

Reproducibility in light-element evaluations

NEA/WPEC/Subgroup 49

Reproducibility in Nuclear Data Evaluation

Mark Paris & Gerry Hale

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Outline

- **EDA** evaluation pipeline
 - Overview/reminder
- *High-fidelity, unitary R-matrix* approach
 - Simultaneous evaluation of *all* data
- Evaluation reproduction
 - Challenges in push-button/script-driven reproducibility for our approach

NB: our evaluation approach is currently heavily hand-spun

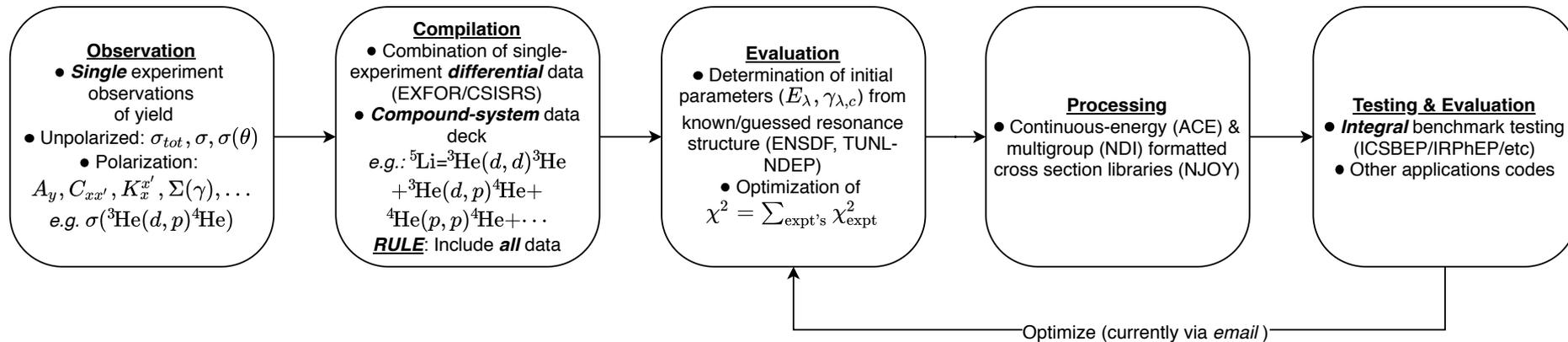
- Automation *limited* but *under development*

Overview/reminder

Light-element evaluation

Nuclear Data Pipeline

EDA cross section evaluation

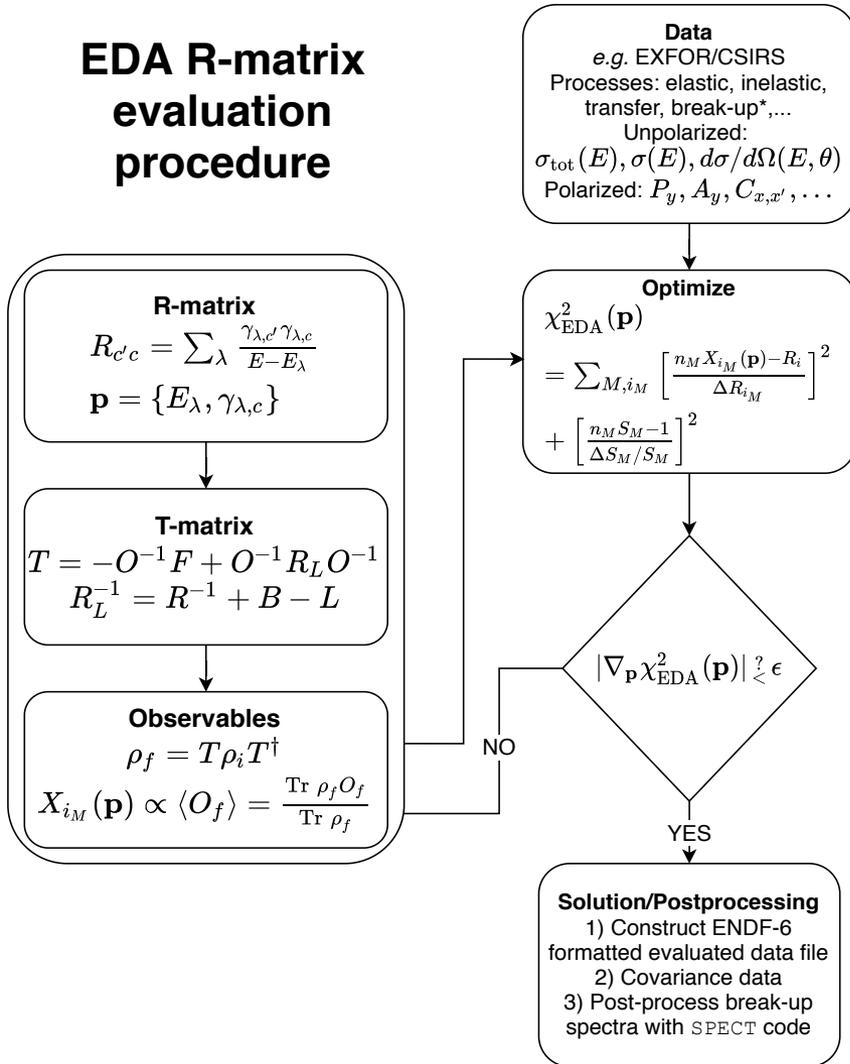


- Data-cull: observables from single experiments are compiled
- Evaluation: one set of variational parameters for all data
 - Unitary parametrization: highly constraining between different processes
 - Elastic & reaction cross sections are coupled in complex ways
 - Not simply drawing smooth curves
- Processing

R-matrix evaluation

⁵Li system

EDA R-matrix evaluation procedure



| Channel | a_c (fm) | l_{max} |
|--|------------|-----------|
| $d + {}^3\text{He}(\frac{1}{2}^+)$ | 4.8 | 4 |
| $p + {}^4\text{He}(0^+)$ | 2.9 | 4 |
| $p + {}^4\text{He}^*(0^+; 20.2 \text{ MeV})$ | 3.4 | 2 |
| $d_0 + {}^3\text{He}(\frac{1}{2}^+)$ | 5.1 | 0 |

| Reaction | Energy Range (MeV) | # Data Points | Observables |
|--------------------------------------|---------------------|---------------|---|
| ${}^3\text{He}(d, d){}^3\text{He}$ | $E_d = 0.32 - 10.0$ | 2,229 | $\sigma(\theta), A_i, A_{ii}, C_{i,j}, C_{ij,k}, K_{i,j'k'}, K_{ij,k'l'}$ |
| ${}^3\text{He}(d, p){}^4\text{He}$ | $E_d = 0.13 - 10.0$ | 3,839 | $\sigma(E), \sigma(\theta), A_i, A_{ii}, C_{i,j}, K_{ij,k'}$ |
| ${}^3\text{He}(d, p){}^4\text{He}^*$ | $E_d = 3.70 - 6.70$ | 28 | $\sigma(\theta)$ |
| ${}^4\text{He}(p, p){}^4\text{He}$ | $E_p = 0.92 - 34.3$ | 867 | $\sigma(E), \sigma(\theta), A_y, P_y$ |
| Total: | | 6963 | |

Table 1: Channel configuration (top) and data summary (bottom) for the ⁵Li system analysis. The column labeled “Observables” indicates the following data types: $\sigma(E)$, integrated cross section; $\sigma(\theta)$, unpolarized angular distributions (energy-dependence suppressed); A initial-state analyzing power; P final-state polarization; C spin correlation coefficients; K polarization transfer coefficients. (We have suppressed the indices i, j, \dots which take on values x, y, z for spins/polarization directions in configuration space.) All polarization and spin distributions are angular distributions, which depend on the angle of the outgoing particle. Chi-squared per degree of freedom for the analysis is $\chi^2/\text{dof} \simeq 2.7$ over 7,178 data points, 215 of which were discarded by eliminating individual data points which contribute to $\chi^2 > 40$.

Evaluation reproduction

Ideal Script Scenario

Provide compound system to script: *NN, ³H, ³He, ⁴He, ⁵He, ⁵Li, etc.*

➔ `python edaEvaluate --cs 5Li`

• Data

- Retrieve all available data from SG50's (future) relational database URL
 - ⁵Li: ⁴He(p,p)⁴He, ⁴He(p,d)³He, ³He(d,d)³He, ³He(d,p)⁴He, ³He(d,np)³He, ...
 - $\sigma(\theta)$, A_i , P_j , A_{ii} , $C_{i,k}$, $C_{ij,k}$, $K_{i,j'k'}$, $K_{ij,k'l'}$, ...
- Construct internal/native code (EDA) representation (frames for Lab/CM, spectra, etc.)
- [Construct data covariance for GLS]
- [Import sets of detector instrument response functions]

• Evaluation configuration

- Load partition (p+⁴He, d+³He, n+p+³He, etc.) and channel information from input deck
- Load R-matrix parameters
- Load code-run parameters (search method, convergence criteria, etc.)

• Execute evaluation

Evaluation reproduction

Realistic Scenario

- **Data**

- Using “all” data in database is generally not feasible
- ‘Data-cull’ is complex, human-intensive endeavor
 - Consult original literature for meaning, interpretation, accuracy, etc.
 - Cull-out data beyond range of applicability of theory/fit
- Solution: specify details of evaluation data-selection
 - VERY COMPLEX

- **Evaluation configuration**

- Generally straightforward
- Can get complex as code versions change
 - Improved physics models
 - Error/bug corrections, etc.
- Solution: detailed versioning required

- **Evaluation execution & testing**



Thank you.

Follow-on material

NN evaluation: configuration & data

- Neutron energies $E_n \leq 50$ MeV
- Charge-independent analysis

$$R(E) = \sum_{\lambda, T} \frac{\gamma_{\lambda}^{(T)} \tilde{\gamma}_{\lambda}^{(T)}}{E_{\lambda}^{(T)} - E}$$

- T=1 (pp, np-isovector)
- T=0 (np-isoscalar)
- Coulomb energy-level shift

$$E_{\lambda}^{(T=1)} = E^{(T=0)} + \Delta_Z$$

- Fit to $a_{nn} = -18.5$ fm
- Predict nn scattering
- High-fidelity description

$$\chi^2/\text{dof} = 0.9$$

- Planned evaluation
- $E_n \lesssim 250$ MeV

TABLE II. Channel configuration (top) and data summary (bottom) for the charge-independent $N - N$ analysis up to 50 MeV. Since the number of free parameters is 43 resonance parameters + 83 normalizations, the chi-squared per degree of freedom for the analysis is 0.90.

| Channel | a_c (fm) | l_{\max} |
|--------------|------------|------------|
| $p + p$ | 3.26 | 3 |
| $n + p$ | 3.26 | 3 |
| $\gamma + d$ | 84.6 | 1 |
| $n + n$ | 3.26 | 3 |

| Reaction | # Pts. | χ^2 | Observable Types |
|-----------------|--------|----------|--|
| $p(p, p)p$ | 675 | 951 | $\sigma(\theta), A_y(p), C_{x,x'}, C_{y,y'}, K_x^{x'}, K_y^{y'}, K_z^{x'}$ |
| $p(n, n)p$ | 4815 | 3764 | $\sigma_T, \sigma(\theta), A_y(n), C_{y,y'}, K_y^{y'}$ |
| $p(n, \gamma)d$ | 86 | 179 | $\sigma_{\text{int}}, \sigma(\theta), A_y(n)$ |
| $d(\gamma, n)p$ | 88 | 77 | $\sigma_{\text{int}}, \sigma(\theta), \Sigma(\gamma), P_y(n)$ |
| $n(n, n)n$ | 1 | 0 | a_0 |
| Norms. | 80 | 86 | |
| Total: | 5745 | 5057 | 20 |