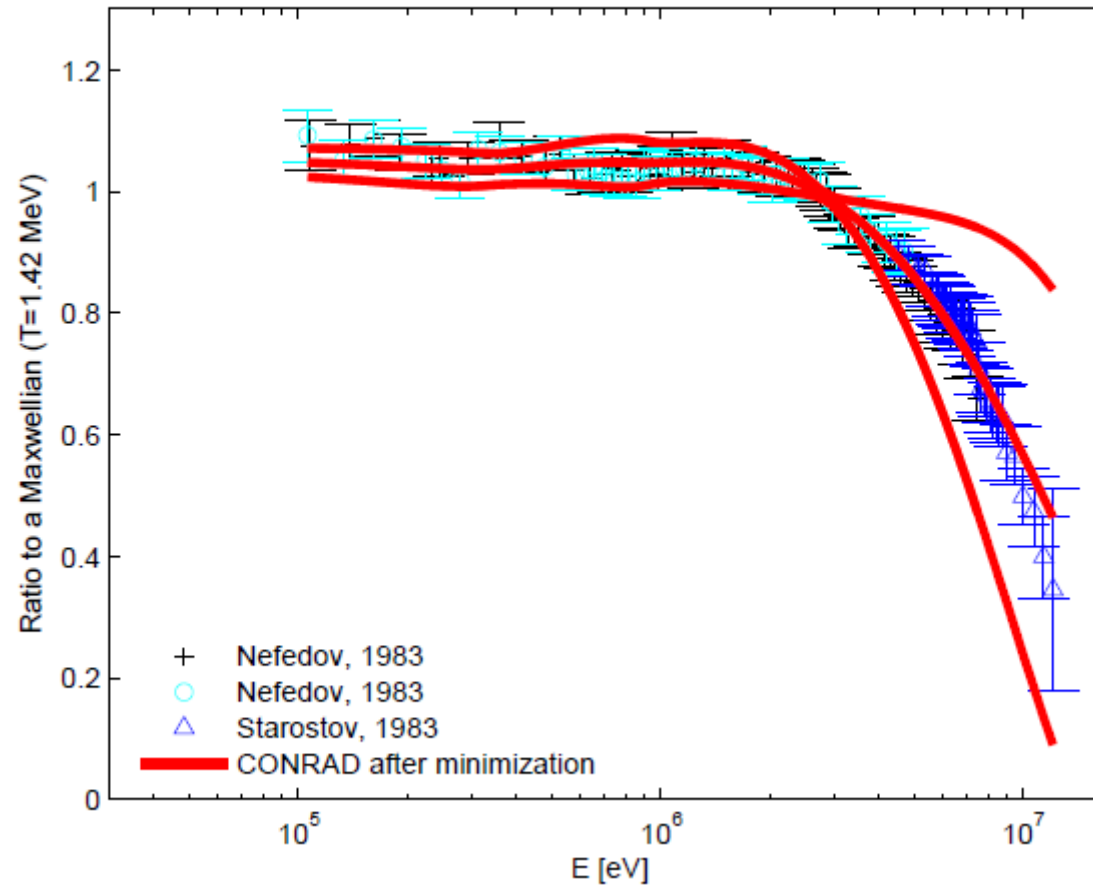
## MADLAND-NIX MODEL

$^{235}\text{U}$  (n(th),f) PFNS

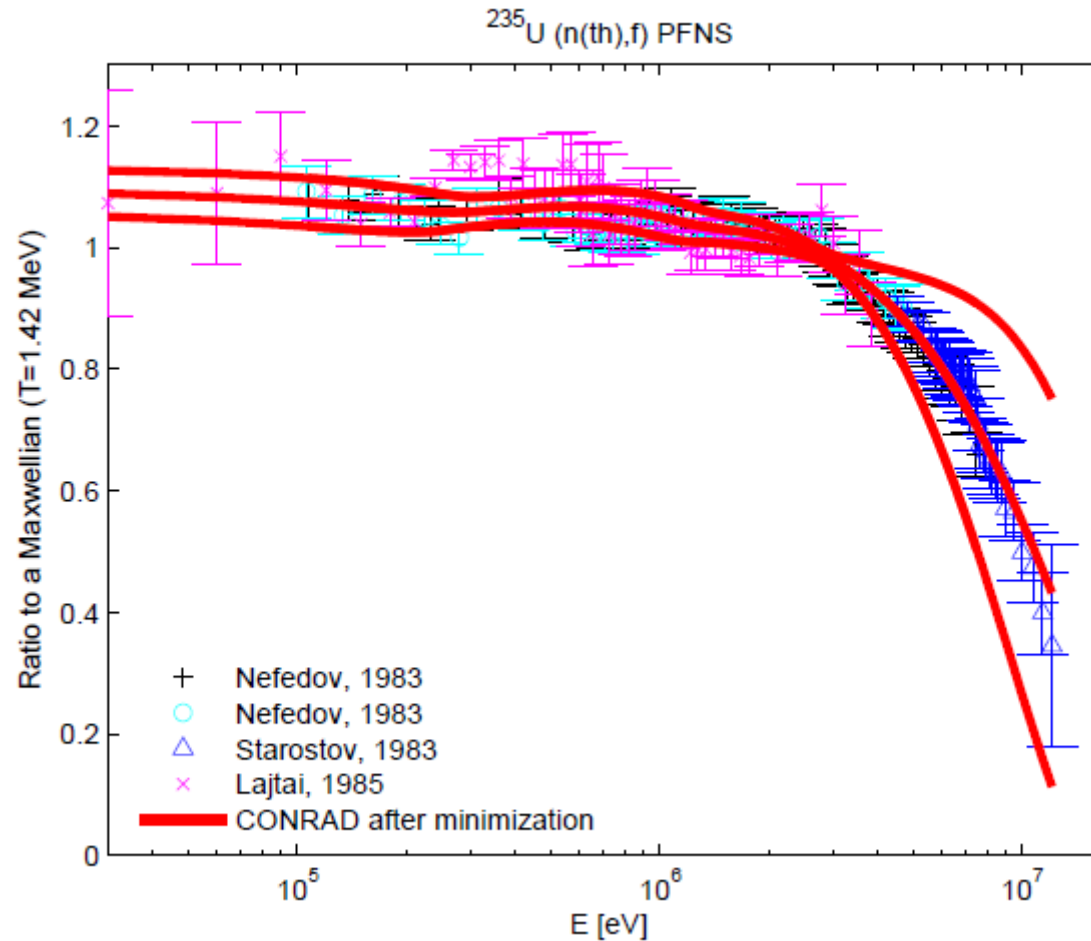


## MADLAND-NIX MODEL

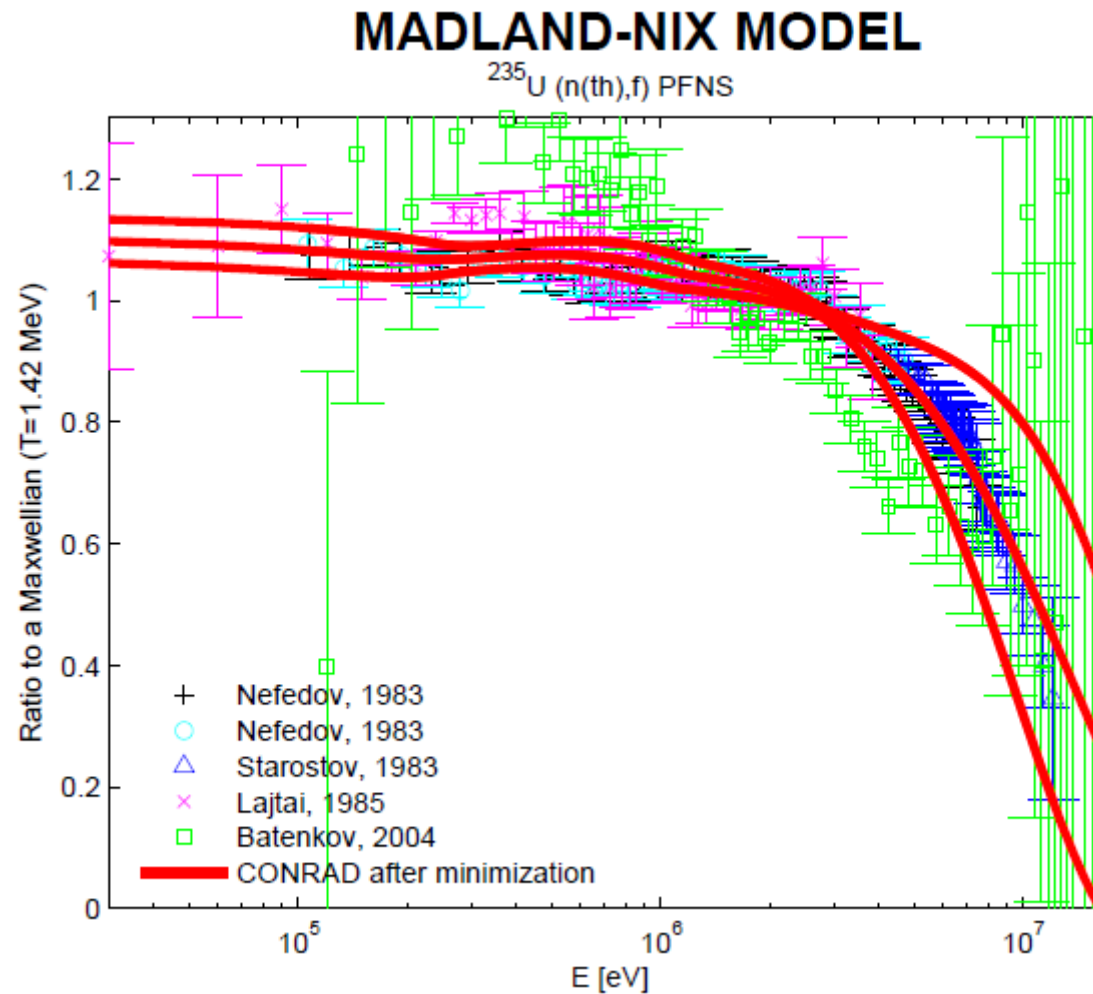
$^{235}\text{U}$  (n(th),f) PFNS



## MADLAND-NIX MODEL

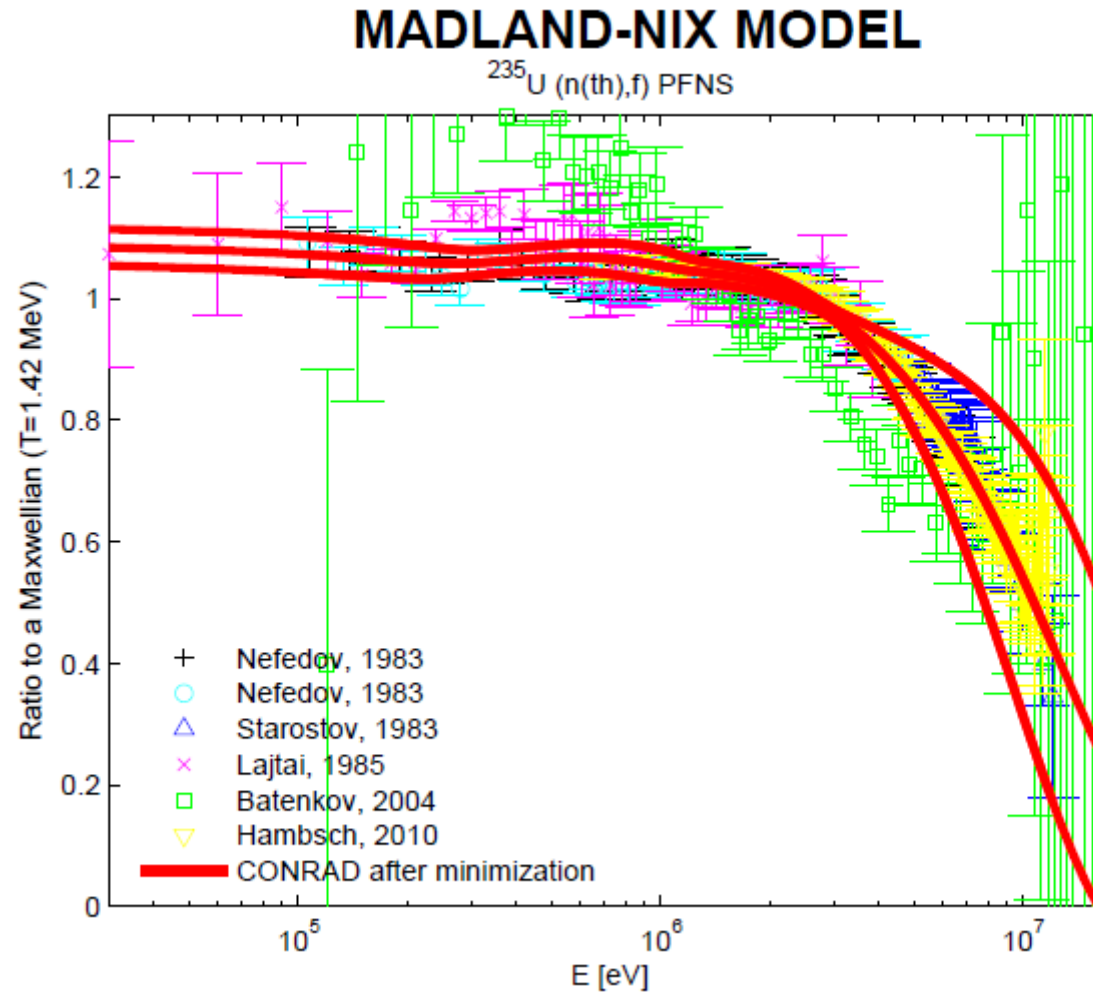


☐ Thermal fission of U235  
(Correlation matrix for Prompt Fission Neutron Spectrum)



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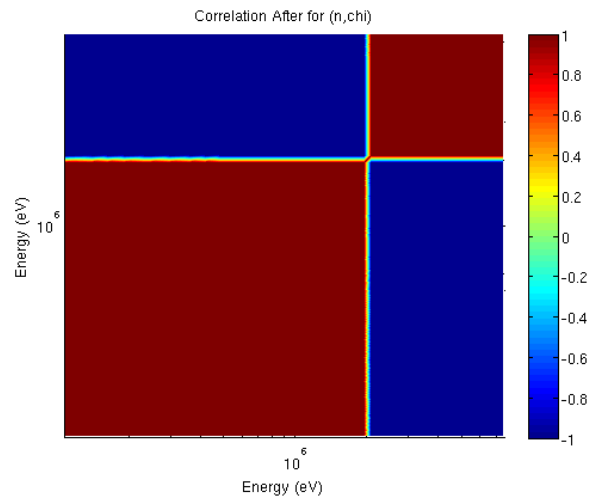


❑ Thermal fission of U235  
(Correlation matrix for Prompt Fission Neutron Spectrum)

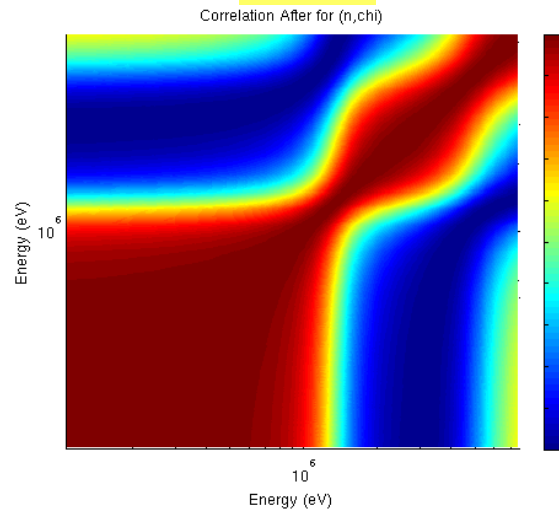


*Without marginalization of the normalization*

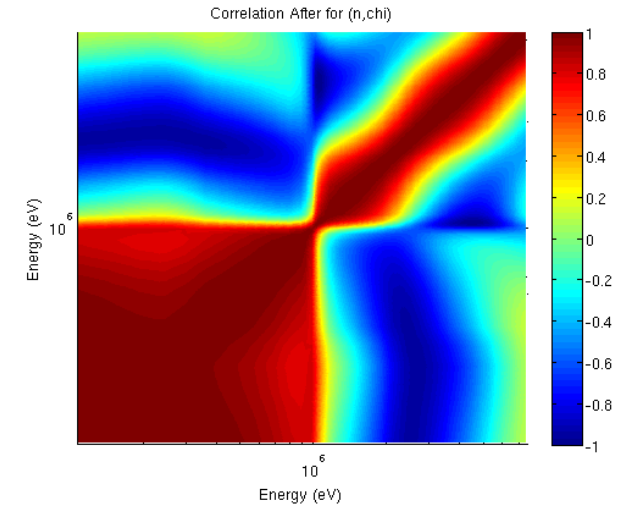
Maxwell



Watt



Madland-Nix



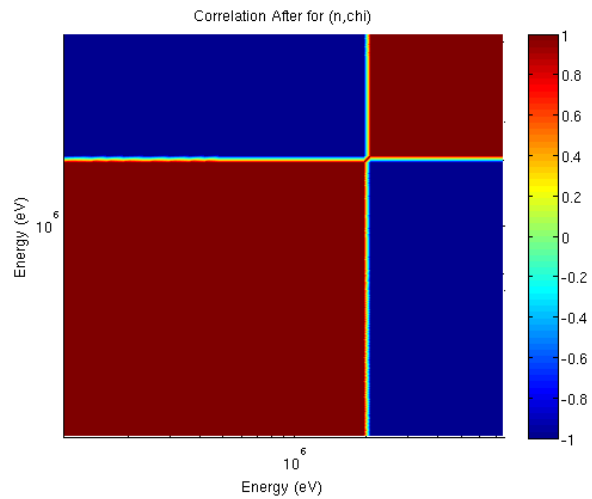
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❑ Thermal fission of U235  
(Correlation matrix for Prompt Fission Neutron Spectrum)

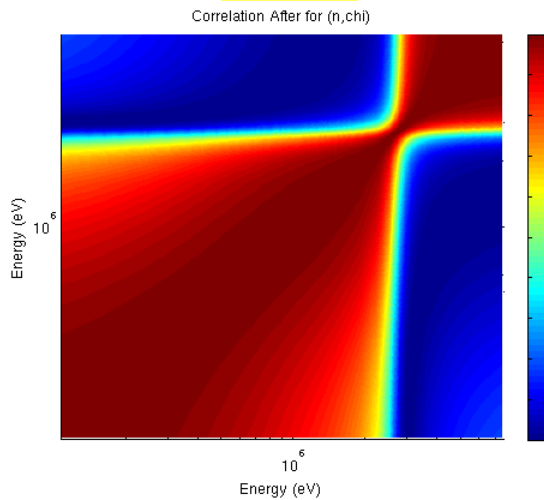


With marginalization of 5% normalization uncertainty

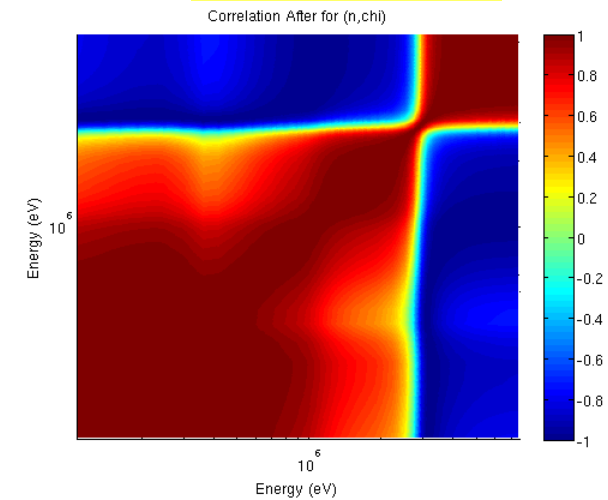
Maxwell



Watt



Madland-Nix



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❑ Thermal fission of U235  
(**Correlation matrix** for Prompt Fission Neutron Spectrum)

5% uncertainty on **normalization parameter** is a more or less realistic value !

→ Depends on the **data** (past and present),

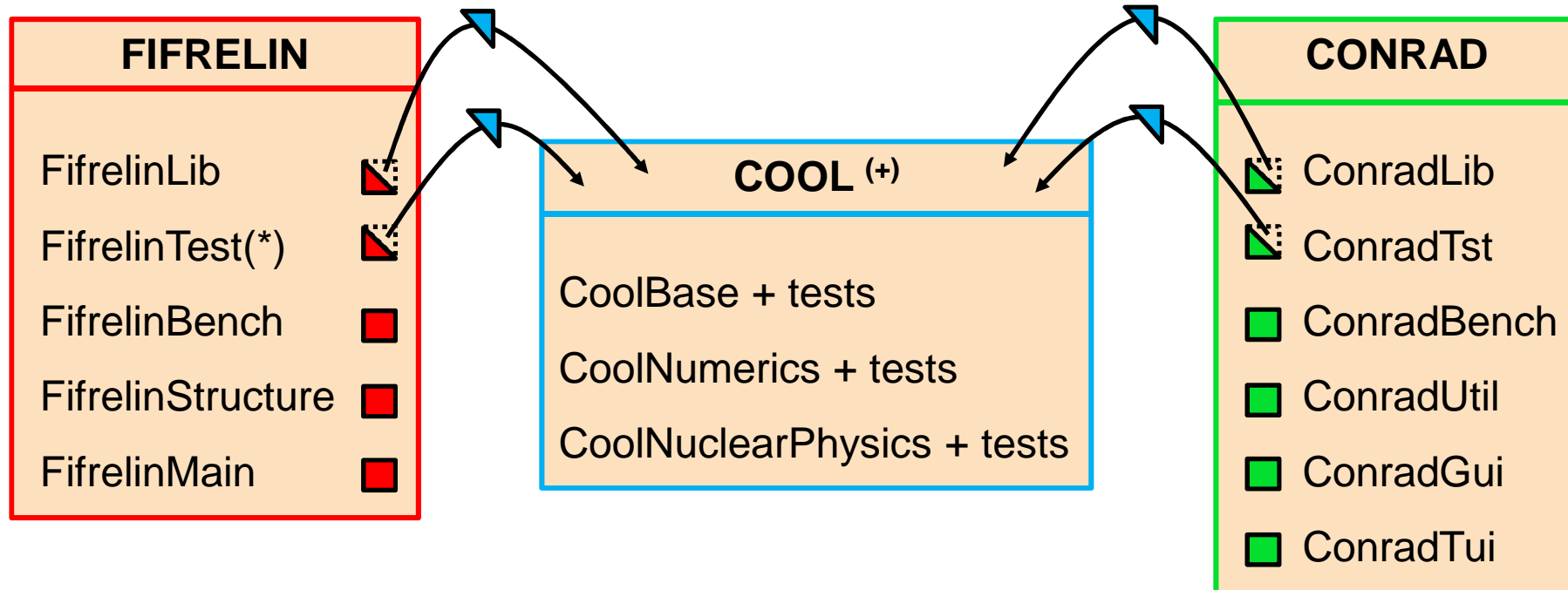
→ Uncertainty can be higher/lower for a **given energy range** : need for another experimental parameter : **neutron detector efficiency** (work in progress).

**Fifrelin model parameter adjustment** from a Conrad/Fifrelin coupled scheme

→ Fifrelin is used as a 'Nuclear Model' inside Conrad to adjust some of the 5 free parameters of the code and generate correlation matrices...(from D.

Regnier Phd work , in progress ...)

- ❖ **Covariance matrices** related to prompt fission neutron spectra can be calculated using so-called Maxwell, Watt or Madland-Nix spectra within the CONRAD code et COOL libraries.
  - ❖ **Fission observables** such as neutron *and* gamma spectra, multiplicities, fission yields can be calculated through a Hauser-Feshbach model within the FIFRELIN Monte Carlo code and COOL libraries.
- 
- ❖ **Improvement of the fission fragment deexcitation** model still in progress within FIFRELIN.
  - ❖ **CONRAD / FIFRELIN coupling under investigation** for covariance matrix generation



(\*) {  
 - *Unitary* tests  
 - *Physics* tests for a given 'parameter' related to a given nucleus (average radiation width, branching ratio, ...)

(+) **Cadarache Object Oriented Libraries**

*Thank you for your attention*

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