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# **GNDStk (GNDS Toolkit)**

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# Objectives

## *Create a software toolkit for working with GNDS data*

- **Generic internal format** for GNDS
- **GNDS versions**: support existing and potential future versions of GNDS
- **Read** GNDS files (XML, JSON, etc.)
- **Modify** existing GNDS data
- **Create** new GNDS data
- **Write** GNDS files (XML, JSON, etc.)
- **Convert** between file types
- **Notation**: clean, concise, uncluttered
- **Queries**: search down into data tree
- **Extensible “keyword” scheme**
- **Interoperability** made easy: interface with viz, production codes, other GNDS libraries, etc.
- **Modern C++**
- **Header-only library**
- **Leverage** good existing C++ libraries for XML, JSON etc.
- **Compile-time polymorphism**; *use the C++ type system*
- **Tools**: dictionary, “x-ray” etc.

# Major Classes/Capabilities: Summary

## External Library Wrappers

**class XML**

...Wraps the “pugi XML” library

**class JSON**

...Wraps the “nlohmann JSON” library

*These provide a uniform look and feel across the external libraries.*

## Some Capabilities

Read & write XML GNDS

Read & write JSON GNDS

Build new GNDS trees

Modify existing GNDS trees

Queries: basic and “smart”

Conversions between file types

## GNDS Hierarchy

**class Node<some container types>**

**class node = Node<default>**

**class Tree<some container types>**

**class tree = Tree<default>**

*Individual nodes vs. entire GNDS tree. Similar, but with some differences that reflect each one’s exact purpose.*

## Keyword System

**class meta\_t<type>**

**class child\_t<type, multiplicity>**

*More on these soon.*

# Example GNDS: atom-004\_Be\_000.xml

```
<?xml version="1.0"?>
<PoPs name="ENDF atomic relaxation for Z = 5" version="1.0" format="0.1">
  <styles>
    <evaluated label="eval" date="2017-12-01" library="ENDF/B"
      version="8.0.0"/>
  </styles>
  <documentations>
    <documentation name="endfDoc"><![CDATA[
5-B - 0 NDS,IAEA Eval-Dec17 D.E.Cullen
NDS-IAEA-224 DIST-FEB18
----ENDF/B-VIII.0 MATERIAL 100
----ATOMIC RELAXATION DATA
-----ENDF-6 FORMAT
*** SOME CONTENT DELETED HERE, FOR BREVITY ***
=====
The Livermore Evaluated Atomic Data Library (EADL) in the
ENDF-6 Format. Translated from the Livermore ENDL format
to the ENDF-6 Format.
=====
Contents
=====
MF/MT Description
=====
28/533 Atomic Relaxation Data for Electrons and Photons
=====
Definition of Data
=====
Atomic Relaxation Data for Electrons and Photons
=====
1) An atom can be ionized by a photon or an electron interaction.
2) The atomic relaxation data included here describes how a
singly ionized atom returns to neutrality, by emitting photons
(x-rays) and/or electrons (Auger, Coster-Kronig).
3) Data is given to define the transition probabilities between
subshells for radiative (x-ray emission) and non-radiative
(Auger, Coster-Kronig) transitions.
4) The complete spectrum of emitted photons and electrons can be
calculated using the data included here, e.g., see ref. 2,
below, for an example of a computer code that analytically
calculates these spectra.
=====
History
```

```
=====
(1) November, 1991 - Initial release in the ENDL format.
(2) November, 2001 - Initial release in the ENDF-6 format.
(3) September, 2014 - Insure Standard C, C++, FORTRAN Format
(4) September, 2014 - Updated based on recently published data
(5) September, 2017 - New Binding Energies (see: ref.3)
Same Transition Probabilities
=====
***** Program DICTIN (VERSION 2017-1) *****]]>
  </documentation>
</documentations>
<chemicalElements>
  <chemicalElement symbol="B" Z="5" name="Boron">
    <atomic>
      <configurations>
        <configuration subshell="1s1/2" electronNumber="2.0">
          <bindingEnergy>
            <double label="eval" value="192.0" unit="eV"/>
          </bindingEnergy>
        </configuration>
        <configuration subshell="2s1/2" electronNumber="2.0">
          <bindingEnergy>
            <double label="eval" value="11.39" unit="eV"/>
          </bindingEnergy>
        </configuration>
        <configuration subshell="2p1/2" electronNumber="0.33">
          <bindingEnergy>
            <double label="eval" value="8.3" unit="eV"/>
          </bindingEnergy>
        </configuration>
        <configuration subshell="2p3/2" electronNumber="0.67">
          <bindingEnergy>
            <double label="eval" value="8.3" unit="eV"/>
          </bindingEnergy>
        </configuration>
      </configurations>
    </atomic>
  </chemicalElement>
</chemicalElements>
</PoPs>
```

# Examples 1, 2, 3

## Example 1

```
#include "GNDStk.hpp"
```

```
int main()  
{  
}
```

## Example 2

```
#include "GNDStk.hpp"
```

```
// For brevity  
using namespace GNDStk;
```

```
int main()  
{  
    tree t("atom-005_B_000.xml");  
}
```

## Example 3

```
#include "GNDStk.hpp"
```

```
// For brevity  
// May eventually be njoy::GNDStk  
using namespace GNDStk;
```

```
int main()  
{  
    tree t("atom-005_B_000.xml");  
  
    // Another way (there are several)  
    {  
        tree t;  
        t.read("atom-005_B_000.xml");  
    }  
  
    // Write as JSON  
    t.write("atom-005_B_000.json");  
}
```

# Example 4

```
#include "GNDStk.hpp"
using namespace GNDStk;

int main()
{
    // Read from xml
    tree x("atom-005_B_000.xml");

    // Write to json
    x.write("atom-005_B_000.json");

    // Read back from json
    tree j("atom-005_B_000.json");

    // Both of the trees should have the
    // same content. Let's verify this...

    // However, GNDS has no "ordering", and
    // content may read or write differently
    // in XML as compared with JSON. So, we
    // provide sort() as a convenience.
    x.sort();
    j.sort();

    // Stream output (<<) writes the tree
    // in our internal "debugging" format
    std::ostringstream ossx;
    ossx << x;
    std::ostringstream ossj;
    ossj << j;

    // Compare
    assert(ossx.str() == ossj.str());
}
```

# Example 5

**Raw data access. It's available, but beware of [] indexing! Remember, GNDS data have no guaranteed ordering.**

```
#include "GNDStk.hpp"
using namespace GNDStk;

int main()
{
    tree t("atom-005_B_000.xml");
    node n = t.top(); // top-level GNDS node
    // A node has:
    //   string name
    //   vector<pair of strings> metadata
    //   vector<pointers to nodes> children

    // name
    assert(n.name == "PoPs");

    // metadata: name, version, format
    assert(n.metadata.size() == 3);
    assert(n.metadata[0].first ==
           "name");
    assert(n.metadata[0].second ==
           "ENDF atomic relaxation for Z = 5");
    assert(n.metadata[1].first ==
           "version");
    assert(n.metadata[1].second ==
           "1.0");
    assert(n.metadata[2].first ==
           "format");
    assert(n.metadata[2].second ==
           "0.1");

    // child nodes: <styles>,
    // <documentations>, <chemicalElements>
    assert(n.children.size() == 3);
    assert(n.children[0]->name ==
           "styles");
    assert(n.children[1]->name ==
           "documentations");
    assert(n.children[2]->name ==
           "chemicalElements");

    // Let's improve on the raw access!
}
```

# Example 6

**Data access via string lookup.** For `metadata`, use `meta()`. Same-named `child nodes` can appear more than once. Use `one()` for one, `all()` for all.

```
#include "GNDStk.hpp"
using namespace GNDStk;

int main()
{
    tree t("atom-005_B_000.xml");

    // Child's metadatum
    assert(t.one("PoPs")
           .meta("version") == "1.0");

    // Child's child
    assert(t.one("PoPs")
           .one("styles")
           .metadata.size() == 0);

    // Child's child's child
    assert(t.one("PoPs")
           .one("styles")
           .one("evaluated")
           .metadata.size() == 4);

    // Child's child's child's metadatum
    assert(t.one("PoPs")
           .one("styles")
           .one("evaluated")
           .meta("date") == "2017-12-01");

    // From child() and meta(), we get back,
    // respectively, node and string. So:
    node &n = t.one("PoPs").one("styles");
    assert(n.one("evaluated")
           .meta("date") == "2017-12-01");

    node &eval = n.one("evaluated");
    std::string datestr = eval.meta("date");
    assert(datestr == "2017-12-01");

    // This is preferable over raw access,
    // but let's try to make it even better!
}
```

# Data Query Improvements

Recall the first few lines of our example XML file:

```
<?xml version="1.0"?>
<PoPs name="ENDF atomic relaxation for Z = 5" version="1.0" format="0.1">
  <styles>
    <evaluated label="eval" date="2017-12-01" library="ENDF/B" version="8.0.0"/>
  </styles>
  ...
```

And, consider this data query, on a `GNDStk::tree` object called `tree`, as illustrated in our previous example:

```
tree.one("PoPs").one("styles").one("evaluated").meta("date")
```

The above query gives us the string "2017-12-01".

**Question: How can we improve this?**

# Improvement #1: Predefined Strings

This one is **super simple**, but useful. We can provide **predefined strings**, like these, for the **names** of all possible GNDS metadata and child nodes:

```
const std::string PoPs      = "PoPs";  
const std::string styles   = "styles";  
const std::string evaluated = "evaluated";  
const std::string date     = "date";
```

These allow us to take our previous query,

```
tree.one("PoPs").one("styles").one("evaluated").meta("date")
```

and replace it with:

```
tree.one(PoPs).one(styles).one(evaluated).meta(date)
```

**That's hardly earth shattering, but it's useful...**

You **save four keystrokes** (shift quote ... shift quote) per name.

A **typo** (evalauted) **presents at compile time**, not at run time ("evalauted").

We can **provide all valid GNDS names**, so it's harder to use one that isn't valid.

# Improvement #2: Metadata vs. Children

Let's take the "predefined strings" concept further. Consider two simple classes, which we'll call **meta\_t** (metadatum type) and **child\_t** (child node type). Briefly:

```
struct meta_t {          struct child_t {
    std::string name;    std::string name;
    // and a constructor // and a constructor
};                       };
```

Now consider some simple C++ **function overloading**. We'll make two functions, both called `f()`. The first takes a **meta\_t**, while the second takes a **child\_t**.

```
string &f(const meta_t &arg) { /* calls .meta(arg.name) */ }
node   &f(const child_t &arg) { /* calls .one (arg.name) */ }

const meta_t foo("foo");
f(foo); // ultimately, this calls meta("foo")

const child_t bar("bar");
f(bar); // ultimately, this calls one("bar")
```

Essentially, we've embedded our strings into types that control where they're sent.

# Improvement #2 (continued)

GNDStk's `meta_t` and `child_t` classes are a bit more complicated than that, but, for now, imagine that we'll provide predefined ones like these:

```
const meta_t date      = "date";  
const child_t PoPs    = "PoPs";  
const child_t styles  = "styles";  
const child_t evaluated = "evaluated";
```

These allow us to take our previous query,

```
tree.one(PoPs).one(styles).one(evaluated).meta(date)
```

and replace it with:

```
tree(PoPs)(styles)(evaluated)(date)
```

**Well, that's a nice improvement.** You no longer need to write `.one` and `.meta` all over the place. Those still work, but our overloaded parentheses operator, `()`, accepts either a `meta_t` or a `child_t`, and knows how to handle each of them properly.

# Improvement #3: One Call

Now that we've **disappeared the .one and .meta clutter**, leaving just a series of calls to (), we'll **also allow for a single call with comma-separated arguments**.

Before, we had this:

```
tree(PoPs)(styles)(evaluated)(date)
```

but now we can write:

```
tree(PoPs, styles, evaluated, date)
```

**Not a major improvement, but slightly shorter and easier to type.**

In general, you can provide any number (possibly zero) of **child\_t** objects, and end the sequence with either a **meta\_t** object or a **child\_t** object:

```
tree ( [child_t, child_t, ... ,] meta_t )  
tree ( [child_t, child_t, ... ,] child_t )
```

Expect – *for now* – a **string** from the first, and a **node** from the second.

# Improvement #4: Custom Types

The improvements we've shown so far constitute part of what we call our “**smart keyword**” system. (“**Keywords**” here really just means variables of our **meta\_t** and **child\_t** types.) Names of allowable GNDS metadata and child nodes are encapsulated into **meta\_t** and **child\_t** objects, then combined with a flexible parentheses operator ( . . . ) to allow *succinct, intuitive node and tree queries*. **Now, perhaps, the most fun part.**

Let's again revisit our example GNDS file:

```
<?xml version="1.0"?>
<PoPs name="ENDF atomic relaxation for Z = 5" version="1.0" format="0.1">
  <styles>
    <evaluated label="eval" date="2017-12-01" library="ENDF/B" version="8.0.0"/>
  </styles>
  ...
```

Consider **date="2017-12-01"**. It'll serve as a simple example of **fitting a custom metadata structure into our existing query system**.

**We'll illustrate with a complete example.**

# Improvement #4 (continued)

```
#include "GNDStk.hpp"
using namespace GNDStk;

// Define a simple type to hold a date
struct date_t {
    int year, month, day;
};

// Define stream input for date_t. (There
// are alternatives, if you don't want to
// have operator>>, or if it already exists
// and does something else.)
std::istream &operator>>(
    std::istream &s, date_t &d
) {
    char ch; // for '-' in "yyyy-mm-dd"
    return s >> d.year >> ch >> d.month
        >> ch >> d.day;
}

// Now make a GNDStk::meta_t object, here
// called date, in the following way.
meta_t<date_t> date("date");

int main()
{
    tree t("atom-005_B_000.xml");

    // GNDStk provides built-in child_t
    // objects in its child:: namespace.
    // We'll use these below.

    // Now, use GNDStk's query system, along
    // with your own "date" object, to get
    // the date as a date_t object.
    date_t d = t(
        child::PoPs, // from GNDStk
        child::styles, // from GNDStk
        child::evaluated, // from GNDStk
        date // <== our own
    );

    // We got a date_t, not a string, so:
    assert(d.year == 2017);
    assert(d.month == 12);
    assert(d.day == 1);
}
```

# Improvements (so far)

In summary, we've taken the original long-winded query into our tree, whittled it down into something **much shorter**, and then provided a way to get a **custom type** instead of the string that's in the original GNDS.

Original:

```
tree.one("PoPs").one("styles").one("evaluated").meta("date")
```

With predefined strings:

```
tree.one(PoPs).one(styles).one(evaluated).meta(date)
```

With overloading via **meta\_t** and **child\_t** types:

```
tree(PoPs)(styles)(evaluated)(date)
```

One call with comma-separated values:

```
tree(PoPs, styles, evaluated, date) // <== return is string
```

**And then finally:**

```
tree(PoPs, styles, evaluated, date) // <== return is our custom date_t type
```

**if** the parameter **date** is formulated as an object of type **meta\_t<date\_t>**.

# Improvement #5

For metadata retrieval, we've seen how anyone can **define a custom type T**, **create an object of type meta\_t<T>**, and **use the object seamlessly**, in GNDStk's query system, to **extract a metadata value as an object of type T**.

## What about extracting child nodes?

For this we can similarly create objects, now of type **child\_t<T>**, to extract child nodes into a custom type T.

However, `child_t<>` also takes a second argument, with two possible values:

```
child_t< T, find::one >  
child_t< T, find::all >
```

**find::one** tells GNDStk to look for **one such child node**, and return it as a T.

**find::all** tells GNDStk to look for **all such child nodes**, and return them in a `vector<T>`. (We do allow for containers other than vector, but the notation for that is a bit cumbersome right now. GNDStk is a work in progress.)

# Improvement #5 (continued)

Consider part of our example XML:

```
<?xml version="1.0"?>
<PoPs name="ENDF atomic relaxation for Z = 5" version="1.0" format="0.1">
  ...
  <chemicalElements>
    <chemicalElement symbol="B" Z="5" name="Boron">
      <atomic>
        <configurations>
          <configuration subshell="1s1/2" electronNumber="2.0">
            <bindingEnergy>
              <double label="eval" value="192.0" unit="eV"/>
            </bindingEnergy>
          </configuration>
          <configuration subshell="2s1/2" electronNumber="2.0">
            <bindingEnergy>
              <double label="eval" value="11.39" unit="eV"/>
            </bindingEnergy>
          </configuration>
          <configuration subshell="2p1/2" electronNumber="0.33">
            <bindingEnergy>
              <double label="eval" value="8.3" unit="eV"/>
            </bindingEnergy>
          </configuration>
          <configuration subshell="2p3/2" electronNumber="0.67">
            <bindingEnergy>
              <double label="eval" value="8.3" unit="eV"/>
            </bindingEnergy>
          </configuration>
        </configurations>
      </atomic>
    </chemicalElement>
  </chemicalElements>
</PoPs>
```

There's **just one bindingEnergy** in any given context, so we might have:

```
struct bindingEnergy_type { ... };

child_t<bindingEnergy_type, find::one>
  binden("bindingEnergy");
```

There are **many configuration nodes** in one place, however, so we might have:

```
struct configuration_type { ... };

child_t<configuration_type, find::all>
  config("configuration");
```

**Each type** that's embedded in a `child_t` will also need a **certain conversion function** from a tree node.

# Example

```
#include "GNDStk.hpp"
using namespace GNDStk;

// For accessing one "bindingEnergy"
struct bindingEnergy_type { };
void node2type(
    const node &, bindingEnergy_type &
) { }
child_t<bindingEnergy_type, find::one>
binden("bindingEnergy");

// For accessing all "configuration"s
struct configuration_type { };
void node2type(
    const node &, configuration_type &
) { }
child_t<configuration_type, find::all>
config("configuration");

int main()
{
    tree gnds("atom-005_B_000.xml");

    // GNDStk's child::chemicalElement
    // and our configuration_type are
```

```
// both encoded with find::all, so
// their use gives us vector<>s...
auto c = gnds(
    child::PoPs,
    child::chemicalElements,
    child::chemicalElement
)[0](
    child::atomic,
    child::configurations,
    config // set up above
);
// c is vector<configuration_type>
assert(c.size() == 4);

// configuration_type as defined
// earlier is a stub, so we can't do
// much with it here. In a complete
// example, it would probably contain
// values for its metadata, and a
// bindingEnergy_type object (also
// remade as more than a stub) for
// its <bindingEnergy> child node.
}
```

# Classes/Capabilities: Sketch

Let's sketch some of GNDStk's capabilities in terms of its major classes:

- **XML**
- **JSON**
- **Node<>**
- **Tree<>**

Information on the following pages is by no means complete.

In particular, I'll omit some of the more-obscure functionality in some of the above classes, and some of the extra niceties you can get from some of their functions, e.g. by sending optional parameters.

Note: the template parameters on **Node** and **Tree** allow you to specify **container types** for metadata and for child nodes. We won't worry about these for now.

# XML Class

```
struct XML {  
    // external XML-library document  
    pugi::xml_document doc;  
  
    // clear  
    void clear();  
  
    // constructors  
    XML() = default;  
    XML(XML &&) = default;  
    XML(const XML &x);  
    explicit XML(const JSON &j);  
    explicit XML(const Tree<> &t);  
    explicit XML(const std::string &file);  
    explicit XML(std::istream &is);  
  
    // assignment  
    XML &operator=(XML &&) = default;  
    XML &operator=(const XML &x);  
  
    // read  
    std::istream &read(std::istream &is);  
    bool read(const std::string &file);  
  
    // write  
    std::ostream &write(std::ostream &os) const;  
    bool write(const std::string &file) const;  
  
}; // struct XML  
  
// stream input  
std::istream &operator>>  
    (std::istream &is, XML &obj);  
  
// stream output  
std::ostream &operator<<  
    (std::ostream &os, const XML &obj);
```

# JSON Class

```
struct JSON {  
    // external JSON-library document  
    nlohmann::json doc;  
  
    // clear  
    void clear();  
  
    // constructors  
    JSON() = default;  
    JSON(JSON &&) = default;  
    JSON(const JSON &j);  
    explicit JSON(const XML &x);  
    explicit JSON(const Tree<> &t);  
    explicit JSON(const std::string &file);  
    explicit JSON(std::istream &is);  
  
    // assignment  
    JSON &operator=(JSON &&) = default;  
    JSON &operator=(const JSON &) = default;  
  
    // read  
    std::istream &read(std::istream &is);  
    bool read(const std::string &file);  
  
    // write  
    std::ostream &write(std::ostream &os) const;  
    bool write(const std::string &file) const;  
  
}; // struct JSON  
  
// stream input  
std::istream &operator>>  
    (std::istream &is, JSON &obj);  
  
// stream output  
std::ostream &operator<<  
    (std::ostream &os, const JSON &obj);
```

# Node Class

```
// <METADATA_CONTAINER,CHILDREN_CONTAINER>
struct Node {
    using metaPair = pair<string,string>;
    using childPtr = unique_ptr<Node>;
    string name;
    METADATA_CONTAINER<metaPair> metadata;
    CHILDREN_CONTAINER<childPtr> children;

    // clear()
    Node &clear();

    // empty()
    bool empty() const;

    // constructors
    Node() { }
    Node(Node &&) = default;
    Node(const Node &from);

    // assignment
    Node &operator=(Node &&) = default;
    Node &operator=(const Node &from);

    // add()
    // Add metadatum/child; many variations

    // meta()
    // Access metadatum

    // one()
    // Access once-appearing child node

    // all()
    // Access many child nodes ==> container

    // child()
    // Access child nodes by using smart
    // keywords. find::one gets one, find::all
    // gets a container of zero or more

    // operator()
    // Access metadatum/child; many variations

    // sort()
    // Orders node's content in a predictable
    // way, for whatever that may help with
    Node &sort();
}; // struct Node
```

# Tree Class, Part 1

```
// <METADATA_CONTAINER,CHILDREN_CONTAINER>
struct Tree {

    // Initial node of the tree
    using nodeType = Node<METADATA_CONTAINER,CHILDREN_CONTAINER>;
    std::unique_ptr<nodeType> root;

    // clear()
    void clear();

    // empty()
    bool empty() const;

    // reset()
    // Re-start a tree, with a particular top-level GNDS node and optionally
    // some XML boilerplate if you plan to write as XML. A couple of variations.

    // constructors
    Tree() = default;
    Tree(Tree &&) = default;
    Tree(const Tree &from);
    explicit Tree(const Tree<different> &from);
    explicit Tree(const XML &x);
    explicit Tree(const JSON &j);
    explicit Tree(const std::string &file, const format form = format::null);
```

# Tree Class, Part 2

```
Tree(const std::string &file, const std::string &type);
explicit Tree(std::istream &is, const format form = format::null);
Tree(std::istream &is, const std::string &type);
// ...and a couple of additional ctors that are more complicated

// assignment
Tree &operator=(Tree &&) = default;
Tree &operator=(const Tree &t);
Tree &operator=(const Tree<different> &t);

// read
bool read(const std::string &file, const format form = format::null);
std::istream &read(std::istream &is, const format form = format::null);
bool read(const std::string &file, const std::string &form);
std::istream &read(std::istream &is, const std::string &form);

// write
bool write(const std::string &file, const format form = format::null) const;
std::ostream &write(std::ostream &os, const format form = format::null) const;
bool write(const std::string &file, const std::string &form) const;
std::ostream &write(std::ostream &os, const std::string &form) const;
```

# Tree Class, Part 3

```
// decl()
// Access "declaration node" if applicable
const nodeType &decl() const;
nodeType &decl();

// top()
// Access top-level GNDS node (reactionSuite, PoPs, ...)
const nodeType &top() const;
nodeType &top();

// Similar to those for node...
// meta()
// one()
// all()
// child()
// operator()
// sort()

}; // struct Tree

// I/O
std::istream &operator>>(std::istream &is, Tree<> &obj);
std::ostream &operator<<(std::ostream &os, const Tree<> &obj);
```