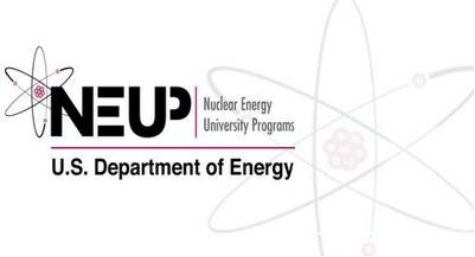


Differential Cross Section Measurements at the University of Kentucky

-- Adventures in Analysis

- J.R. Vanhoy, S.F. Hicks, B.R. Champine, B.P. Crider, E.A. Garza, S.L. Henderson, S.H. Liu, E.E. Peters, F.M. Prados-Estévez, M.T. McEllistrem, T.J. Ross, L.C. Sidwell, J.L. Steves, and S.W. Yates
 - *US Naval Academy, Annapolis, MD 21402*
 - *University of Dallas, Irving, TX 75062*
 - *University of Kentucky, Lexington, KY 40506*
 - *US Military Academy, West Point, NY*



- General Intro to the Laboratory
- Sample results for recent ^{23}Na , ^{54}Fe , $^{\text{nat}}\text{Fe}$ (n, n') & ($n, n'\gamma$)
- Adventures in Analysis
 - Ambiguities in Neutron Detection Efficiency attributed to $^3\text{H}(p, n) d\sigma/d\Omega$
 - The technique
 - Choices for $d\sigma/d\Omega$
 - Impact on Efficiency (E)
 - Challenges in Normalizing ($n, n'\gamma$)
 - What we did for $^{23}\text{Na}(n, n'\gamma)$
 - What will we do for $^{54,56}\text{Fe}$?
 - How well do we know the finite geometry corrections?
 - Proving our correction code is rigorous
- Conclusion



- **Accelerator**

- HVEC Model CN: 7 MV
- rf source
- p, d, ^3He , α , ... ions
- Authorized for ^3H gas targets
- 1 ns pulse widths

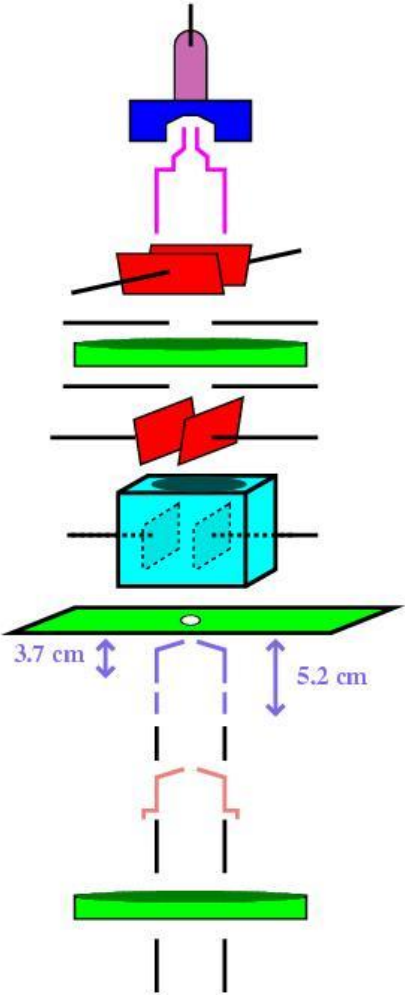
- **Basic Nuclear Science**

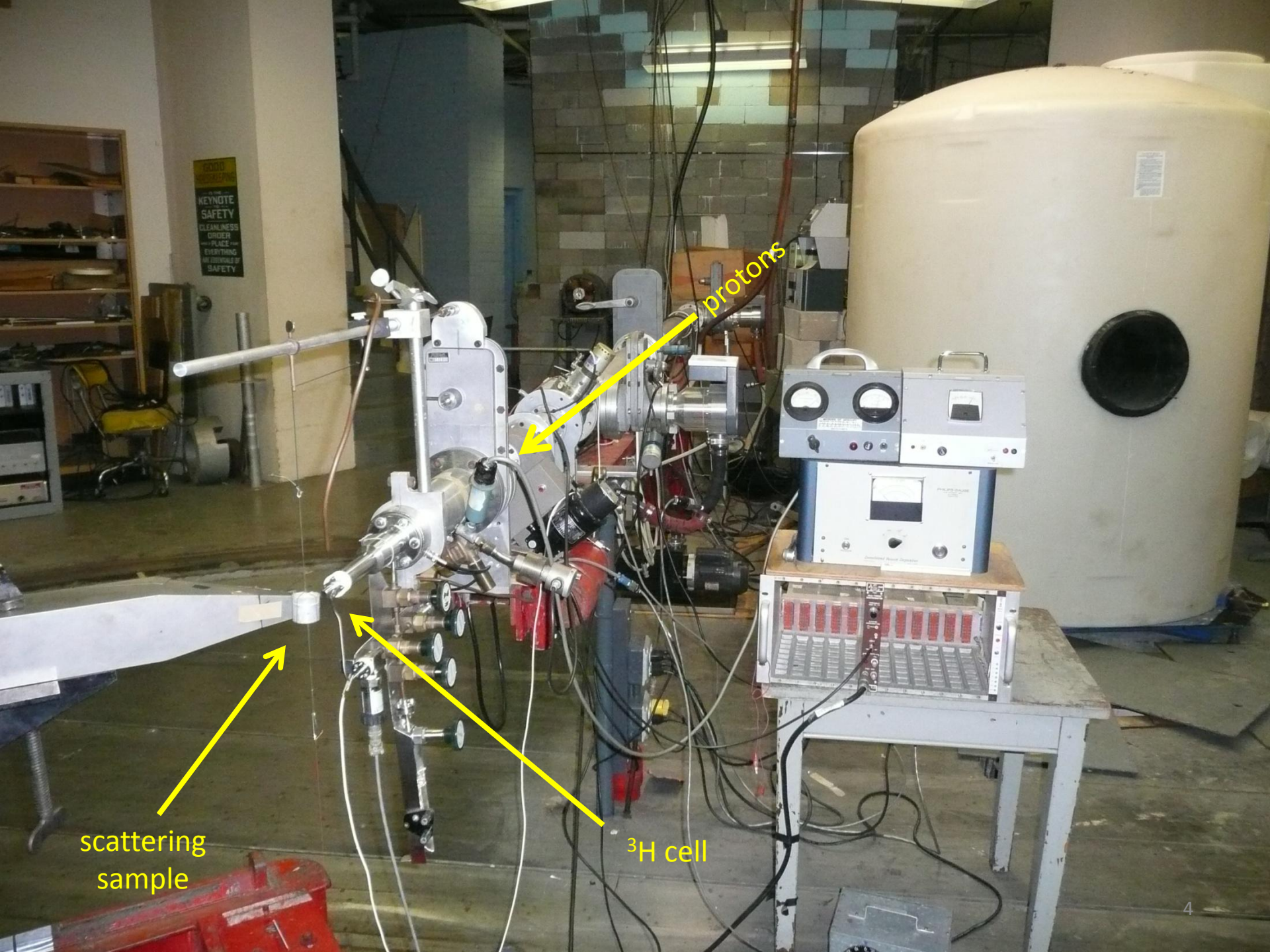
- Nuclear Structure via $(n, n'\gamma)$
 - Level Schemes & Transitions
 - Spectroscopic Information
 - DSAM Lifetimes

- $(^3\text{He}, n\gamma)$

- **Applied Nuclear Science**

- Differential (n, n') Cross Sections
 - ^{23}Na , ^{54}Fe , ^{56}Fe
- Detector Development
 - Univ Guelph
 - Univ Mass @ Lowell
 - RMD





protons

scattering
sample

^3H cell

WEYNOTE
SAFETY
CLEANLINESS
ORDER
PLACE
EVERYTHING
IN OVERSEAS OF
SAFETY

Tungsten wedge

$3\text{H}(p,n)$ $Q = -0.76$ MeV
 $2\text{H}(d,n)$ $Q = 3.3$ MeV
 $3\text{H}(d,n)$ $Q = 17.6$ MeV

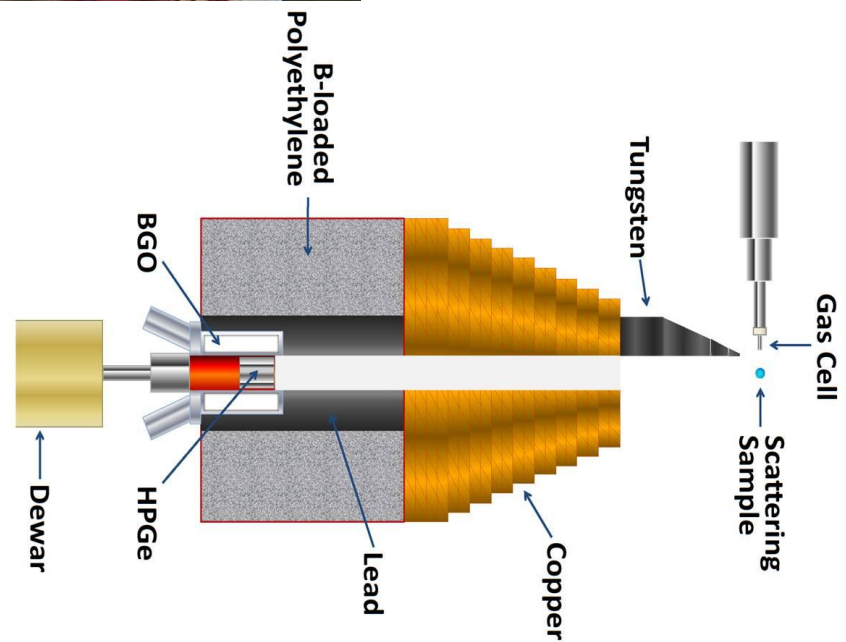
Neutron detector

Beam line

Gas cell

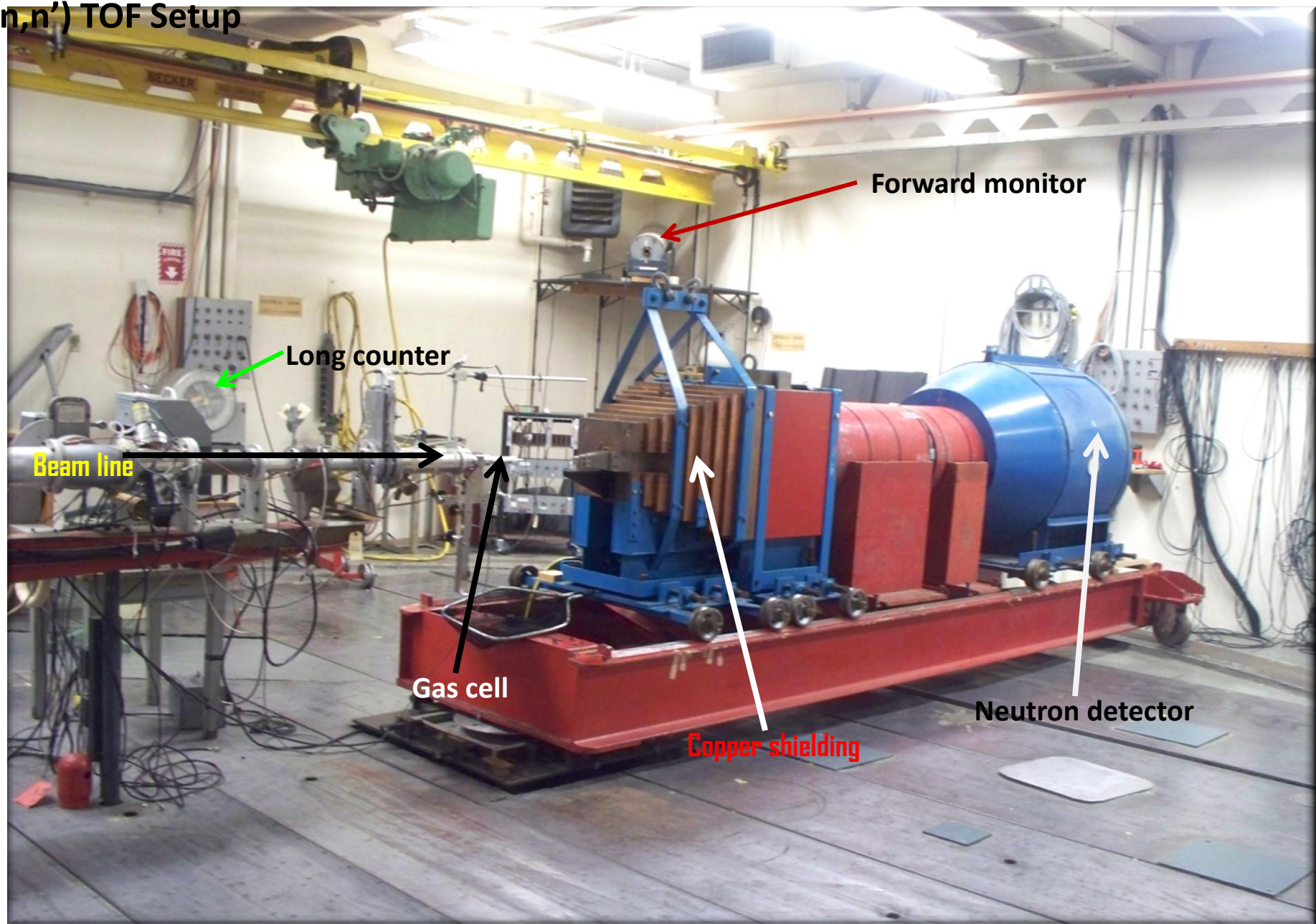
Na sample

Typical adjustment of wedge with cell and sample



**γ -Ray Detection
(singles setup)**

(n,n') TOF Setup



Forward monitor

Long counter

Beam line

Gas cell

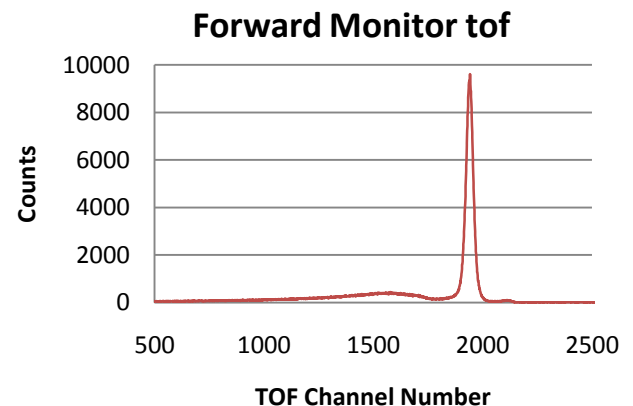
Copper shielding

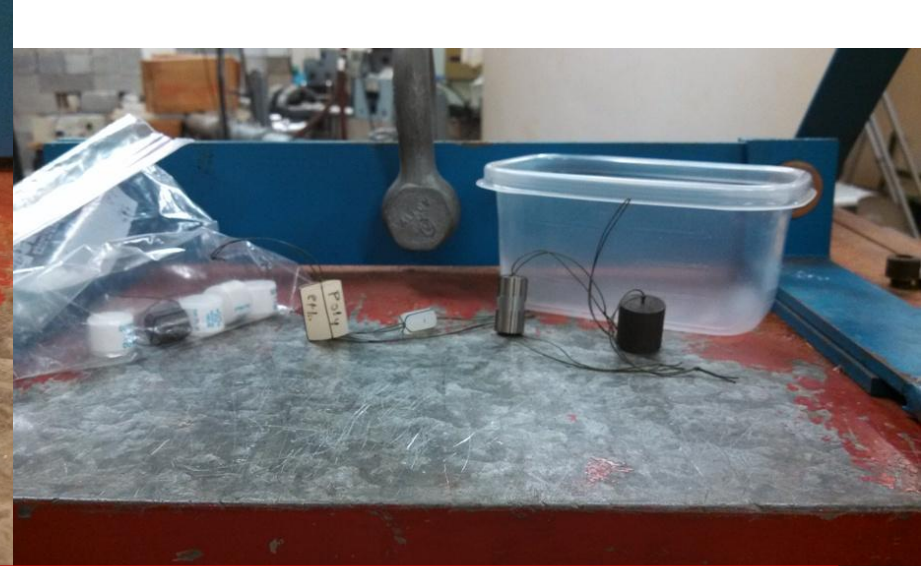
Neutron detector

Monitoring Neutron Production

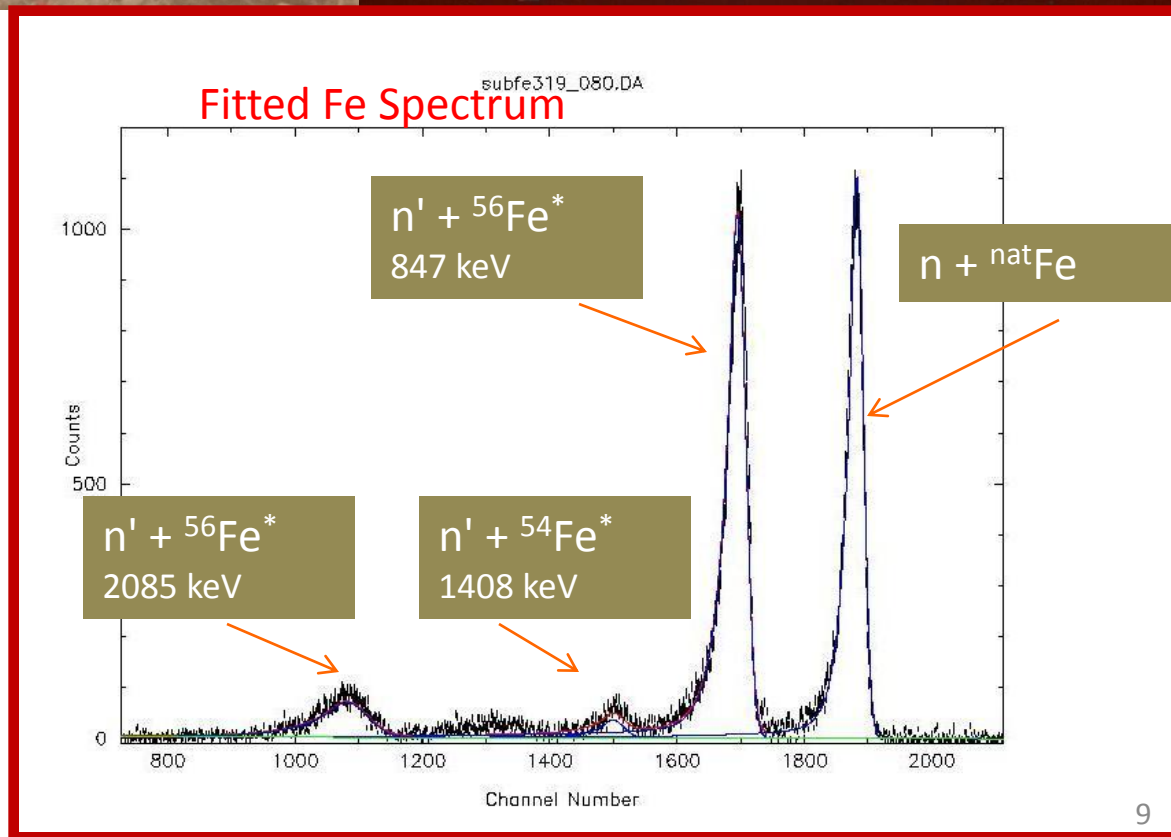
- **Forward Monitor**
 - C_6D_6 liquid scintillator
 - Best choice for n angular distributions
 - Views source neutrons from gas cell
 - PSD cleanly identifies neutrons
- **Long Counter(Hanson & McKibben 1947)**
 - Moderated BF3 tubes
 - Generally used for excitation functions
 - Insensitive to γ -rays
 - Insensitive to room thermals
 - Placement at large angles reduces concern over resonances in LC efficiency.
- **$^{74}Ge(n,g)$ 140-keV line in HPGe**
 - Measures prompt-thermal fraction during beam pulse.

For absolute $d\sigma/d\Omega$ values, use
 $^1H(n,n)$ for neutrons
& _____ for γ -rays





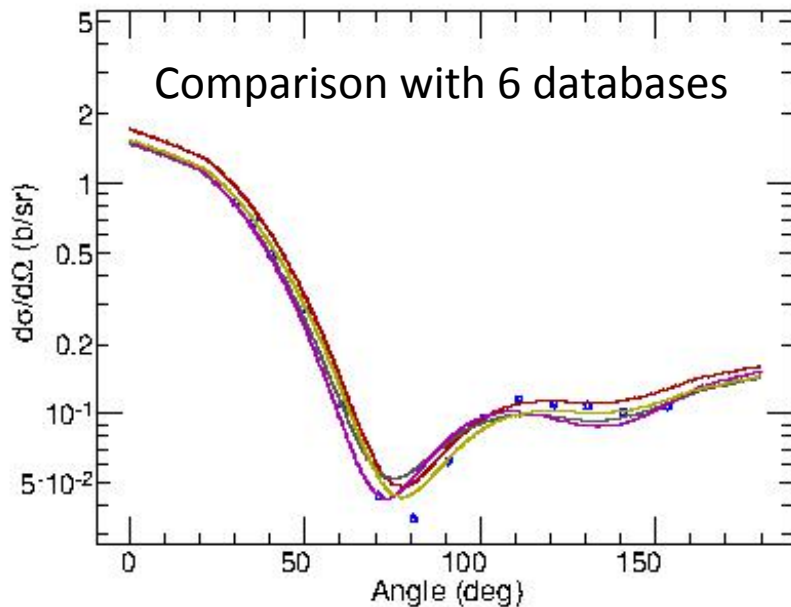
early natFe spectrum



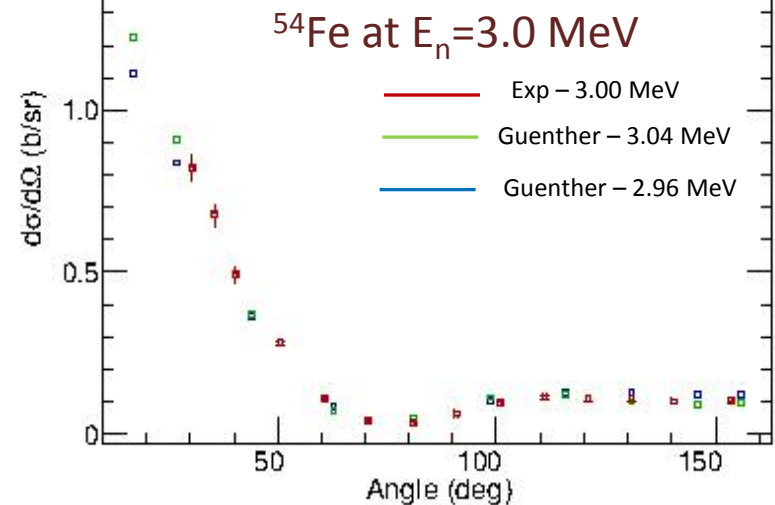
26-Fe-54(N,EL),DA Ei3.00E+6

$^{54}\text{Fe}(n,n)$

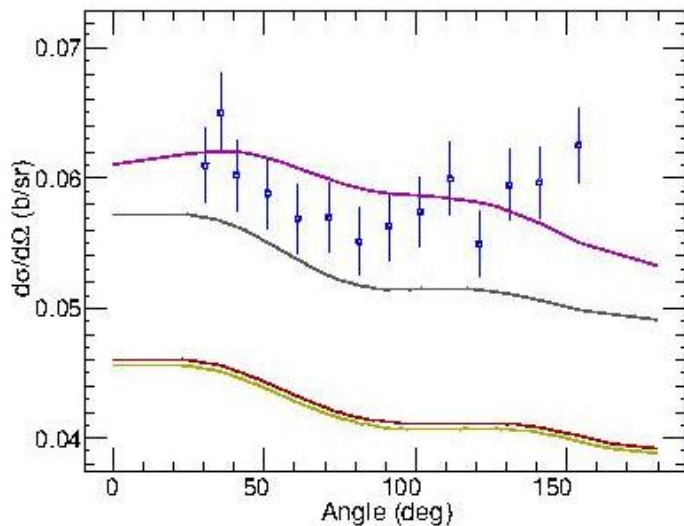
PRELIM ANALYSIS BY SALLY HICKS



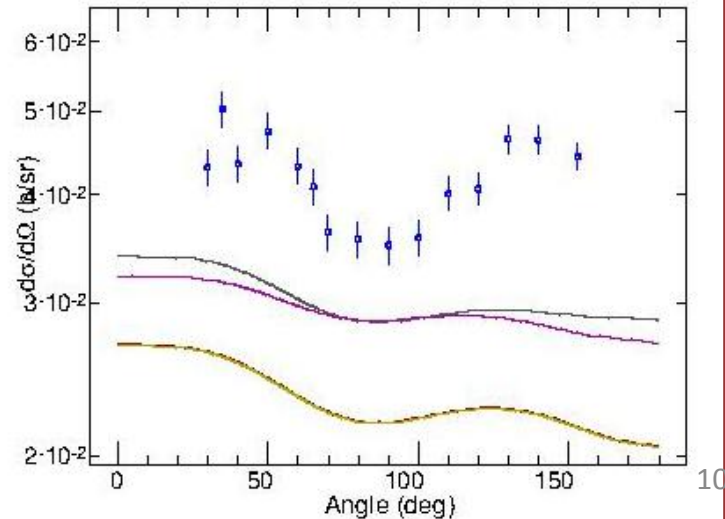
Guenther Ann Nucl Energy 13 601 (1986)



26-Fe-54(MT=51),DA Ei3.00E+6 Ei1.41E+6

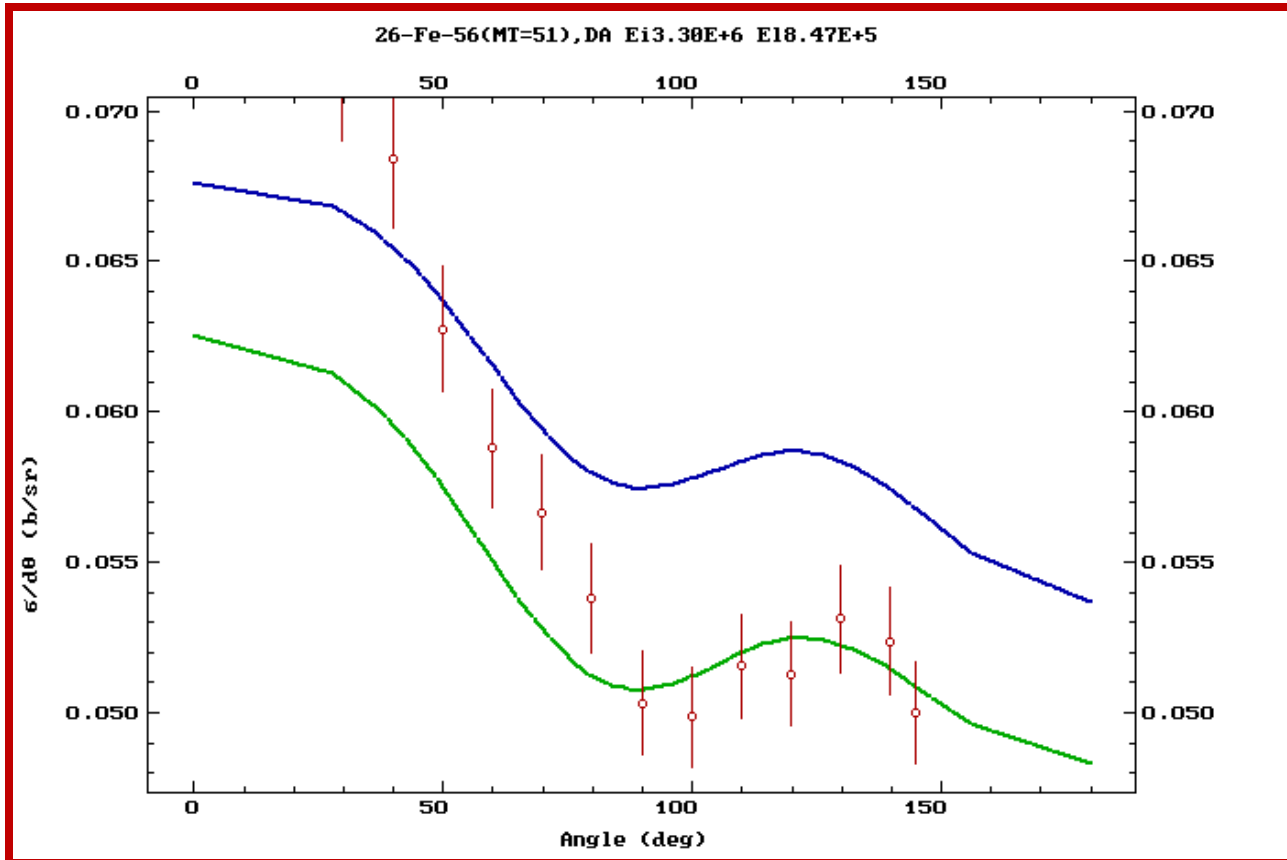


26-Fe-54(MT=51),DA Ei4.00E+6 Ei1.41E+6



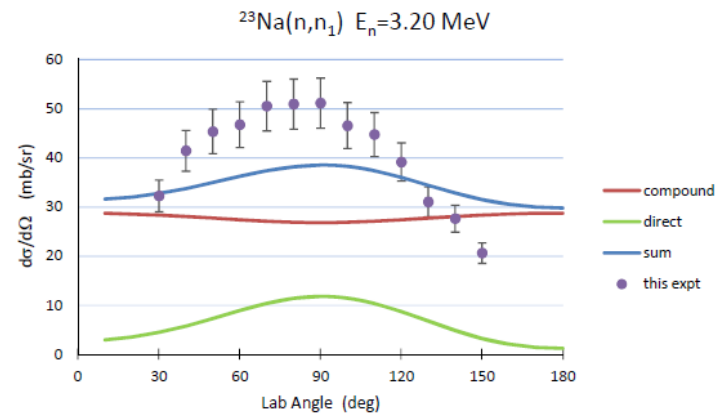
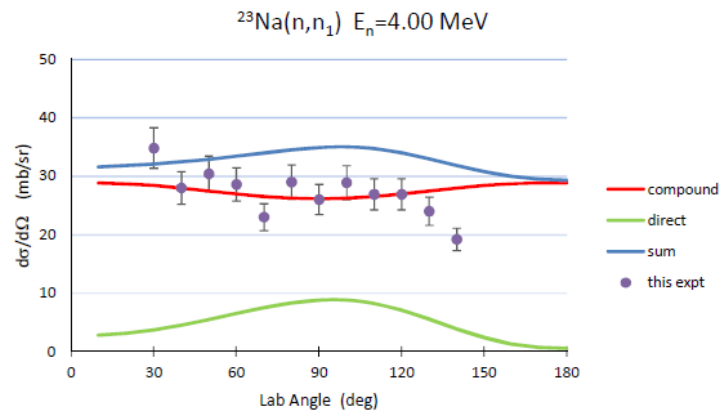
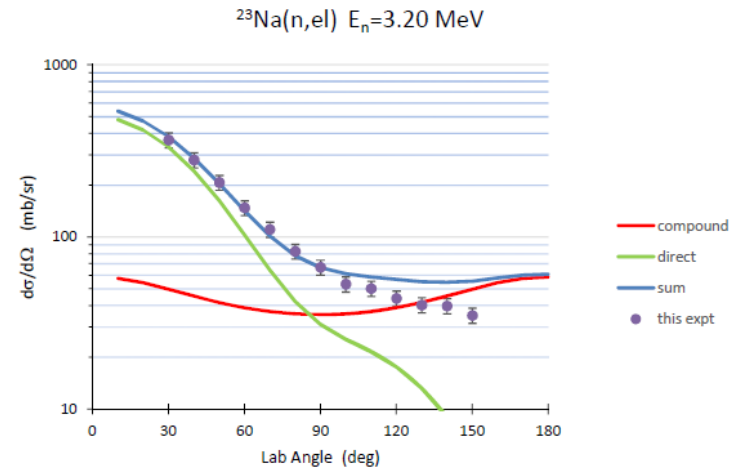
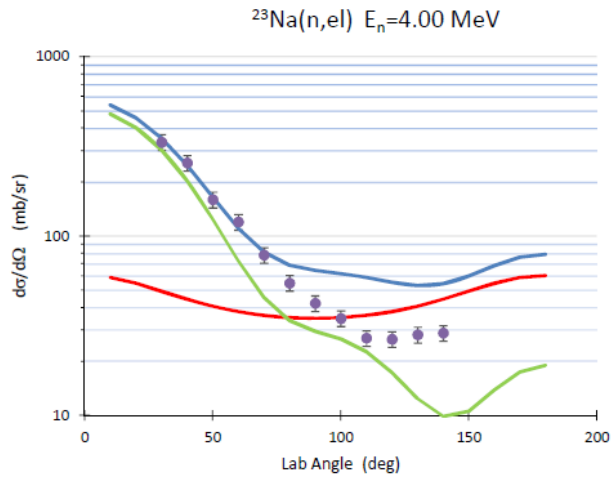
$^{56}\text{Fe}(n,n_1)$ using $^{\text{nat}}\text{Fe}$

PRELIM ANALYSIS BY SALLY HICKS



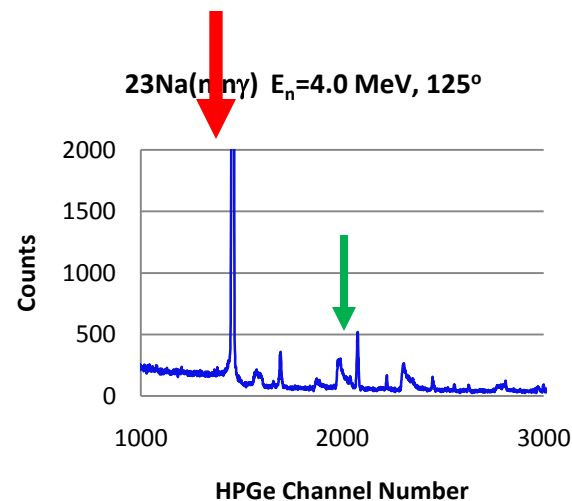
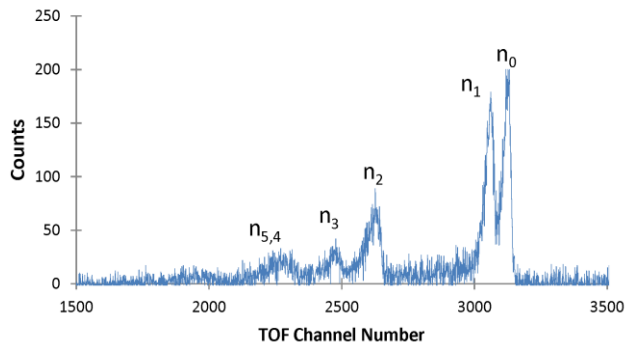
$^{23}\text{Na}(n,n)$

ECIS06 Calculations

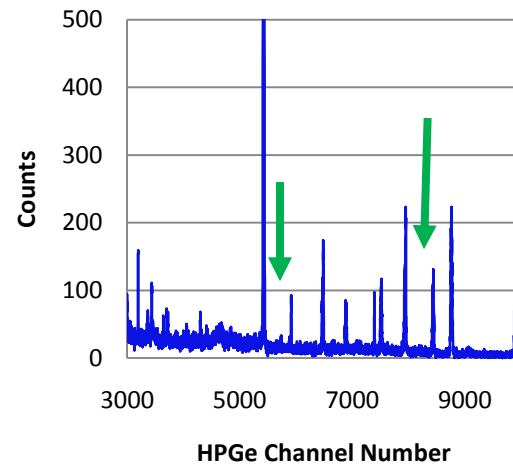
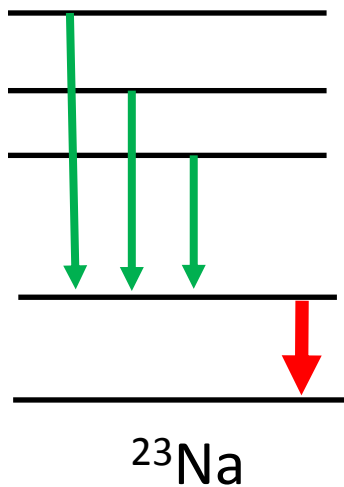


Inelastic Cross Sections --Two Techniques

$$\sigma_{n,n'} \leftrightarrow \sigma_{n,n'\gamma}$$

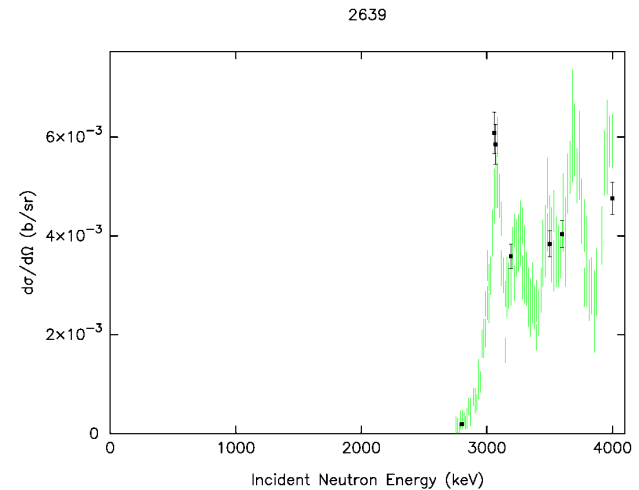
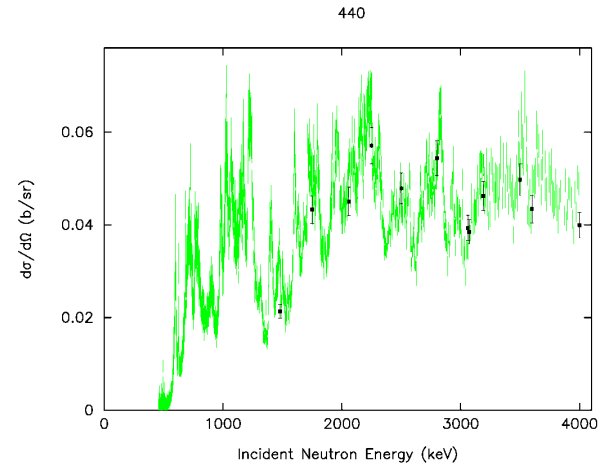
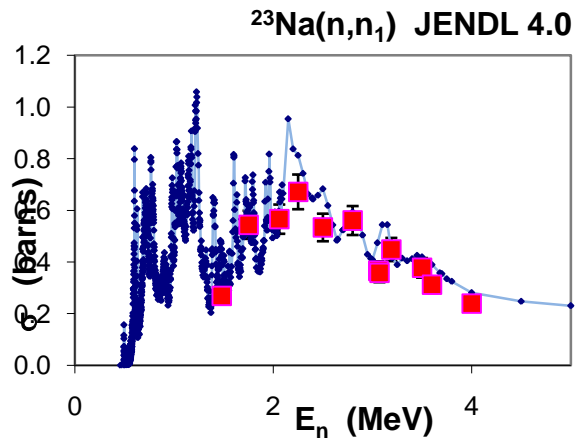
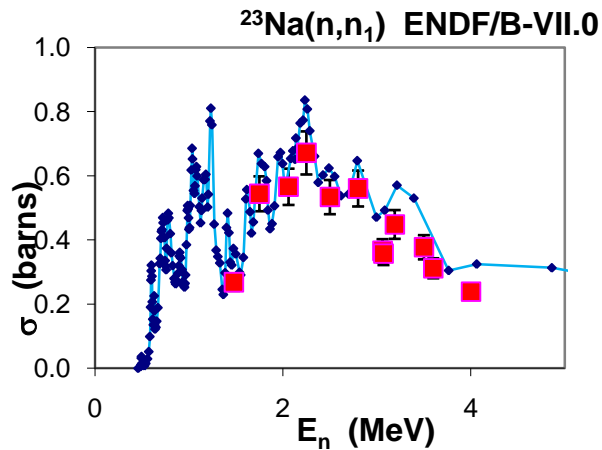


(n,n')



$$\sigma_{n,n'_k} = \sum \sigma_{de-excitation} - \sum \sigma_{feeders}$$

$^{23}\text{Na}(n,n'\gamma)$



Comparison of inelastic (n,n_1) cross sections as determined from $(n,n'\gamma)$ measurements with values in the evaluated nuclear libraries. ENDF over-predicts the data by $\sim 15\%$, while the data track JENDL quite nicely. The JEFF library (not shown) undershoots the data by $\sim 15\%$.

Comparison of measured γ -ray excitation functions with those of the GELINA/IRMM group [Rouki *et al*, NIM A 673, 83 (2012)]. UnivKY data points are in black. The agreement is striking considering the experiments use different normalization techniques and the neutron energy resolutions are significantly different.

1

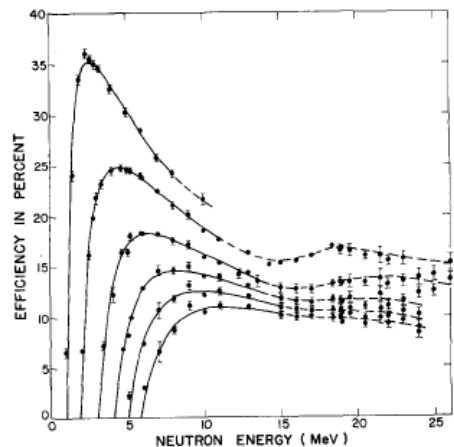


Fig. 4. Measured efficiency points for biases at 0.4, 1.0, 2.0, 3.0, 4.0 and 5.0 times Cs and calculated fits (solid lines). The dashed lines are handfitted.

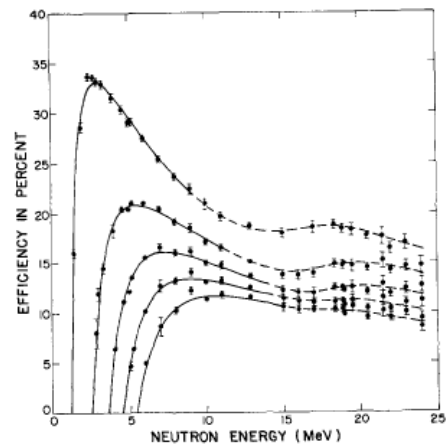


Fig. 5. Same as fig. 4, but for biases at 0.5, 1.5, 2.5, 3.5, and 4.5 times Cs.

ADVENTURES IN ANALYSIS

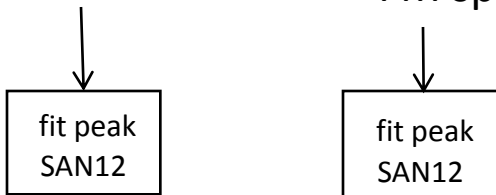
-- NEUTRON DETECTION EFFICIENCY

1



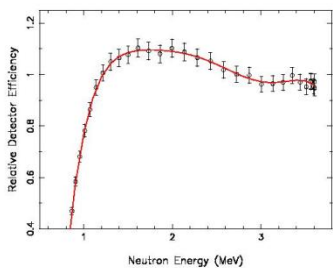
T-cell spectrum

FM spectrum



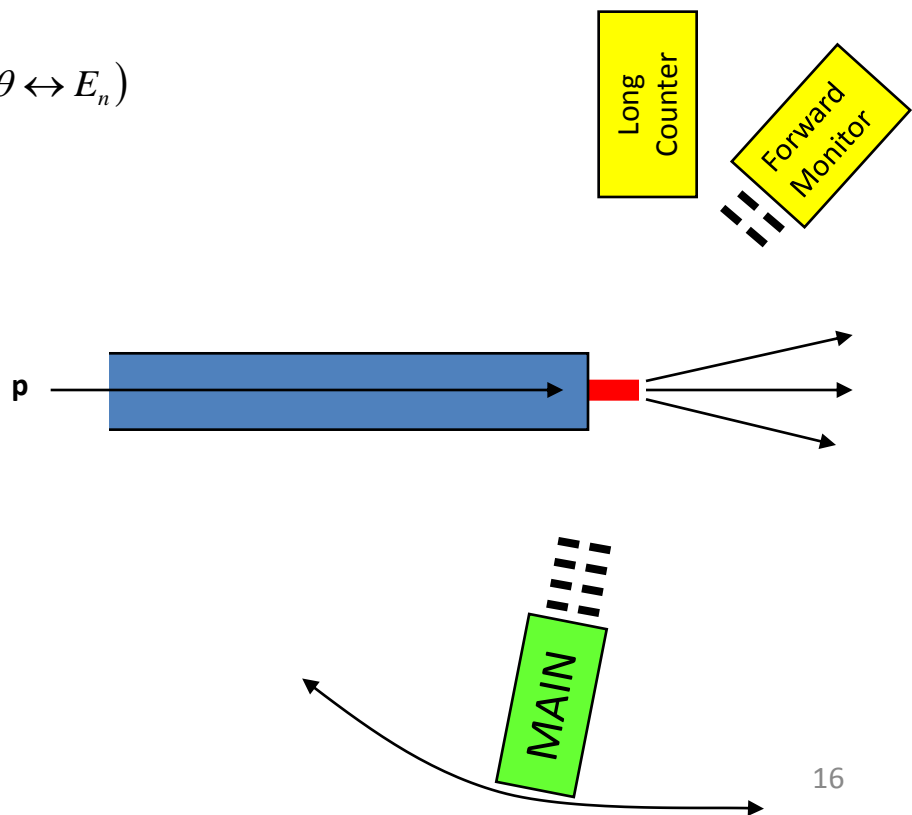
$$eff(E_n) = \frac{Yield}{FM \cdot \frac{d\sigma}{d\Omega_{Tpn}}}$$

$$\frac{d\sigma}{d\Omega_{3H(p,n)}} (\theta \leftrightarrow E_n)$$



$eff(E_n)$

Main Detector relative Efficiency

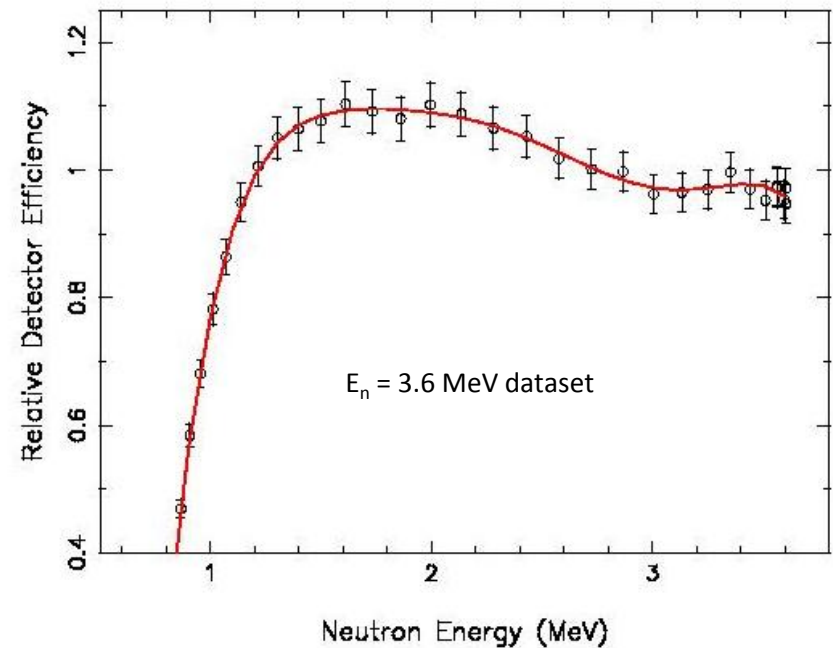


1

$$eff(E_n) = \frac{Yield}{FM \bullet \frac{d\sigma}{d\Omega_{Tpn}}}$$

- Neutron detection efficiency
 - Main detector
 - Amplifier gain
 - Thresholds
 - PSD cuts
 - Forward Monitor detector
 - Amplifier gain
 - Thresholds
 - PSD cuts
- Variances arise
 - Yield in ^3H cell spectrum ($\ll 1\%$)
 - Yield in FM spectrum ($\ll 1\%$)
 - Fit quality
 - Knowledge of $T(p,n)$ angular variation (3% ??)

Main Detector relative Efficiency



Sources for $T(p,n) d\sigma/d\Omega$

H.Liskien & A.Paulsen

M. Drogg

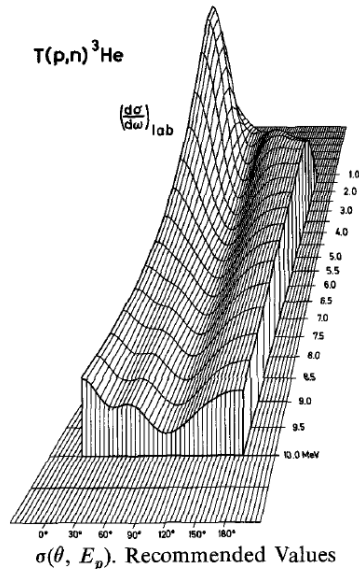
G. Hale

NUCLEAR DATA TABLES II, 569-619 (1973)

NEUTRON PRODUCTION CROSS SECTIONS AND ENERGIES FOR THE REACTIONS $T(p,n)^3\text{He}$, $D(d,n)^3\text{He}$, AND $T(d,n)^3\text{He}$

HORST LISKIEN and ARNO PAULSEN
Joint Nuclear Research Center
Central Bureau for Nuclear Measurements, Geel, Belgium

Center-of-mass best values for the normalized Legendre coefficients and the 0° differential cross section as functions of input energy have been derived from various experimental results for the reactions $T(p,n)^3\text{He}$, $D(d,n)^3\text{He}$, and $T(d,n)^3\text{He}$. This information has been used to calculate laboratory differential cross sections as functions of laboratory input energy and neutron emission angle which are given in tabular form with the corresponding neutron energy.



INTERNATIONAL ATOMIC ENERGY AGENCY
NUCLEAR DATA SERVICES
DOCUMENTATION SERIES OF THE IAEA NUCLEAR DATA SECTION

IAEA-NDS-87
Rev. 8, January 2003

DROSG-2000: Neutron Source Reactions

Data files with computer codes
for 59 monoenergetic neutron source reactions

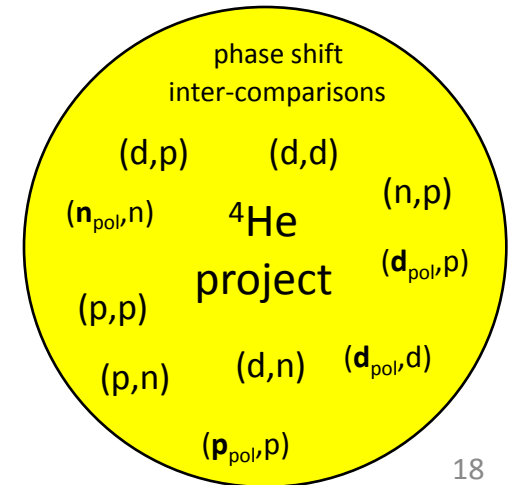
Version 2.2

prepared by

M. Drogg
Institute of Experimental Physics
University of Vienna

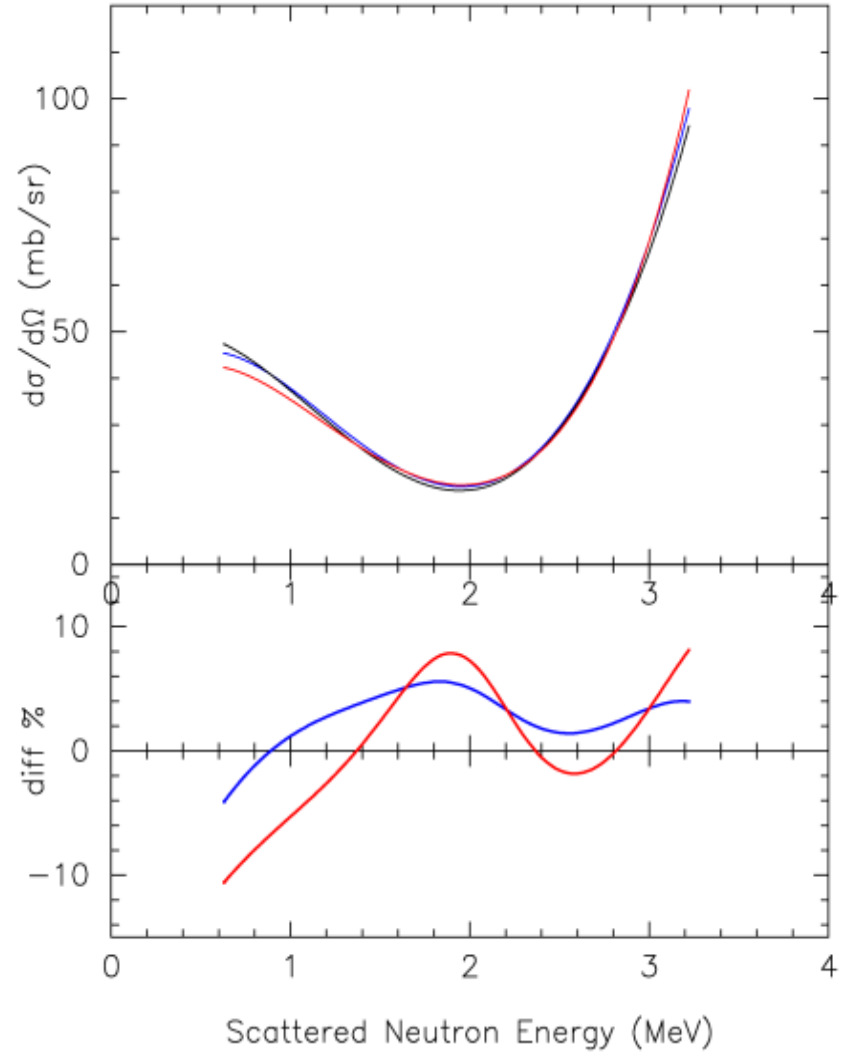
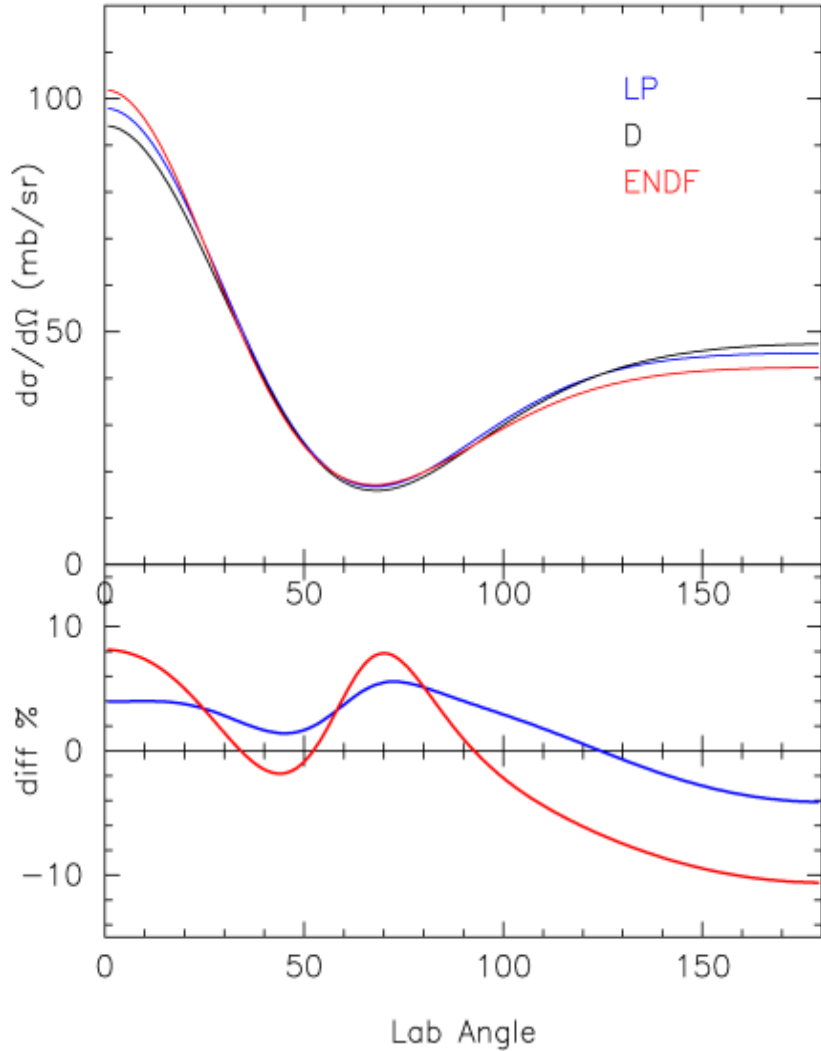
Summary documentation

Abstract: This package contains data and three computer codes to calculate:
- neutron energies, differential cross-sections and differential yields;
- thick-target yields and white neutron spectra from monoenergetic neutron producing reactions;
- differential cross sections and energies of (n,p), (n,d), (n,t) and (n,⁴He) reactions which are time-reversed neutron production reactions (using detailed balance calculations)
The package is available online or on PC diskette from the IAEA Nuclear Data Section.



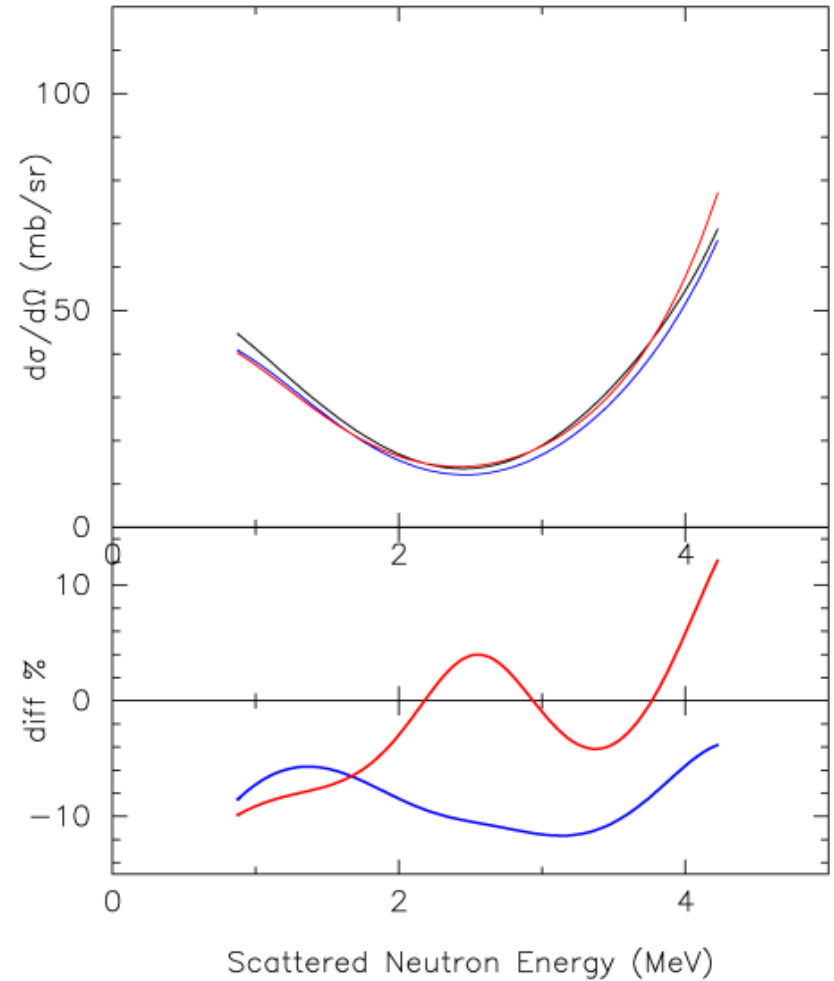
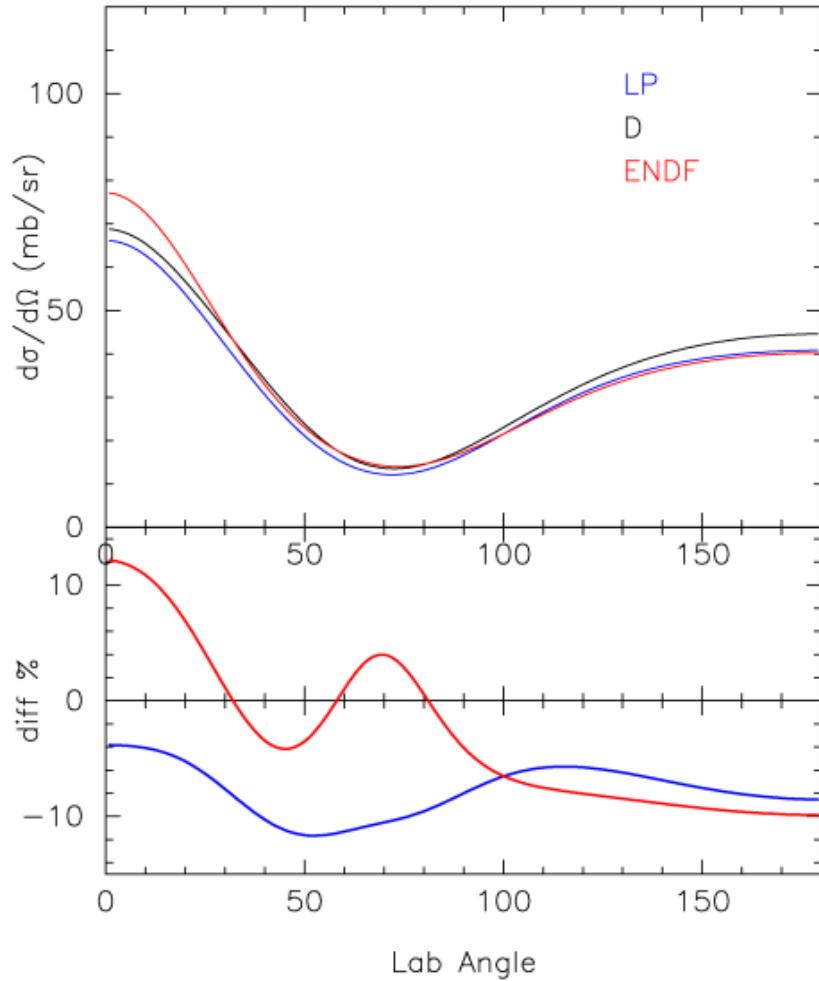
1

T(p,n) at $E_p = 4.0$ MeV

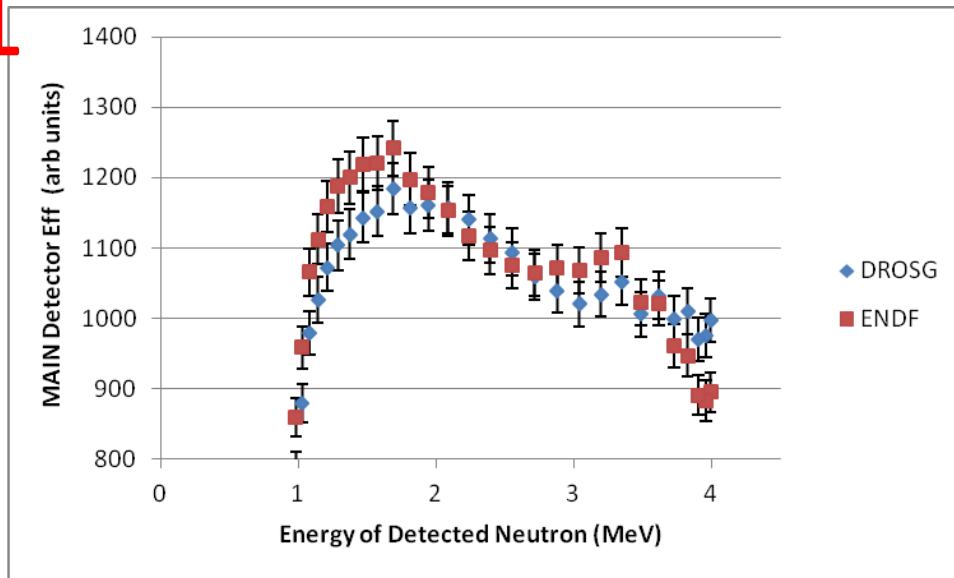
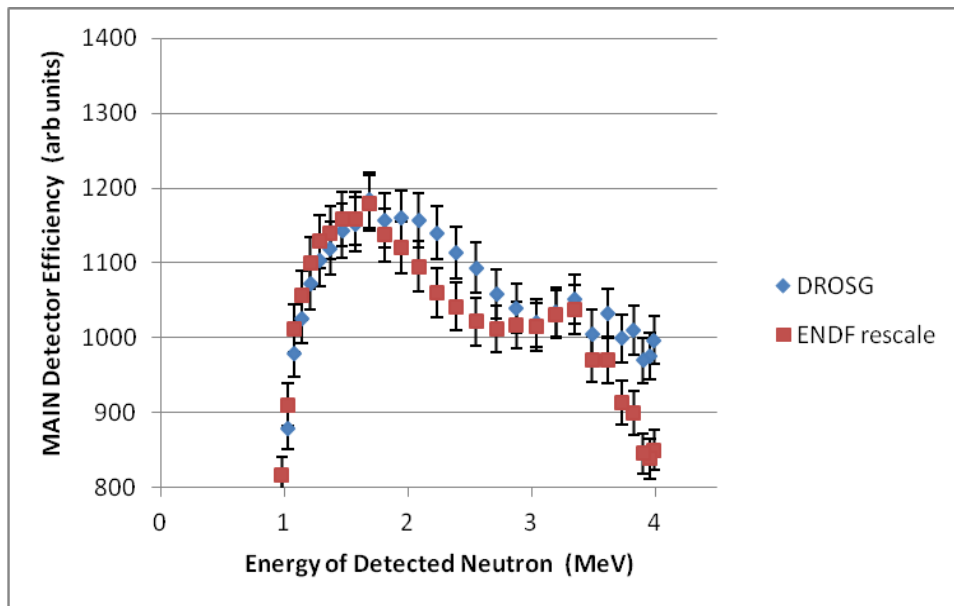


1

T(p,n) at $E_p = 5.0$ MeV



1

Efficiency Curve for $E_p=4.77$ MeV / $E_n = 4.0$ 

Same as above, but rescaled to accentuate differences.

Example Efficiency Curve

$$E_p=4.77 / E_{n,max} = 4.0$$

Reaction	Angular Range	$E_{scattered}$ (MeV)
$^{23}\text{Na}(n,n0)$	30-150	3.95-3.43
$^{23}\text{Na}(n,n0)$	30-150	3.52-3.02
$^{23}\text{Na}(n,n0)$	30-150	1.87-1.52
Normalization $\text{H}(n,n)$	30-50	3.00-1.65

1

Comparisons at Various Energies

Table B.2 Comparison of the three approaches for T(p,n) upon the $eff(E_n)$

Energy for Efficiency curve	Comments
4.00	D has much better anticipated shape vs ENDF. LP tracks D but up to +9% in the 2.4-3.5MeV range
3.60	D has better shape than ENDF. LP and D almost exactly the same.
3.57	D has better shape than ENDF. LP and D almost exactly the same.
3.50	D has slight upturn, ENDF maybe better? LP at forward angles similar to ENDF
3.40	D better than ENDF. LP & D very similar.
3.07	LP & ENDF actually very similar with the exception of the 0.9-1.3MeV region where ENDF can be as such a 6% higher. D has a +6% buldge 1.5-2.1MeV. Here if I had to pick the best, I'd guess the most realistic is ENDF or LP.
3.06	Very few points to judge with. Hard to make a call here. All very similar.
2.89	Dunno which one I'd choose here. No basis to choose one over the other.
2.05	Dunno which one I'd choose here. No basis to choose one over the other.
1.48	Dunno which one I'd choose here. No basis to choose one over the other.

$E_p < 4.0 \text{ MeV}$, no basis to chose one description over the other.

$E_p > 4.0 \text{ MeV}$, Drogg and Liskien & Paulsen preferred.

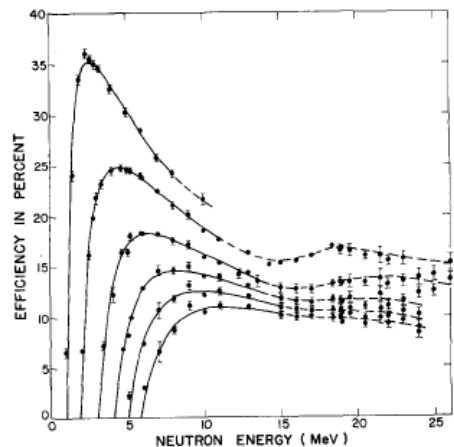


Fig. 4. Measured efficiency points for biases at 0.4, 1.0, 2.0, 3.0, 4.0 and 5.0 times Cs and calculated fits (solid lines). The dashed lines are handfitted.

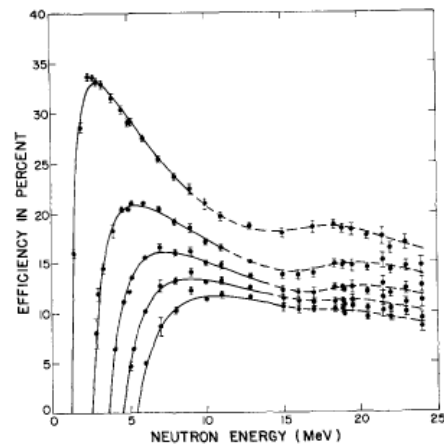


Fig. 5. Same as fig. 4, but for biases at 0.5, 1.5, 2.5, 3.5, and 4.5 times Cs.

ADVENTURES IN ANALYSIS

-- CONVERTING γ -RAY YIELDS TO CROSS SECTIONS

2

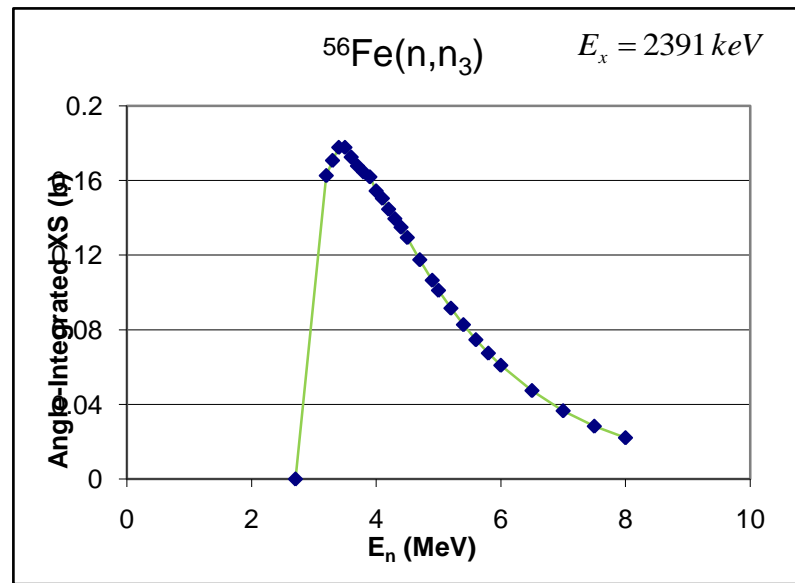
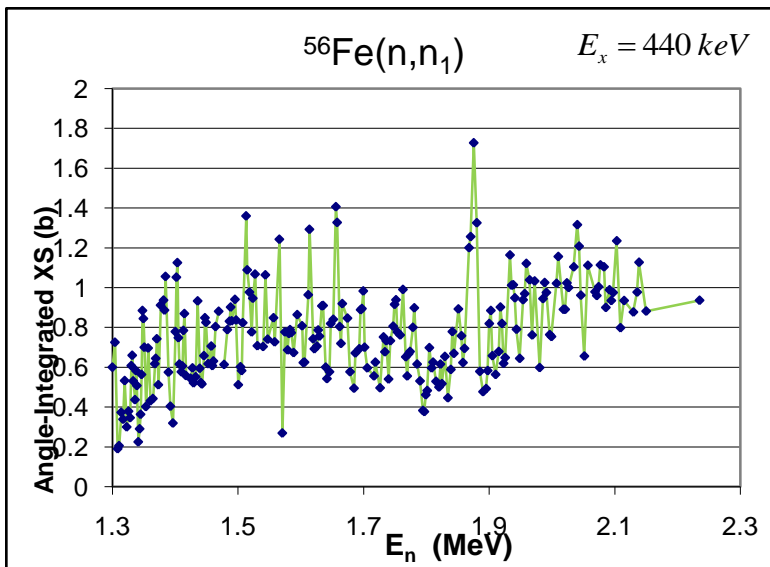
Scaling ^{23}Na Yields to ENDF ^{56}Fe Cross Sections

-- use γ -rays from Fe sample to discover the conversion factor

$$\sigma_{Na, \gamma\text{-ray}i} \sim \frac{\text{Na Corrected Yield} / \#Na}{\text{Fe Corrected Yield} / \#Fe} \bar{\sigma}_{Fe}$$

Comparison to evaluated data

26-Fe- 56 LANL,ORNL EVAL-SEP96 M.B.Chadwick,P.G.Young,C.Y.Fu CH99,FU86,Fu91

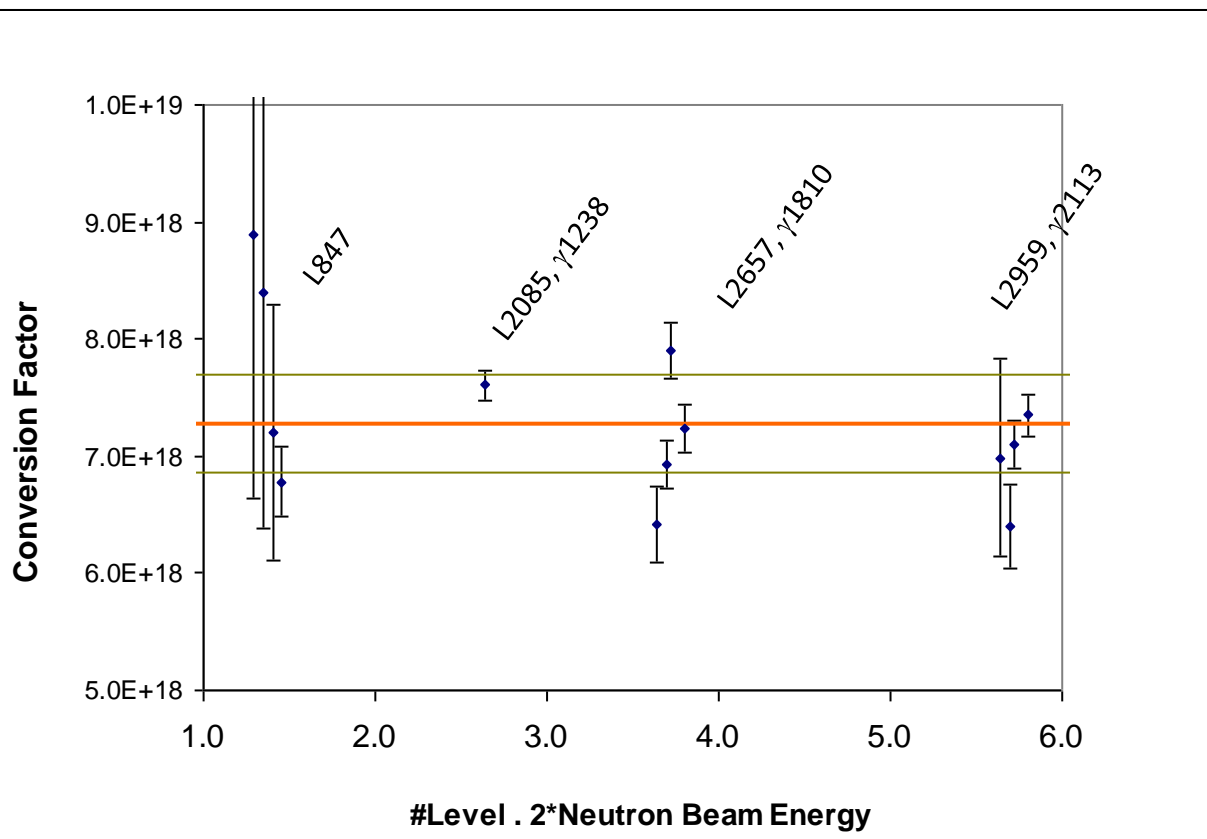


2

Scaling to ENDF ^{56}Fe Cross Sections

$$\sigma_{\text{Na},\gamma\text{-ray}i} \sim \frac{\text{Na Corrected Yield} / \# \text{Na}}{\text{Fe Corrected Yield} / \# \text{Fe}} \bar{\sigma}_{\text{Fe}}$$

$$\sigma_{\text{Na},\gamma\text{-ray}i} = \frac{\text{Na Corrected Yield}_{\gamma\text{-ray}i} / \# \text{Na}}{\left\langle \frac{\text{br}_{j\text{transition}k} \bar{\sigma}_{\text{Fe},\text{level } j}}{\text{Fe Corrected Yield}_{j\text{transition}k} / \# \text{Fe}} \right\rangle}$$

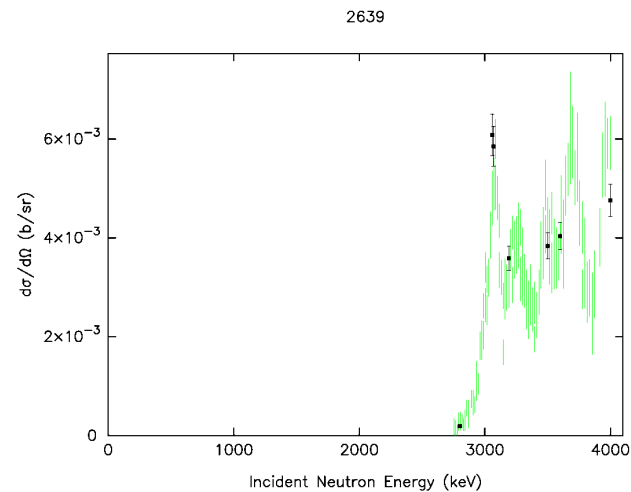
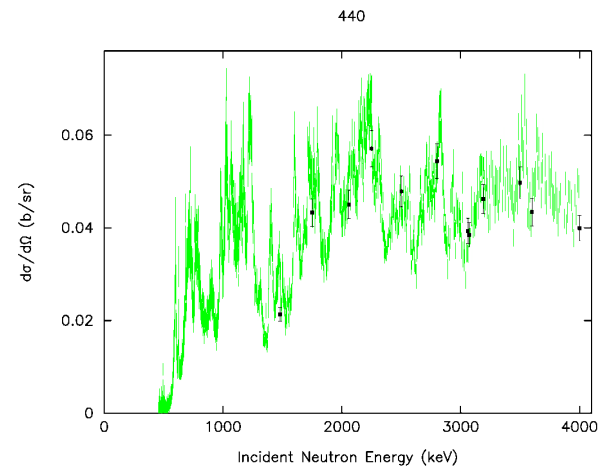
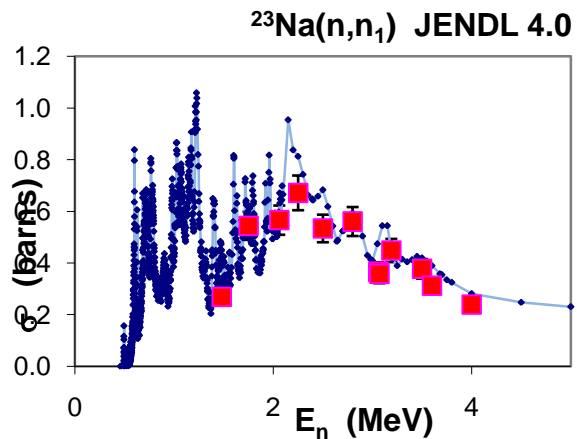
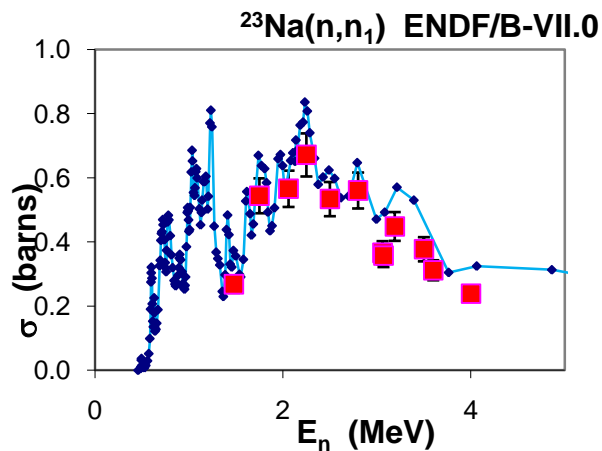


$$\langle \rangle = 7.27(41) \bullet 10^{18}$$

uncertainty ~ 6%

$$\bar{x} = \frac{\sum w_i x_i}{\sum w_i} \quad w_i = \frac{1}{\sigma_i^2}$$

$$\sigma^2 \approx \frac{N \sum w_i (x_i - \bar{x})^2}{(N-1) \sum w_i}$$

$^{23}\text{Na}(n,n'\gamma)$ 

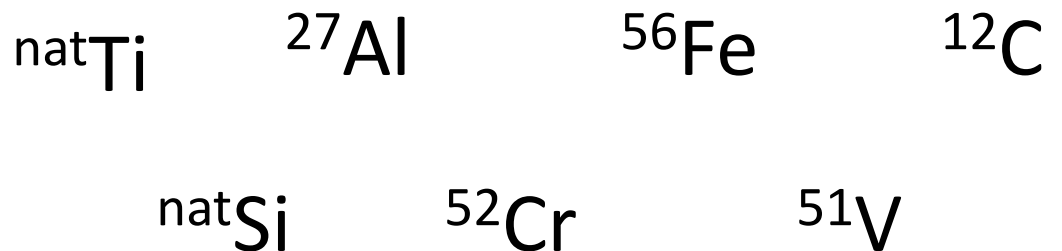
Comparison of inelastic (n,n_1) cross sections as determined from $(n,n'\gamma)$ measurements with values in the evaluated nuclear libraries. ENDF over-predicts the data by $\sim 15\%$, while the data track JENDL quite nicely. The JEFF library (not shown) undershoots the data by $\sim 15\%$.

Comparison of measured γ -ray excitation functions with those of the GELINA/IRMM group [Rouki *et al*, NIM A 673, 83 (2012)]. UnivKY data points are in black. The agreement is striking considering the experiments use different normalization techniques and the neutron energy resolutions are significantly different.

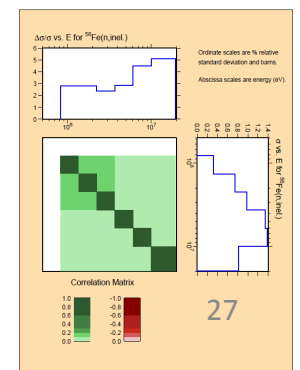
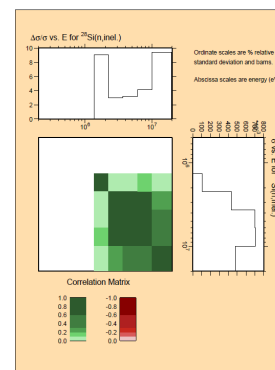
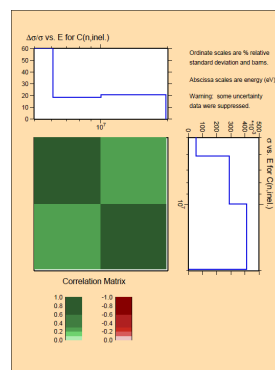
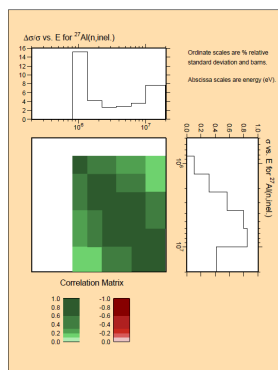
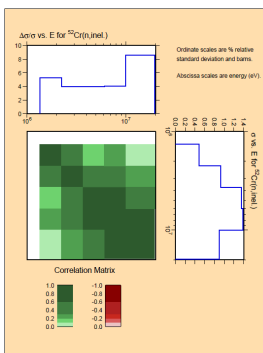
Use several samples in an attempt to average out the deficiencies of each?

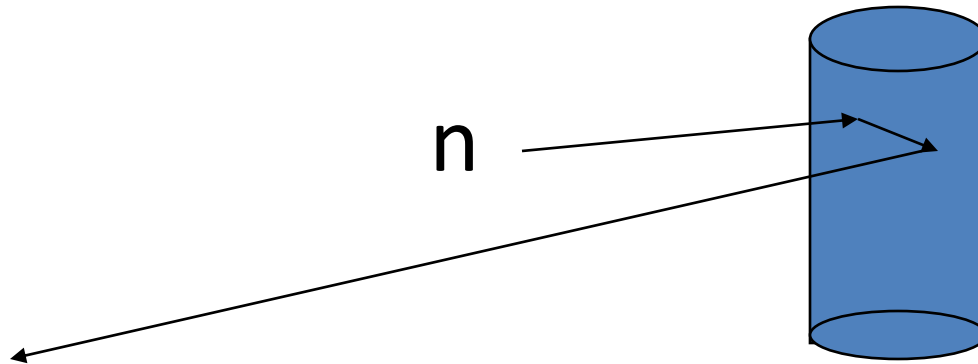


Unfortunately this produces 'better estimates' rather than "2ndry standards"



Oblozinsky, "Progress on Nuclear Covariances: AFCI-1.2 Covariance Library" BNL-90897-2009





ADVENTURES IN ANALYSIS

-- ATTENUATION AND MULTIPLE SCATTERING CORRECTIONS

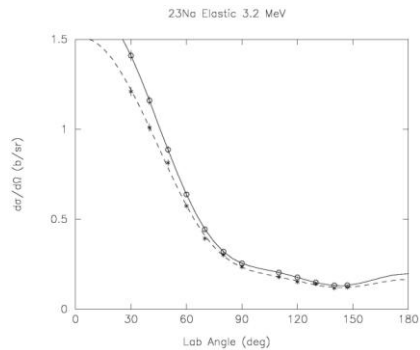
MT McEllistrem MULCAT (...)

JR Lilley "...Monte Carlo Multiple Scattering Correction...", CEA-DAM P2N-934-80 (1980)

DE Velkey, "... with Analytic & Monte Carlo Methods", NIM 129, 231 (1975)

WE Kinney "Finite Sample Corrections..." NIM 83, 15 (1970).

3 Multiple Scattering and Attenuation Correction using MULCAT

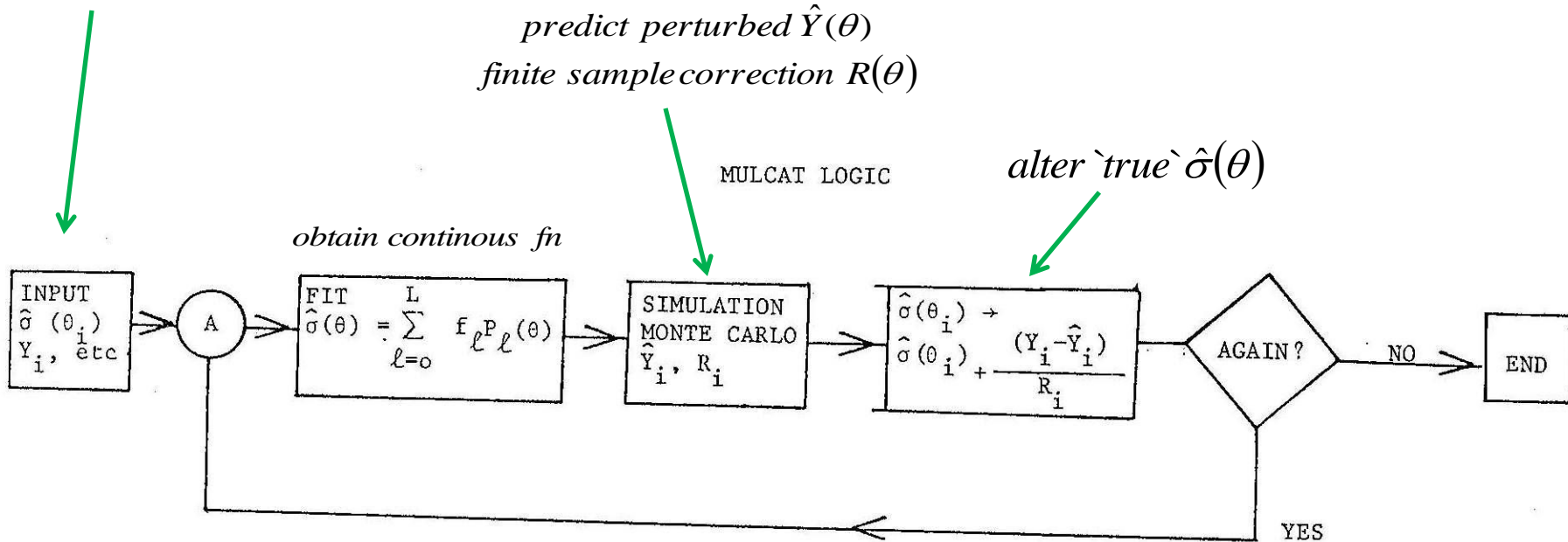


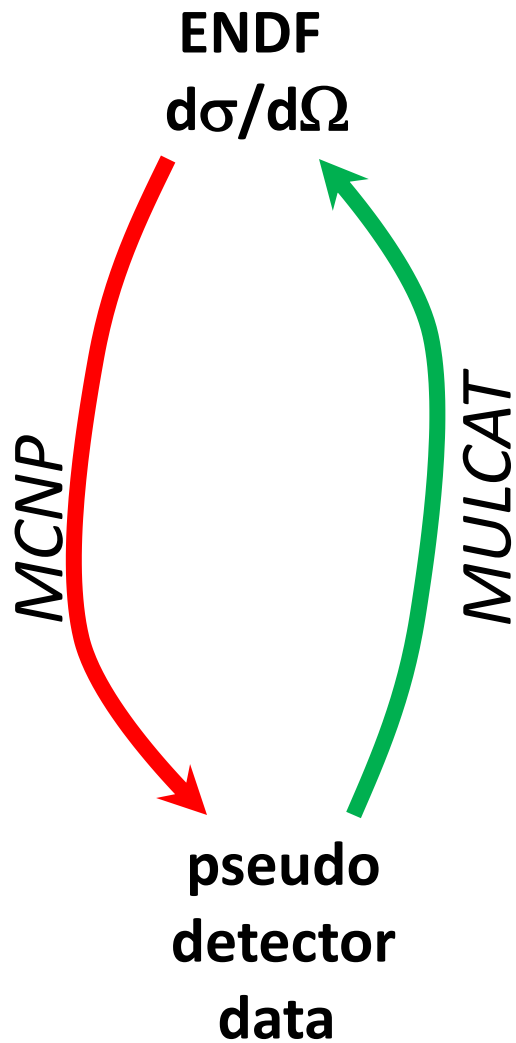
for a typical sample:
 $\Sigma_{\text{tot}}^{-1} \sim 16 \text{ cm}$
 double/singl = 10^{-4}
 triple/dble = 10^{-4}

- Issues
 - Single element
 - Extensive experience using the routine on medium-mass nuclei
 - Limited # of $\sigma_{\text{tot}}(E_n)$ values
 - Elastic angular distribution used at one E_n
 - Runs **** histories

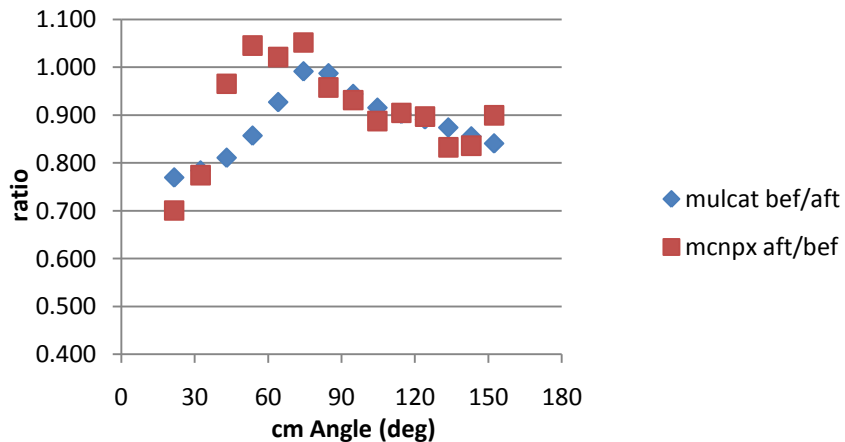
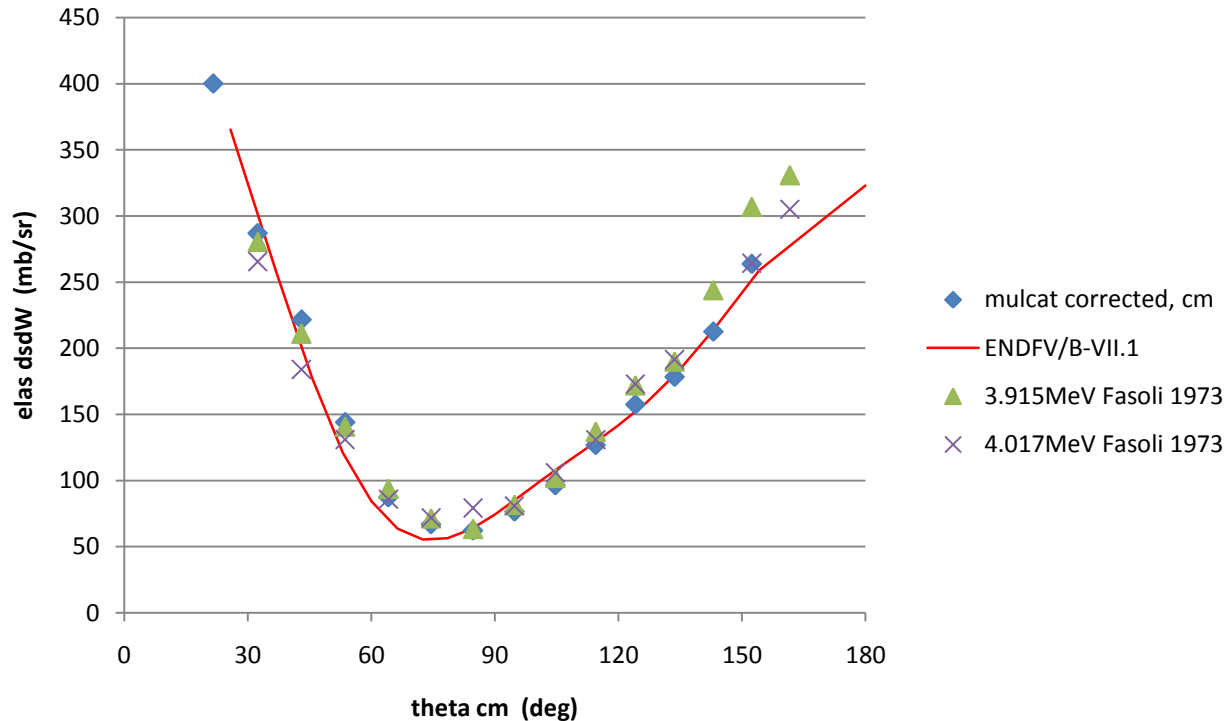
init guess at `true` $\hat{\sigma}(\theta)$
finite sample $Y(\theta)$

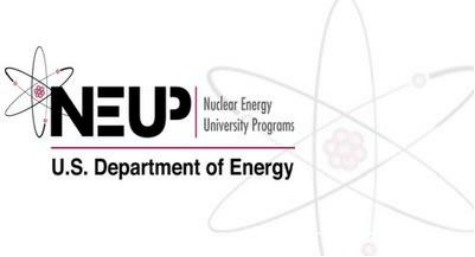
predict perturbed $\hat{Y}(\theta)$
finite sample correction $R(\theta)$





mulcat-corrected mcnp calculation: 12C





- General Intro to the Laboratory
- Sample results for recent ^{23}Na , ^{54}Fe , $^{\text{nat}}\text{Fe}$ (n,n') & ($n,n'\gamma$)
- Adventures in Analysis
 - Ambiguities in Neutron Detection Efficiency attributed to $^3\text{H}(p,n) d\sigma/d\Omega$
 - The technique
 - Choices for $d\sigma/d\Omega$
 - Impact on Efficiency (E)
 - Challenges in Normalizing ($n,n'\gamma$)
 - What we did for $^{23}\text{Na}(n,n'\gamma)$
 - What will we do for $^{54,56}\text{Fe}$?
 - How well do we know the finite geometry corrections?
 - Proving our correction code is rigorous
- Conclusion



DATA REDUCTION OVERVIEW FOR (N,N') & (N,N'G)

$(n, n'\gamma)$



Na (n, n'γ) spectrum

Extract γ Peak Yields

1 Correct for Detector Efficiency

Normalize to LongCounter*, #Na

2 Correct for n, γ Atten & n Multiple scatt

Convert to Cross Section



Fe (n, n'γ) spectrum

Extract γ Peak Yields

Correct for Detector Efficiency

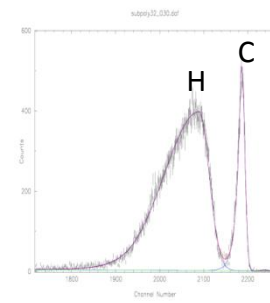
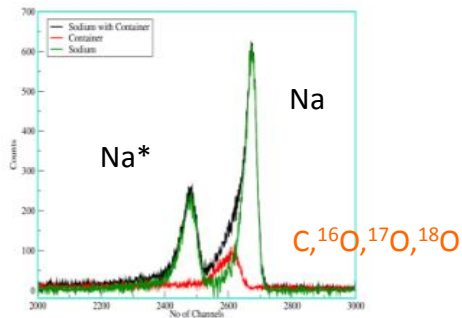
Normalize to LongCounter*, #Fe

Correct for n, γ Atten & n Multiple scatt

3 Obtain scaling factor using ENDF Cross Sections



2



Sample spectrum

Container spectrum

Polyethylene spectrum

3

Na ← Sample - Cont.

Extract Peak Yields

Extract Peak Yields

1

Correct for Detector Efficiency

Correct for Detector Efficiency

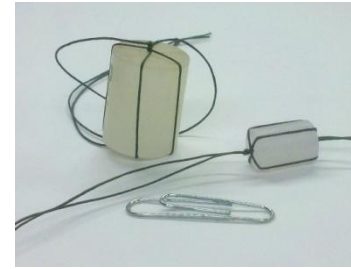
4

Convert to raw Cross Section

2

Correct for Atten & Multiple scatt





Sample spectrum

Container spectrum

Polyethylene spectrum

3

Na \leftarrow Sample - Cont.

Extract Peak Yields

1

Correct for Detector Efficiency

4

Convert to raw Cross Section

2

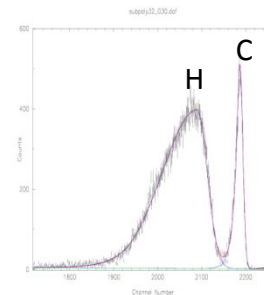
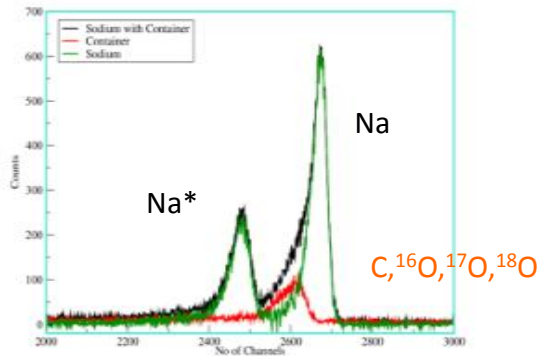
Correct for Atten & Multiple scatt

Extract Peak Yields

Correct for Detector Efficiency



3



Sample spectrum

Container spectrum

Polyethylene spectrum

3

$Na \leftarrow Sample - Cont.$

Extract Peak Yields

Extract Peak Yields

1

Correct for Detector Efficiency

Correct for Detector Efficiency

4

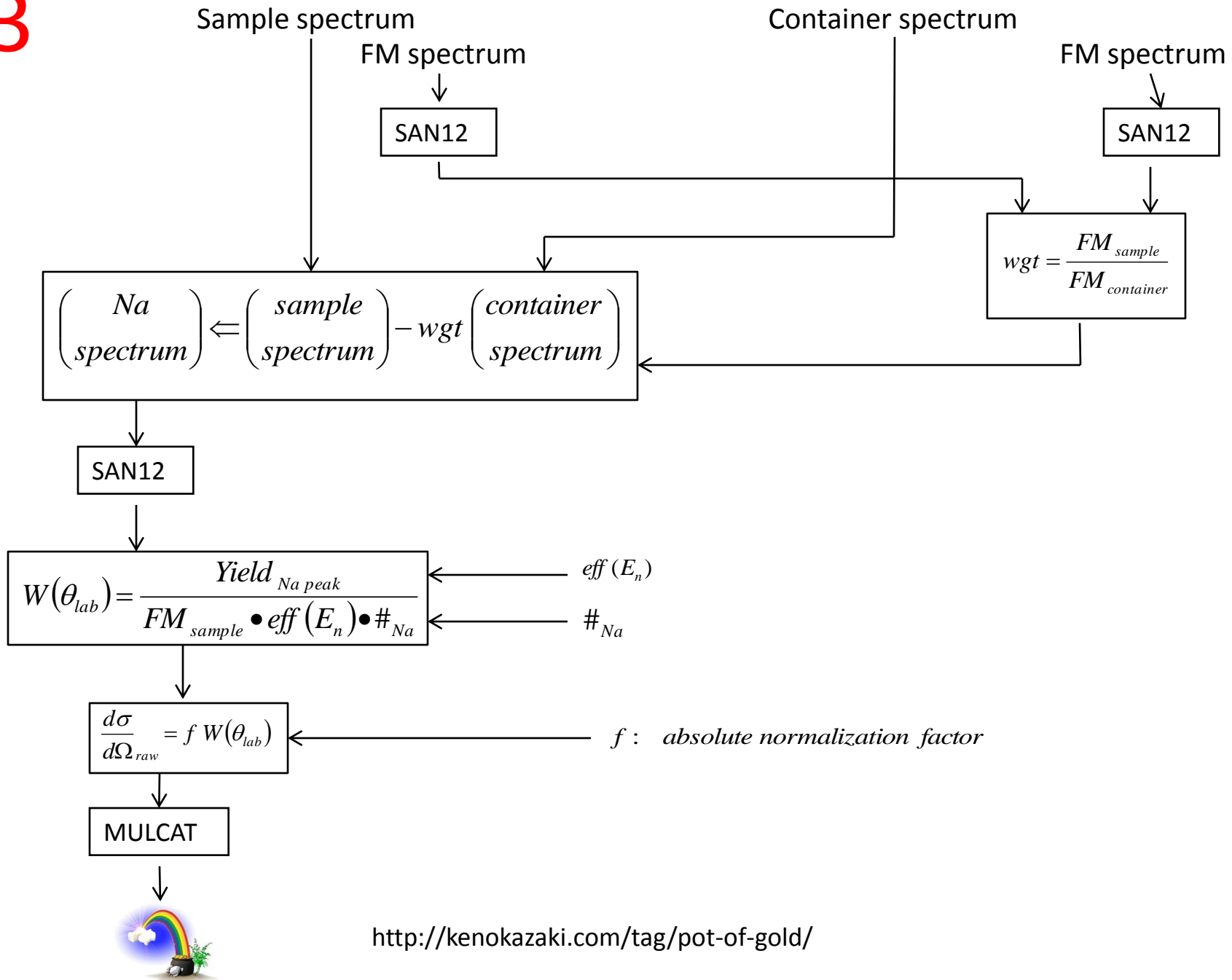
Convert to raw Cross Section

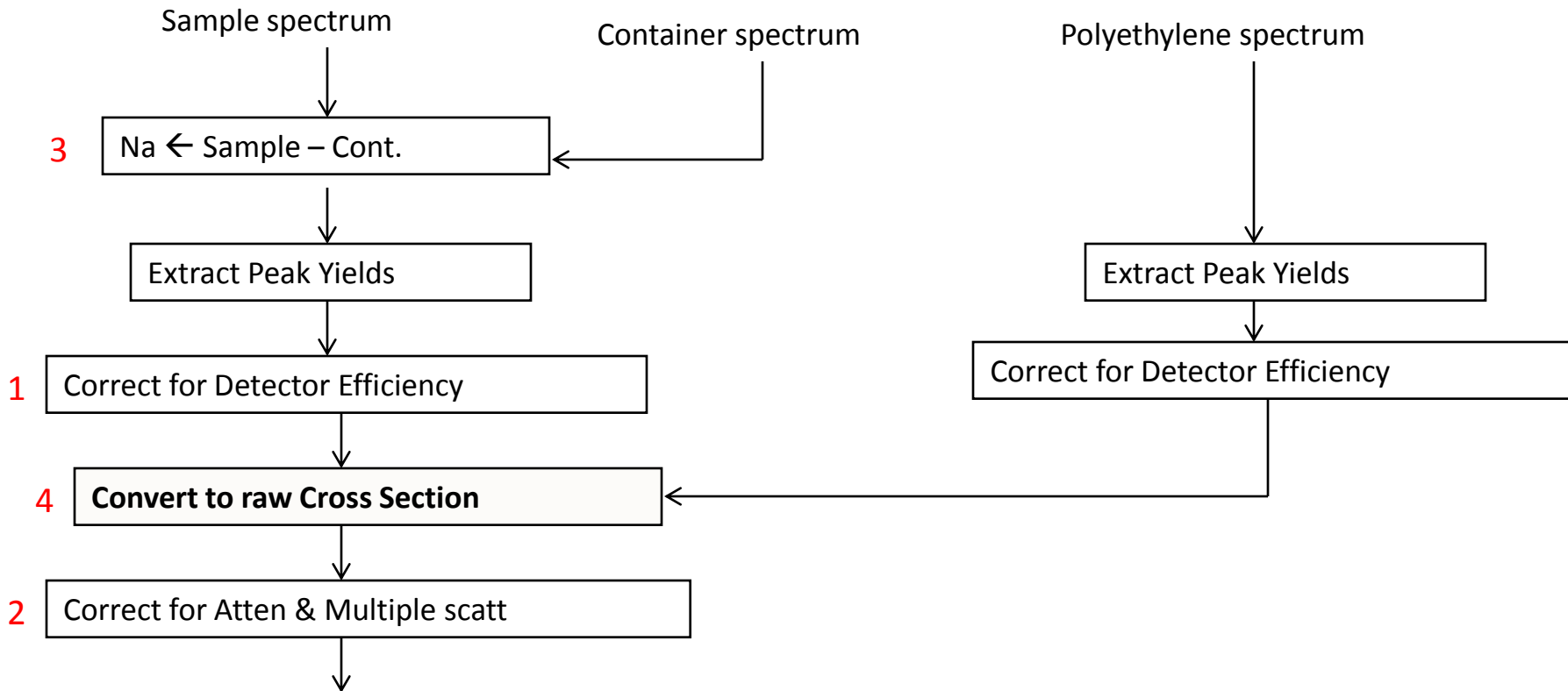
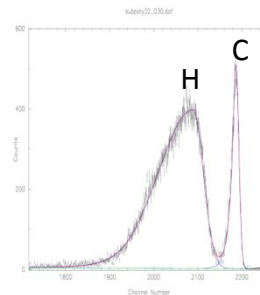
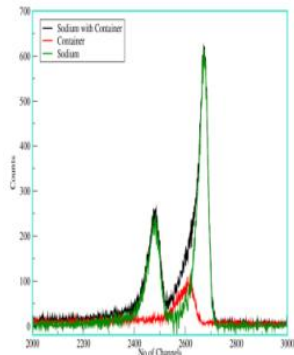
2

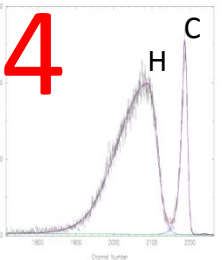
Correct for Atten & Multiple scatt



3





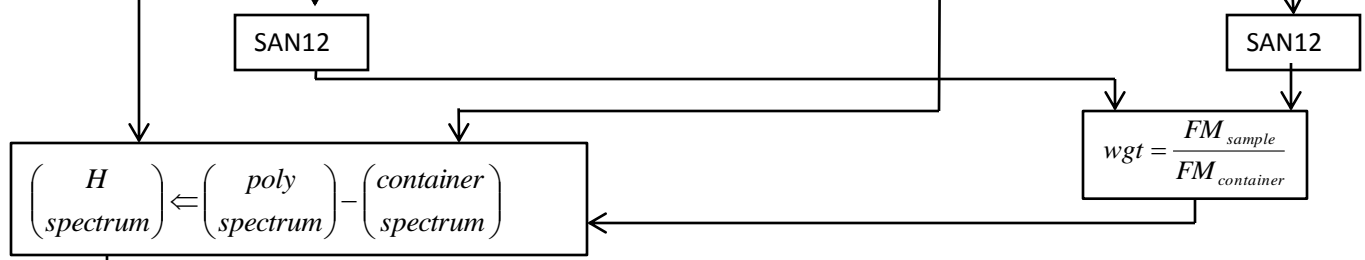


polyethylene spectrum

Blank spectrum

FM spectrum

FM spectrum



SAN14

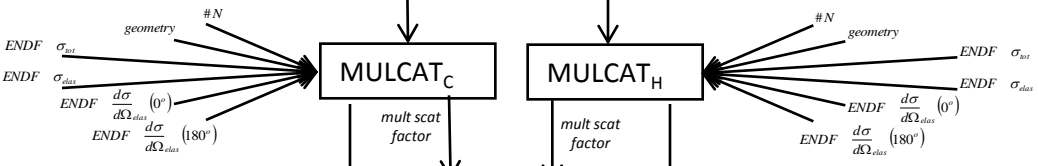
$$W_H(\theta_{lab}) = \frac{Yield_{H\ peak}}{FM_H \cdot eff(E_n) \cdot \#_H}$$

← $eff(E_n)$
← $\#_H$

$$W_{tot} = \int W_H(\theta) d\Omega$$

$$f = \frac{\sigma_{elas}}{W_{tot}}$$

$$\frac{d\sigma}{d\Omega_{H,raw}} = f W(\theta_{lab})$$



weighted mult scat

$$\frac{d\sigma}{d\Omega_{H,primitive}} = \frac{d\sigma}{d\Omega_{H,raw}} / \text{atten}_C \text{ atten}_H \text{ multscat}$$

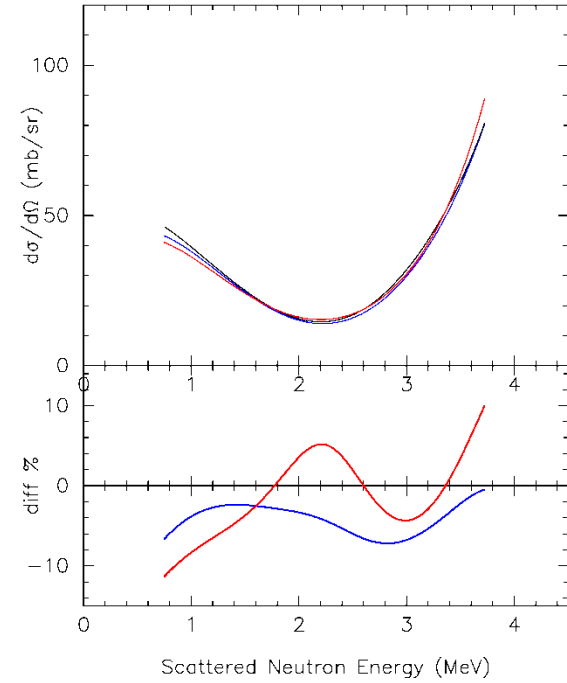
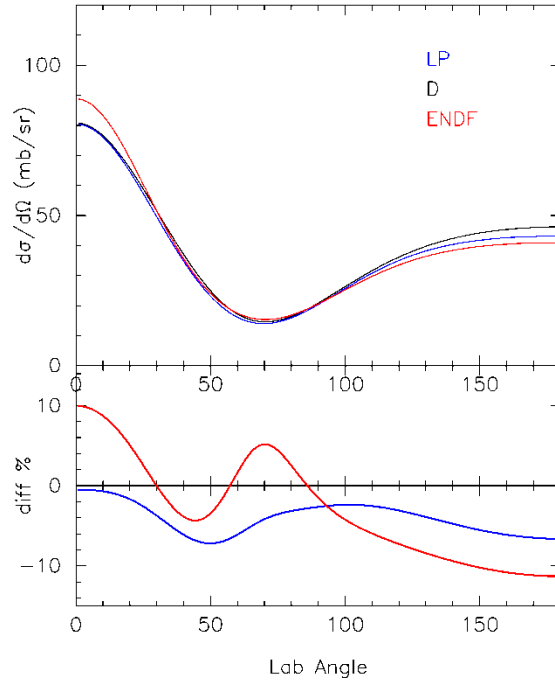
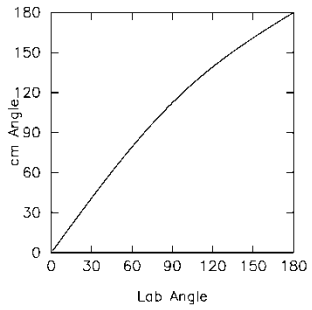
$$f \leftarrow r f$$

$$r = \frac{\sigma_{H,evaluated}}{\sigma_{H,check}}$$

$$\sigma_{check} = \int \frac{d\sigma}{d\Omega_{primitive}} d\Omega$$

(should get r = 1.00)

$E_p = 4.5 \text{ MeV}$



Ambiguities in Neutron Detection Efficiency attributed to ${}^3\text{H}(p,n)$ dsdW -- choices for dsdW --

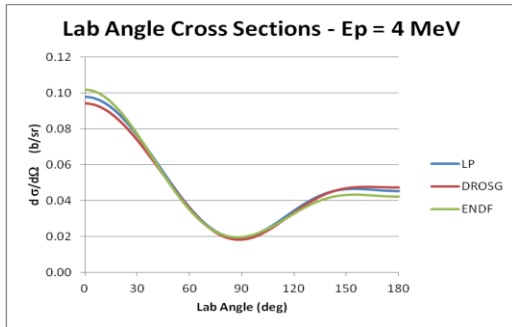
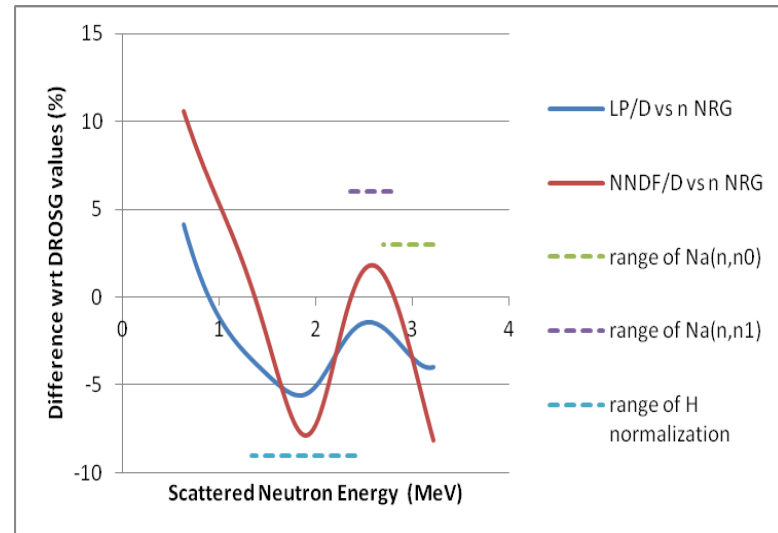
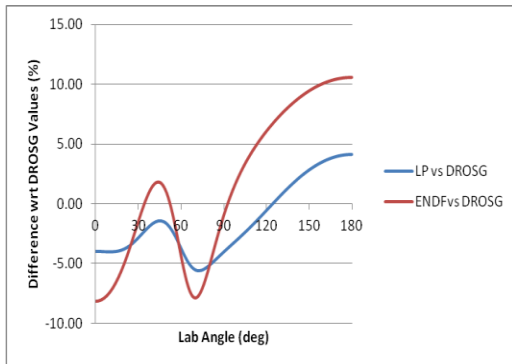
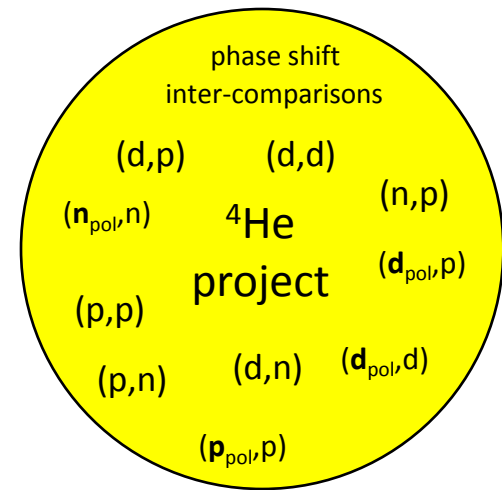


FIG. 6. Comparison of the three reference $T(p,n)$ cross sections at $E_p=4$ MeV. The lower subfigure displays the percentage difference with respect to the DROSG parameterization. Differences between descriptions can be as much as $\pm 10\%$ and vary with angle.



1 Actually need $d\sigma/d\Omega$



94

H.M. Hoffmann, G.M. Hale / Nuclear Physics A 613 (1997) 69–106

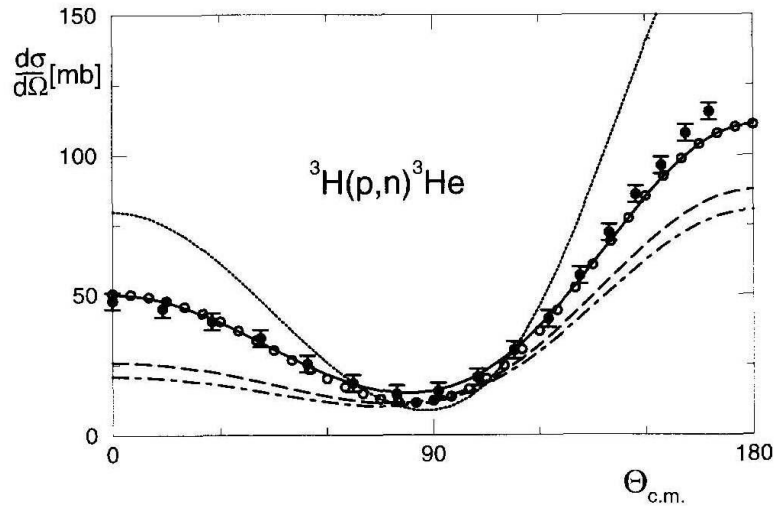


Fig. 18. Differential cross section of the reaction ${}^3\text{H}(p,n){}^3\text{He}$ calculated for $E_{\text{cm}} = 3.0$ MeV. The for 4.101 MeV protons from Ref. [31]. The labeling is as in Fig. 16.

solid line R-matrix analysis

$d\sigma/d\Omega$ predictable to

- <5% for $\theta_{\text{cm}} < 50^\circ$
- Really good for $50^\circ < \theta_{\text{cm}} < 140^\circ$

H. M. HOFMANN AND G. M. HALE

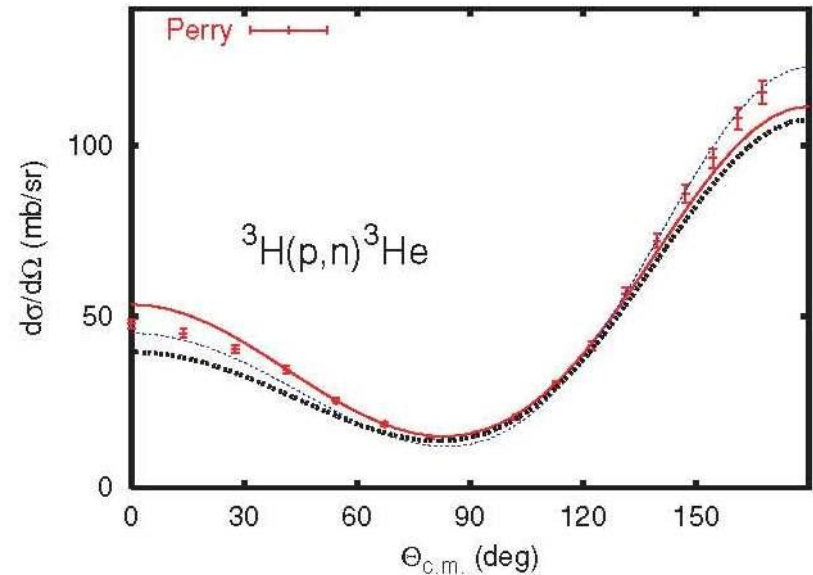
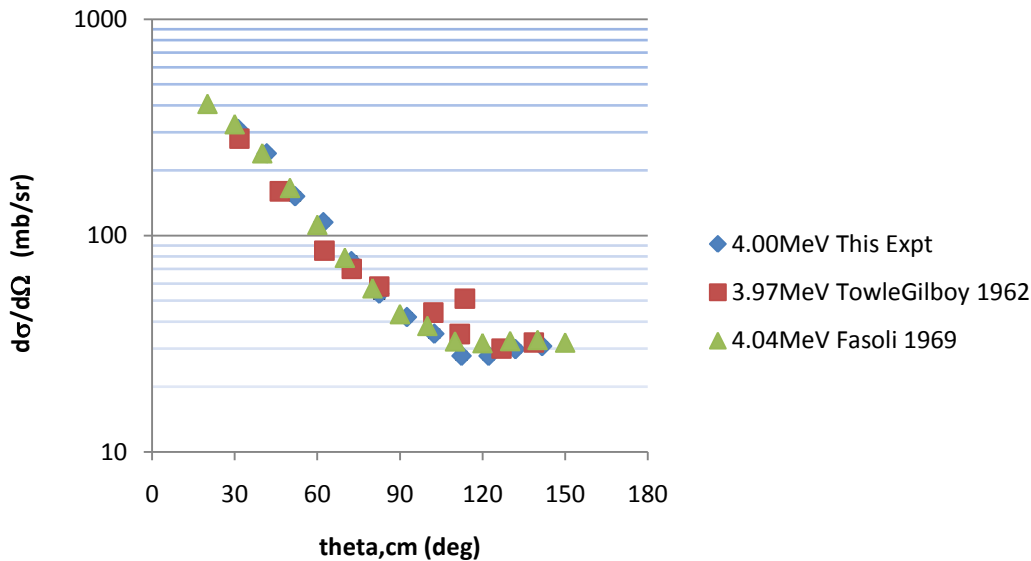


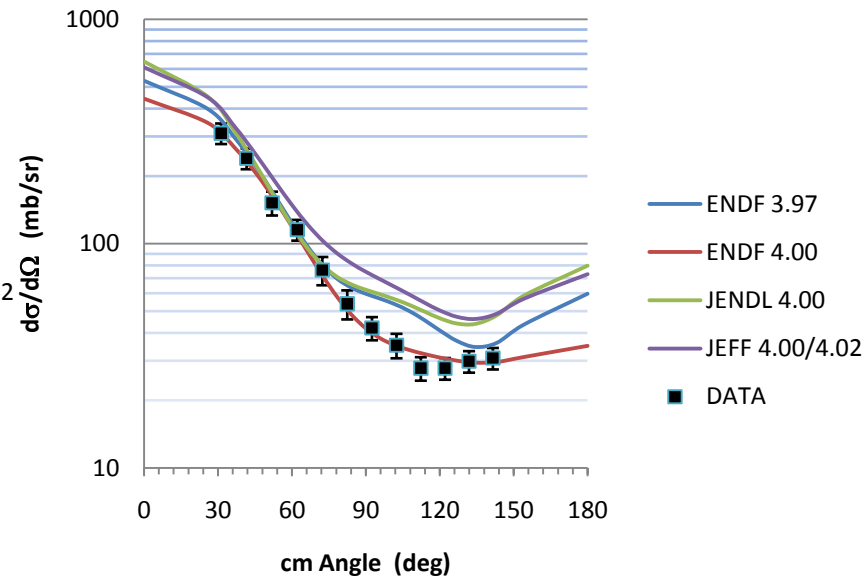
FIG. 17. (Color online) Differential cross section for the reaction ${}^3\text{H}(p,n){}^3\text{He}$ calculated at 3.0 MeV E_{cm} . The data at 3.08 MeV are from Perry *et al.* [43].

$^{23}\text{Na}(n,\text{el})$

(n,el) 4.00 MeV



(n,el) 4.00 MeV

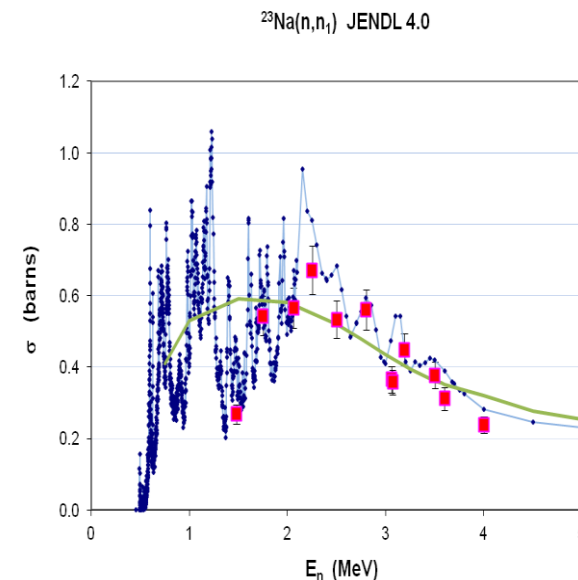
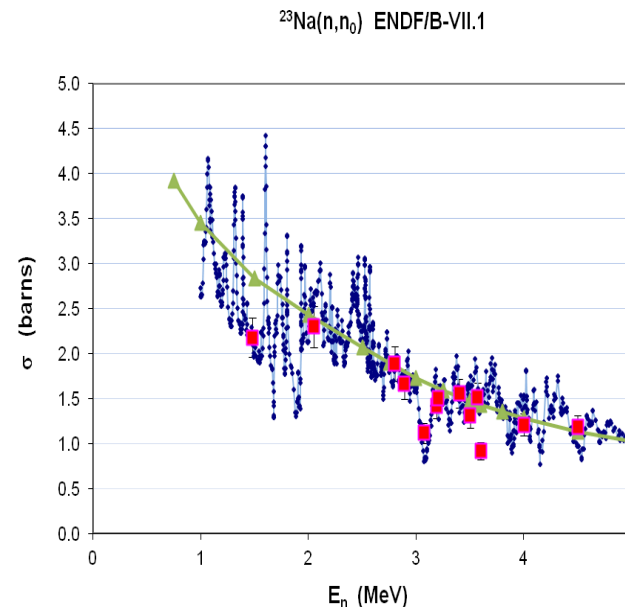
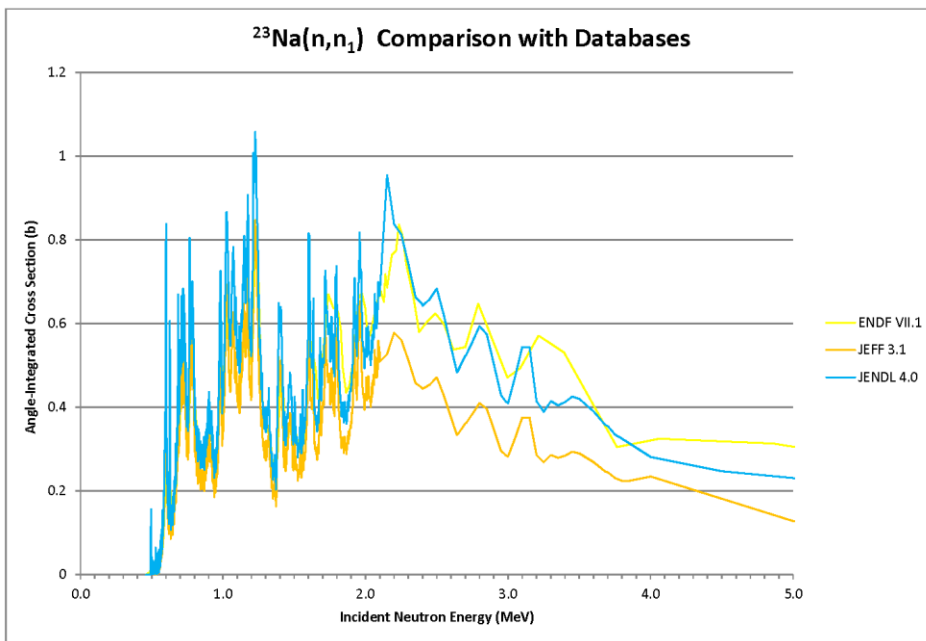
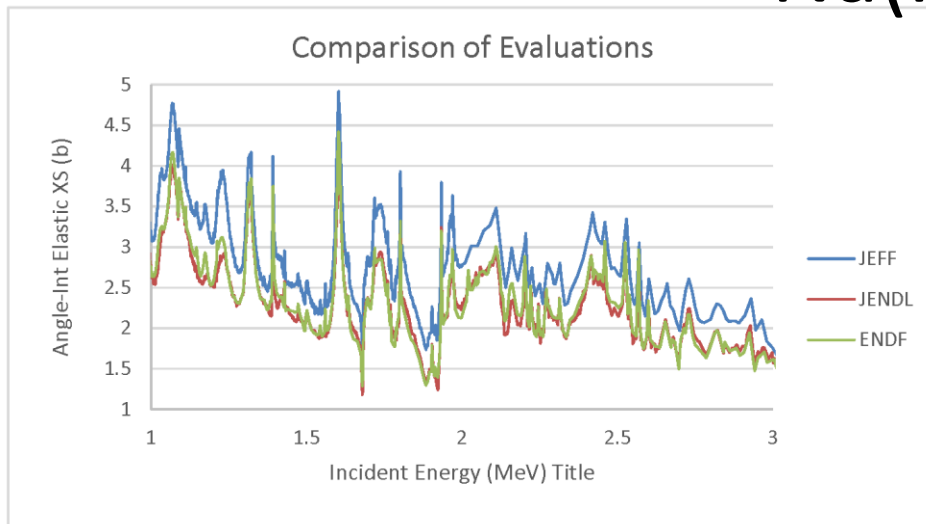


Comparison of our elastic cross sections to previous measurements (top) and the evaluated nuclear libraries (bottom). The shape of $d\sigma/d\Omega$ changes quickly at angles $>80^\circ$ with energy and is sensitive to the reaction mechanism.

EVALUATIONS

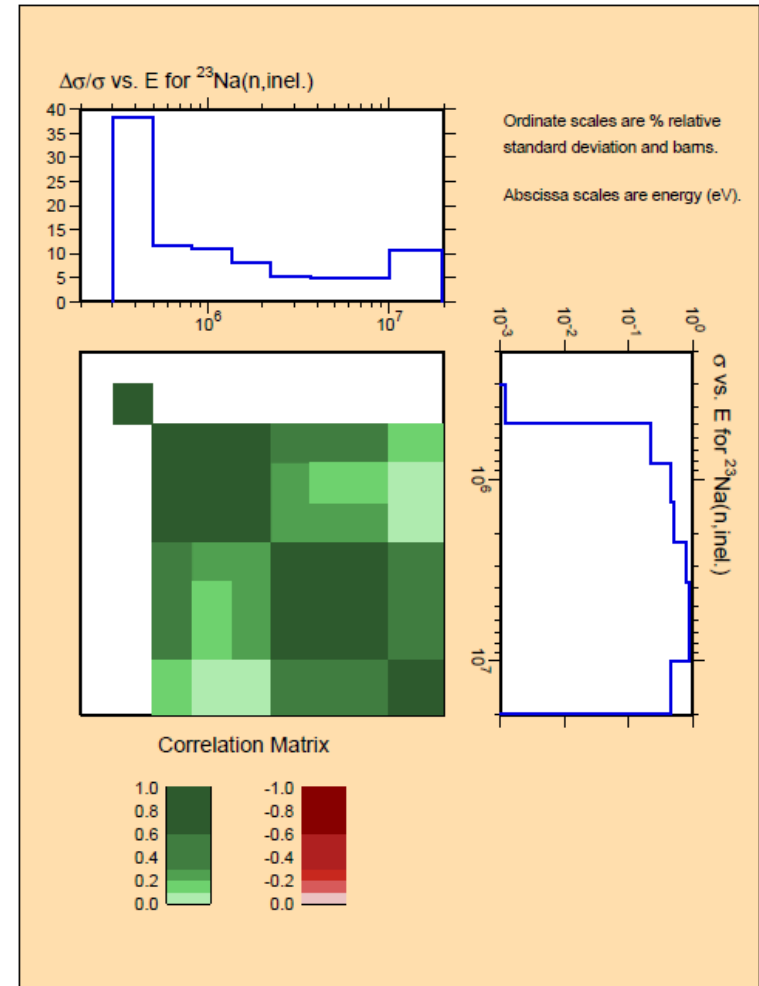
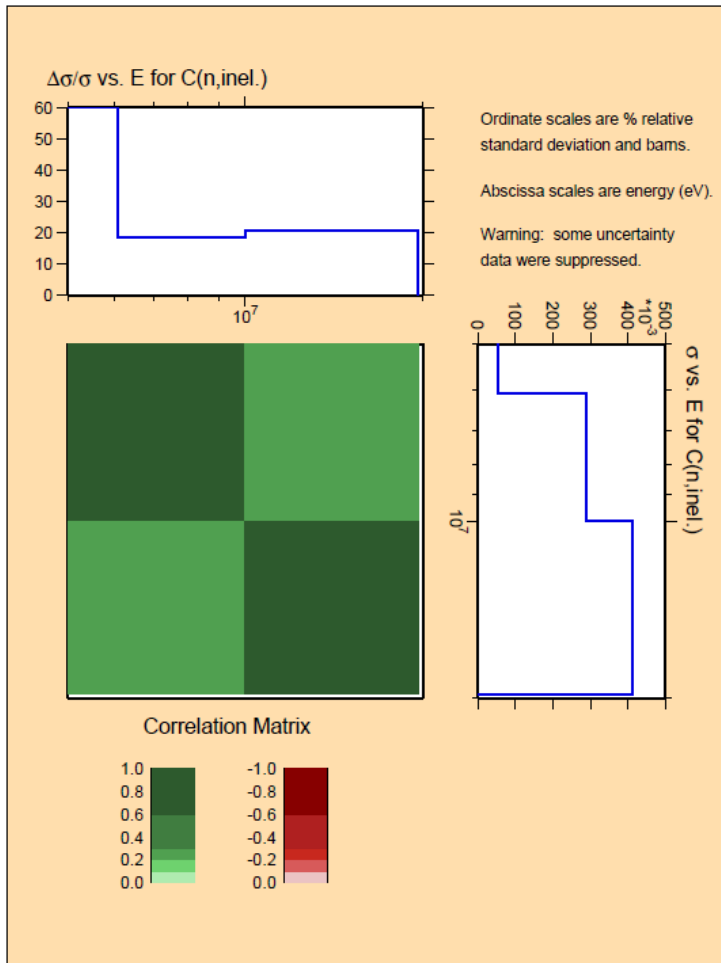
$^{23}\text{Na}(n,el)$

EXPERIMENTAL DATA

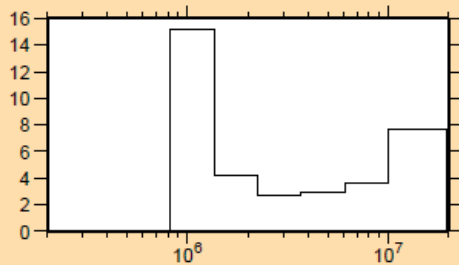


(LEFT: There can be significant disagreements between the libraries for cross sections. RIGHT: Our measurements determine the best choices. Our measurements indicate that both the ENDF & JENDL libraries have good values for elastics, while only the JENDL properly describes the inelastic.)

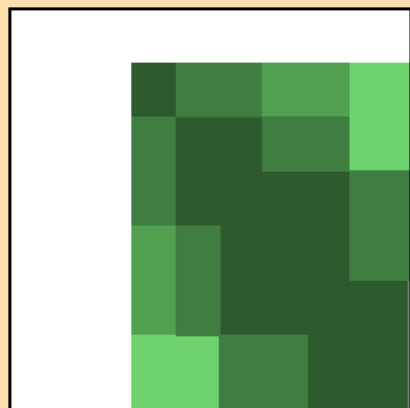
Oblozinsky, "Progress on Nuclear Covariances: AFCI-1.2 Covariance Library" BNL-90897-2009



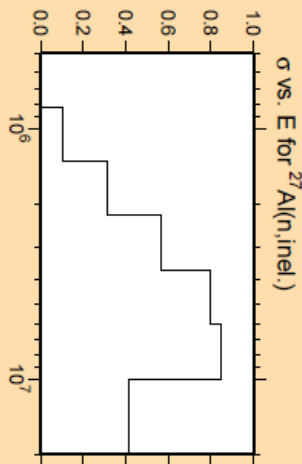
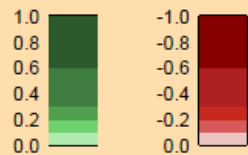
$\Delta\sigma/\sigma$ vs. E for $^{27}\text{Al}(n,\text{inel.})$



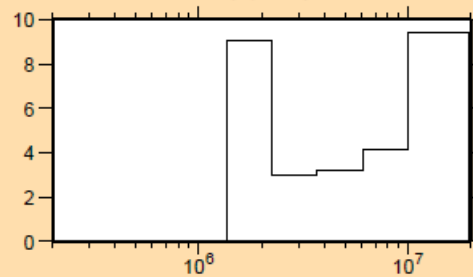
Ordinate scales are % relative standard deviation and bars.
Abscissa scales are energy (eV).



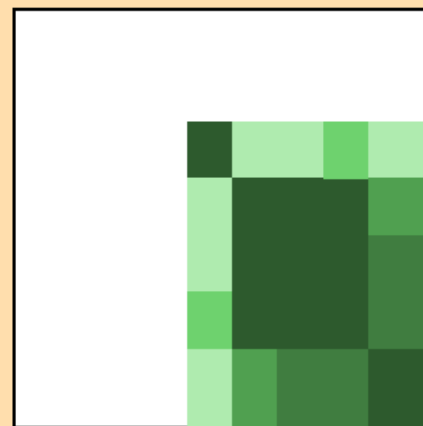
Correlation Matrix



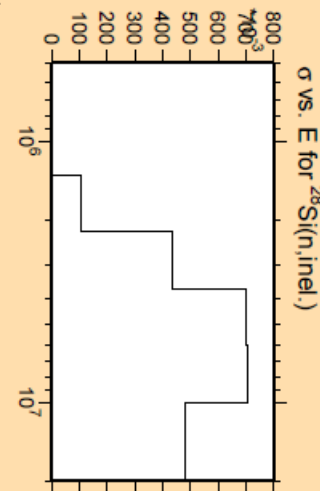
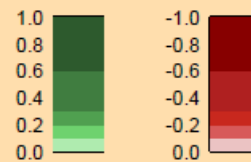
$\Delta\sigma/\sigma$ vs. E for $^{28}\text{Si}(n,\text{inel.})$



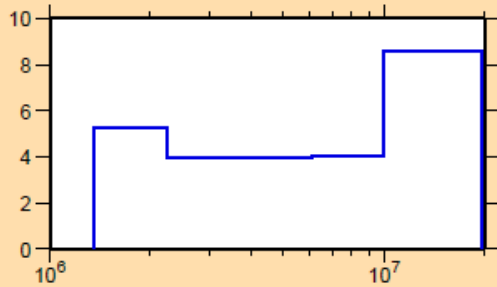
Ordinate scales are % relative standard deviation and bars.
Abscissa scales are energy (eV).



Correlation Matrix

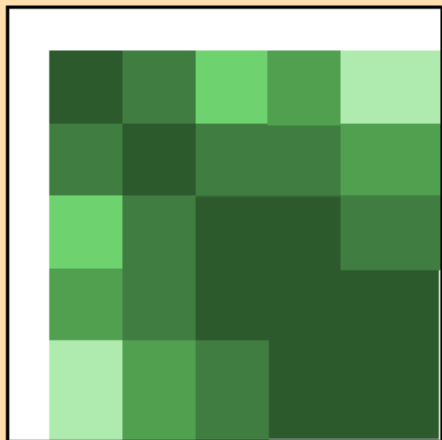


$\Delta\sigma/\sigma$ vs. E for $^{52}\text{Cr}(n,\text{inel.})$

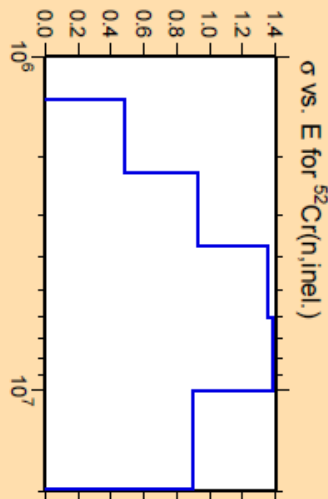
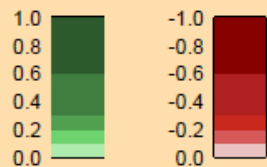


Ordinate scales are % relative standard deviation and bars.

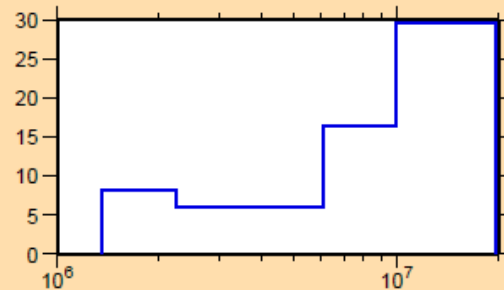
Abscissa scales are energy (eV).



Correlation Matrix

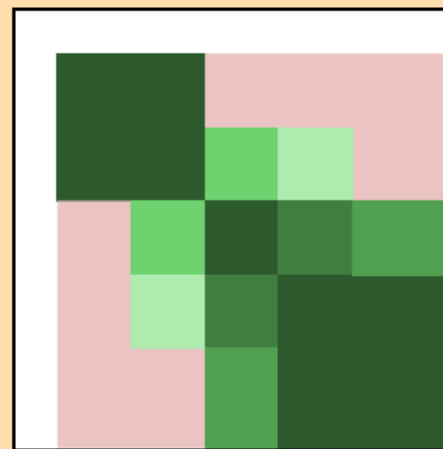


$\Delta\sigma/\sigma$ vs. E for $^{54}\text{Fe}(n,\text{inel.})$

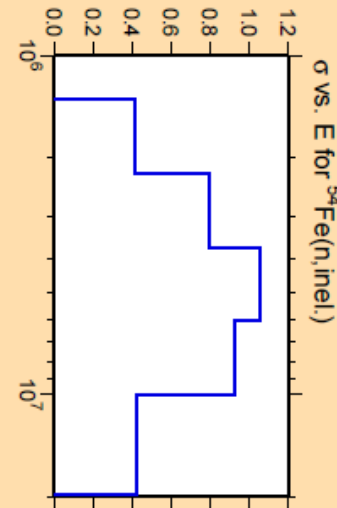
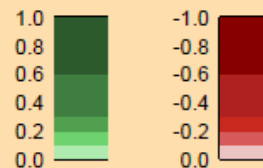


Ordinate scales are % relative standard deviation and bars.

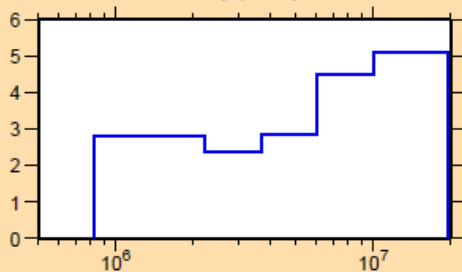
Abscissa scales are energy (eV).



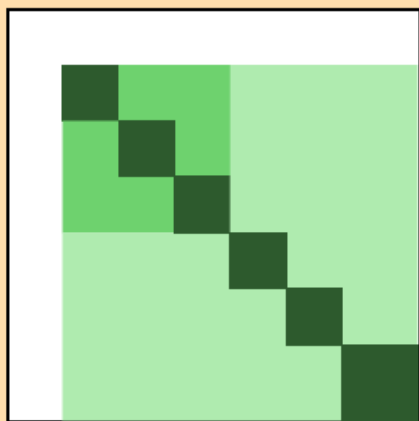
Correlation Matrix



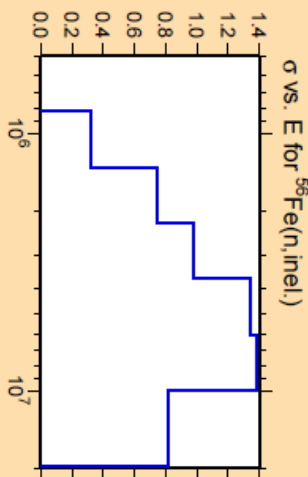
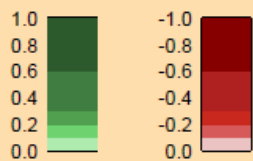
$\Delta\sigma/\sigma$ vs. E for $^{56}\text{Fe}(n,\text{inel.})$



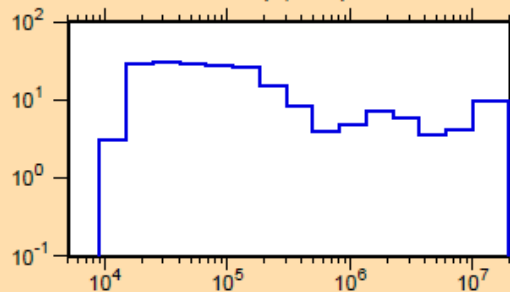
Ordinate scales are % relative standard deviation and bars.
Abscissa scales are energy (eV).



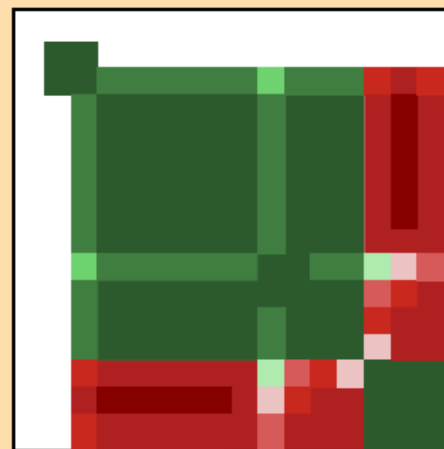
Correlation Matrix



$\Delta\sigma/\sigma$ vs. E for $^{57}\text{Fe}(n,\text{inel.})$



Ordinate scales are % relative standard deviation and bars.
Abscissa scales are energy (eV).



Correlation Matrix

