

METHODS AND APPROACHES DEVELOPMENT AT ORNL FOR PROVIDING FEEDBACK FROM INTEGRAL BENCHMARK EXPERIMENTS FOR IMPROVEMENT OF NUCLEAR DATA FILES

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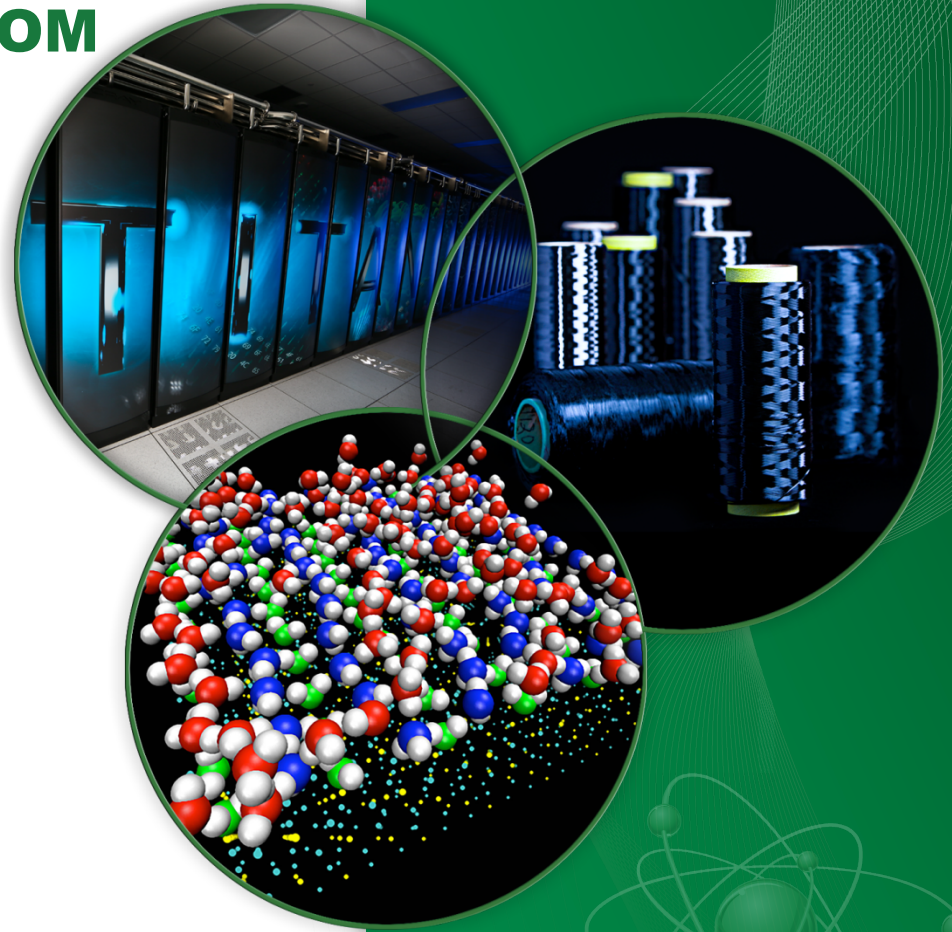


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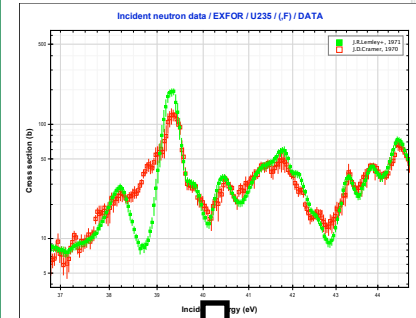


SAMINT: A Code for Nuclear Data Adjustment with SAMMY Based on Integral Experiments

- Allow coupling of differential and integral data evaluation in a continuous-energy framework
- Update the resonance parameter evaluation directly based on integral benchmark experiments

Integral Experiments to Aid Nuclear Data Evaluation

- SAMINT can be used to extract information from integral benchmarks to aid the nuclear data evaluation process.
- Near the end of the evaluation based on differential experimental data, integral data can be used to:
 - Resolve remaining ambiguity between differential data sets
 - Guide the evaluator to troublesome energy regions
 - Inform the evaluator of the most important nuclear data parameters to integral benchmark calculations
 - Improve the nuclear data covariance matrix evaluation



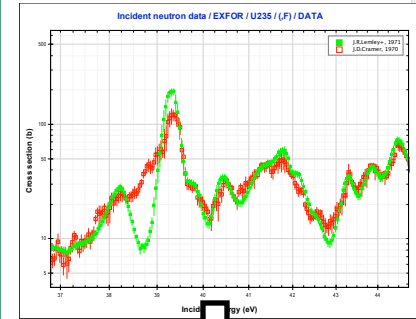
SAMMY



ENDF

SAMINT Proper Uses

- SAMINT is **not intended** to bias the nuclear data towards fitting a certain set of integral experiments
- SAMINT should be used to **supplement** evaluation of differential experimental data
- Using the GLLS methodology ensures that the updated nuclear data parameters respect the original fit of the differential data



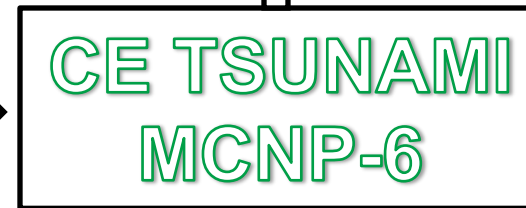
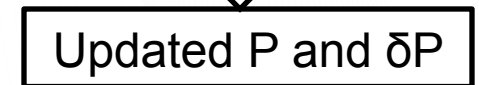
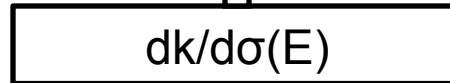
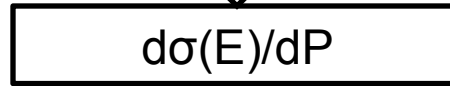
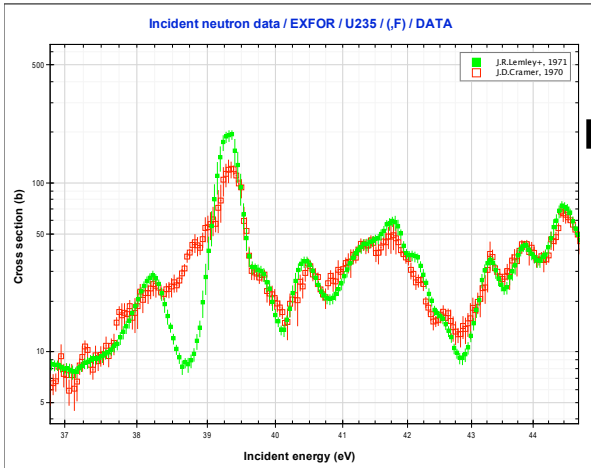
SAMMY



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Using SAMINT with SAMMY

Differential Experimental Data



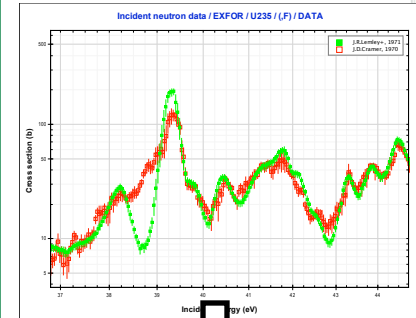
P stands for all resonance parameters: E_λ , Γ_γ , Γ_n , Γ_f , etc.

Integral Experimental Data



SAMINT Capabilities for Initial Release from RSICC

- Current Capabilities
 - Adjusting resolved resonance parameters and associated covariance
 - Adjusting number of prompt neutrons per fission
 - Calculating continuous energy cross sections and eta values (reactor physics) to satisfy integral benchmarks
 - Works with both CE TSUNAMI and MCNP-6 k-eigenvalue sensitivities
 - Iteration for non-linearity



SAMMY



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SAMINT Release Through RSICC

- SAMINT will be distributed with the SAMMY code from RSICC!
<https://rsicc.ornl.gov/>
- Optional compile-time inclusion
- LAPACK/BLAS for all linear algebra operations
- Mac, Linux, Windows
- Version control
- Automated test cases

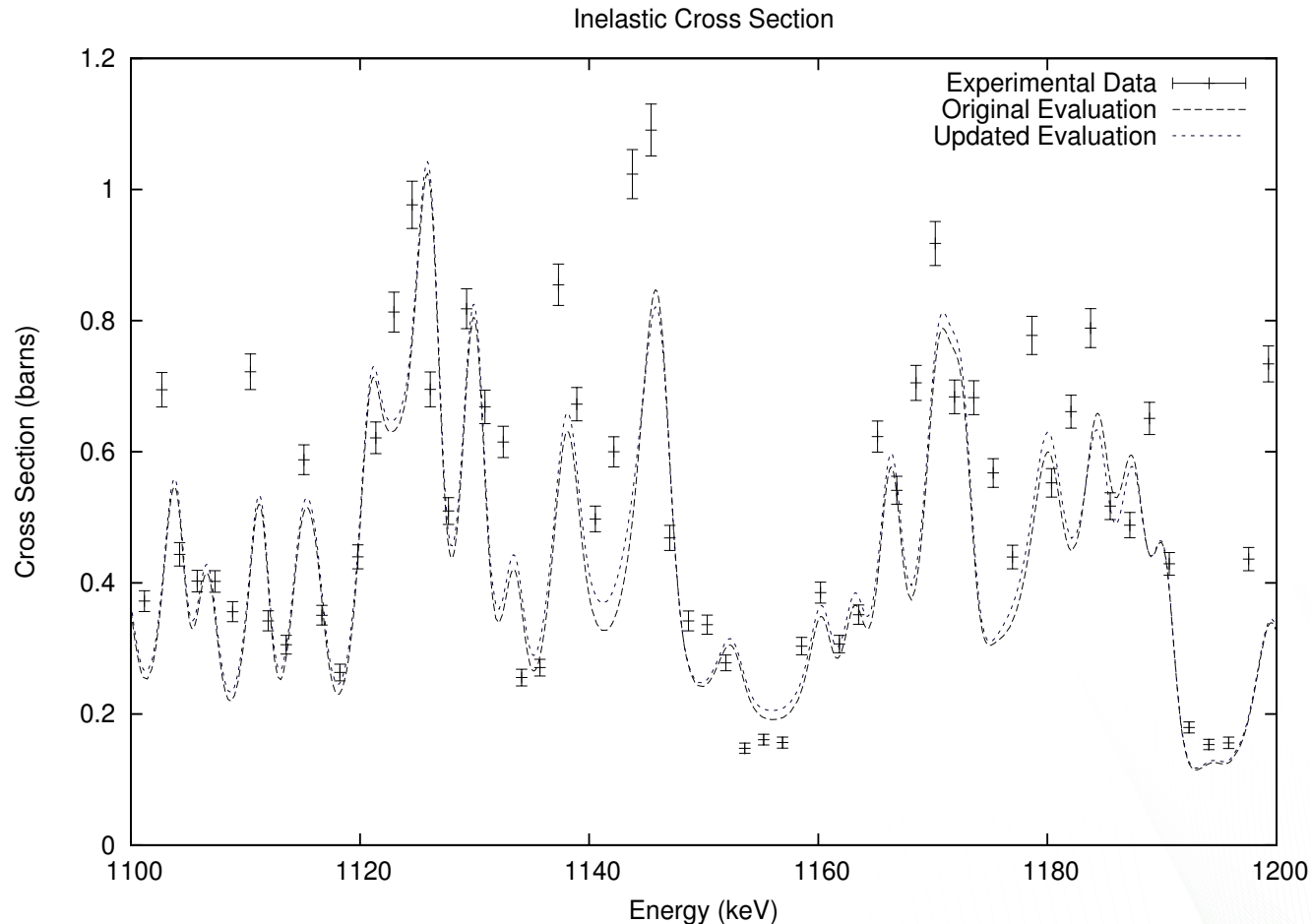
Case Name	SAMINT Capability	Sensitivity Code	Notes
tr181	<ul style="list-style-type: none">- Resonance Parameter updating- Eta updating with correlations- Eta updating without correlations- Integral experiment covariance matrix	CE TSUNAMI-3D	Independently confirmed by MATLAB calculations
tr182	<ul style="list-style-type: none">- ^{56}Fe case- Fitting resonance parameters with inelastic channel open	MCNP6	Complication comes from appearance of zero cross-sections due to threshold reactions
tr183	<ul style="list-style-type: none">- ^{239}Pu case- Fitting resonance parameter and nu-bar simultaneously- Independent eta updating	MCNP6	

Sample Calculations

- As a demonstration calculation, SAMINT was used to adjust the resolved resonance region evaluation of ^{56}Fe .
- Four integral experiments from the ICSBEP were selected.
- Energy region of evaluation: 1e-5 eV to 2 MeV.
- 1190 resonance parameters varied:
 - Γ_{γ} : 450 keV – 2MeV
 - $\Gamma_{(n,n'),1}$ and $\Gamma_{(n,n'),2}$: 846 keV – 2MeV

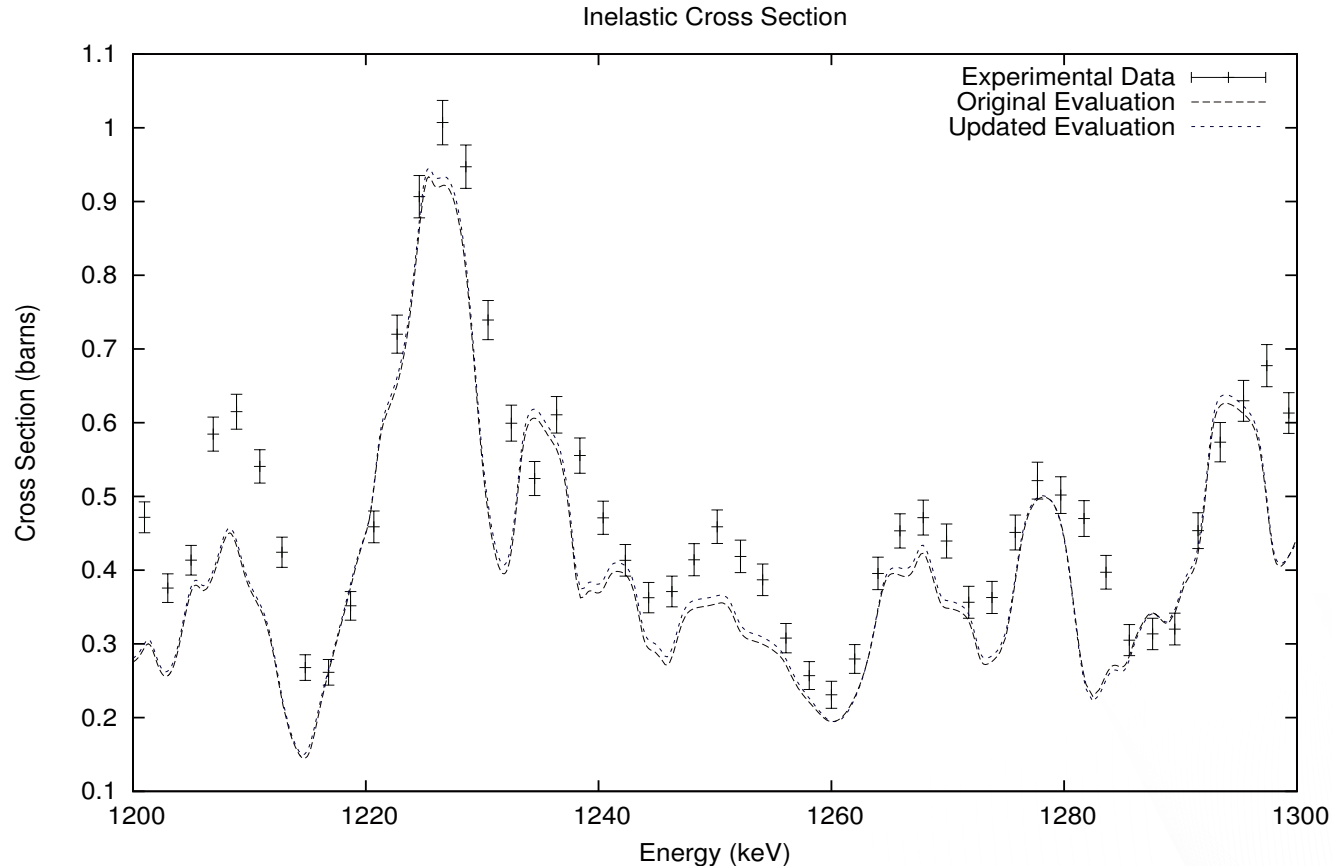


Cross Section Changes: Finer Scale than Differential Experimental Data



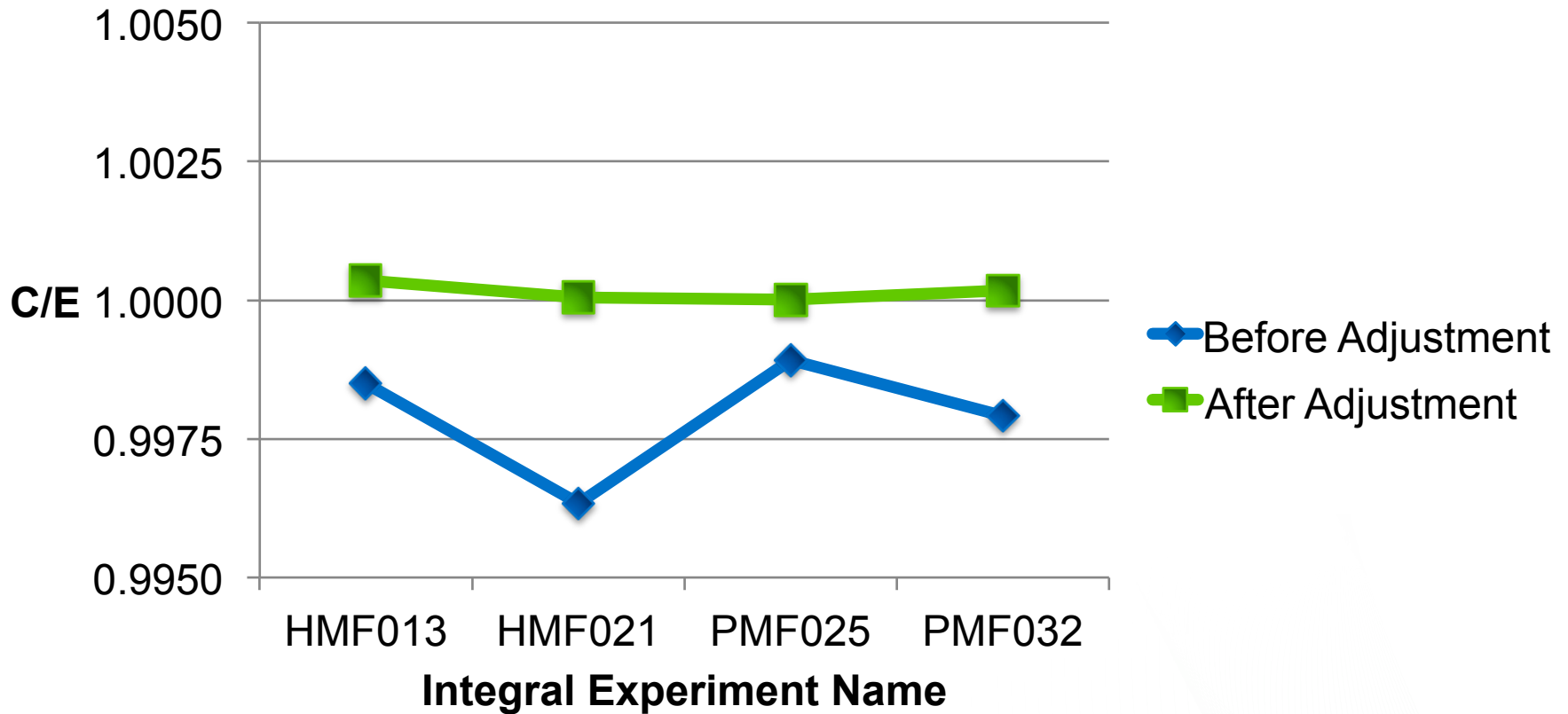
Inelastic cross section of ^{56}Fe before ($\chi^2 = 73.3382$) and after ($\chi^2 = 73.6877$) the adjustment based on integral experimental data plotted on top of differential experimental data of Plompen, presented with one standard deviation error bars.

Cross Section Changes: Finer Scale than Differential Experimental Data



Inelastic cross section of ^{56}Fe before ($\chi^2 = 23.6023$) and after ($\chi^2 = 22.9036$) the adjustment based on integral experimental data plotted on top of differential experimental data of Perey, presented with one standard deviation error bars.

⁵⁶Fe Results



- **C/E:** $\frac{\text{Computed Value}}{\text{Experimentally Measured Value}}$

Expanded Capabilities

First Update Release (Spring)

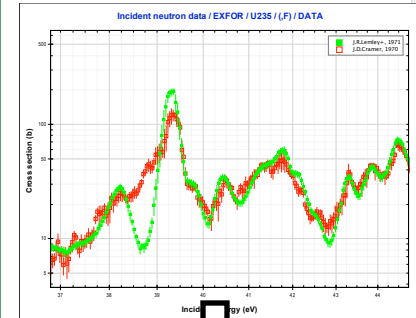
- Cross-Isotope correlation matrices
 - Determine the posterior correlation matrix created by adjusting several isotopes simultaneously
- Use of Angular Distribution Sensitivity with MCNP6 for adjusting resonance parameters
- Immediate application:
 ^{63}Cu and ^{65}Cu

In FY2016

- Extension to Unresolved Resonance Region
- Support of Generalized Sensitivity Capabilities of CE TSUNAMI-3D

Summary

- SAMINT should be used to **supplement** evaluation of differential experimental data.
- SAMINT will also improve the nuclear data covariance matrix evaluation.
- Plans to extend the SAMINT methodology to the unresolved resonance region and the high energy region.
- Support for this work was provided by the US DOE Nuclear Criticality Safety Program.



SAMMY



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INSURE: INverse Sensitivity/UnceRtainty Estimator

- Determine target accuracies of nuclear data needed to model applications within prescribed tolerances
- Minimize the cost of acquiring improved data that would yield acceptable uncertainties of responses

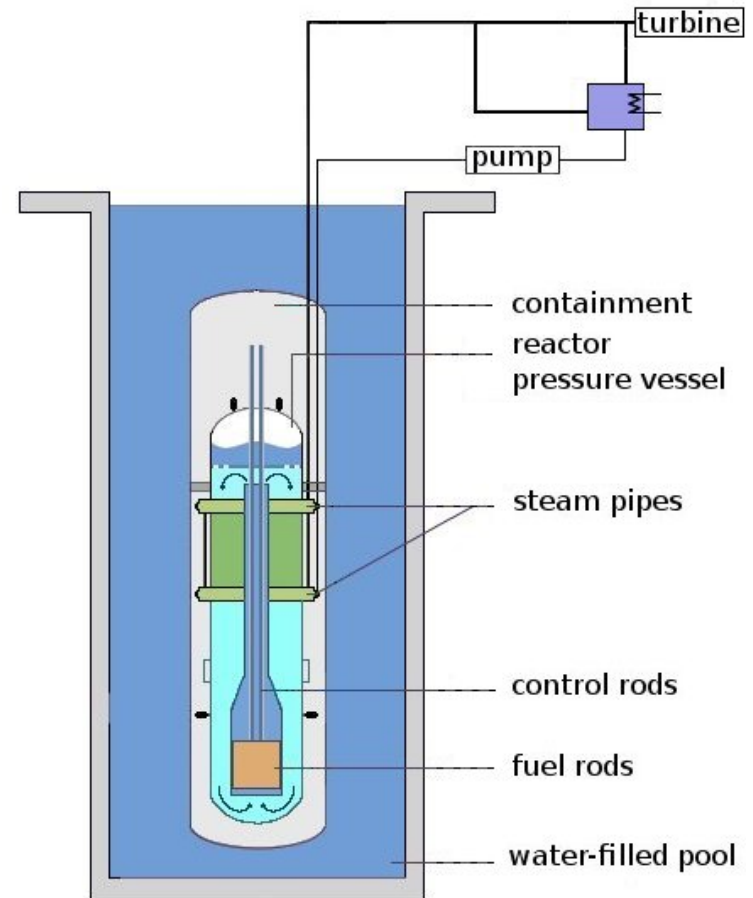
Applications

Application Examples:

- Light Water Reactors
- Fast neutron reactors
- Spent Nuclear Fuel
 - Reprocessing
 - Transport
 - Disposal

Response Examples

- Neutron multiplication factor
- Cycle length
- Power distribution
- Reaction rate ratio



Inverse S/U: Definitions

- A nuclear application design specifies maximum allowed uncertainties on performance parameters (“responses”)
 - e.g. the multiplicity factor and its tolerance

$$R \pm \Delta R$$

- Neutron transport using existing cross section uncertainties often leads to an application response uncertainty *greater* than the maximum allowed, i.e.:

$$\sigma_0 \pm \Delta\sigma_0 \Rightarrow R_0 \pm \Delta R_0 \quad \text{where } \Delta R_0 > \Delta R$$

- Inverse S/U: What set of improved data would lower the response uncertainty below the specified tolerance?
 - While minimizing the cost of data measurements

$$\sigma' \pm \Delta\sigma' \Rightarrow R' \pm \Delta R' \leq \Delta R \quad \text{for } \min(\text{cost}[\Delta\sigma'])$$

Inverse S/U Math

- Given a desired responses \pm tolerances: $R \pm \Delta R$
- And the existing data \pm uncertainties: $\sigma_0 \pm \Delta \sigma_0$
- Minimize the *cost* of acquiring improved data uncertainties that yield a response uncertainty within tolerance:

$\min \{ \text{Cost}[\Delta \sigma] \}$ such that

$$S(\Delta \sigma)^2 S^T \leq (\Delta R)^2$$

$$S = \left. \frac{\delta R(x)}{\delta \sigma} \right|_{\sigma = \sigma_0}$$

- This is a constrained optimization problem:
 - MINCON: open source subroutine is used by MATLAB and DAKOTA

Including Integral Benchmark Experiments in IS/U

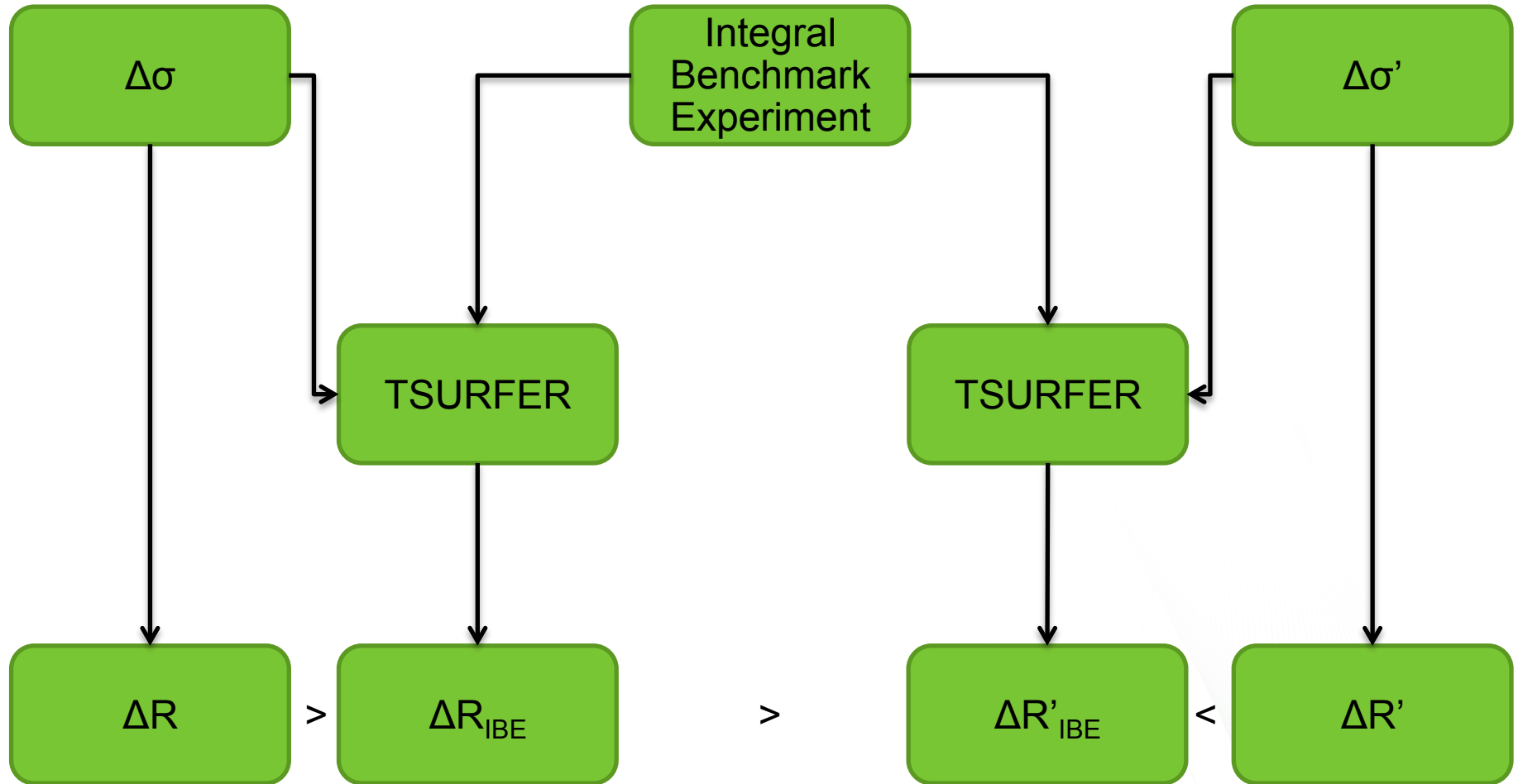
- Differential data uncertainties are limited by experimental methods
- Some data already at the present-day limits of experimental precision
- Uncertainties required by IS/U lower than these may be unrealistic

Table II. Uncertainties of the present-day state-of-the-art measurements for various cross sections

<i>Reaction</i>	<i>MT</i>	<i>Min. Rel. Uncertainty</i>
Fission	18	0.7%
Capture	102	2%
Neutron yields	452	0.3%
Elastic scattering	2	2%

- IS/U results obtained with integral benchmark experiments afford larger differential data uncertainties, i.e.: lower cost of differential data

Including Integral Benchmark Experiments in IS/U



Example Calculations

- For PWR fuel array:
 - for extant data $dk_{\text{eff}} = 0.0031$
 - we desire $dk_{\text{eff}} = 0.0010$, $\text{var}(k_{\text{eff}}) = 10^{-6}$

TABLE I. SUMMARY OF INVERSE S/U RESULTS

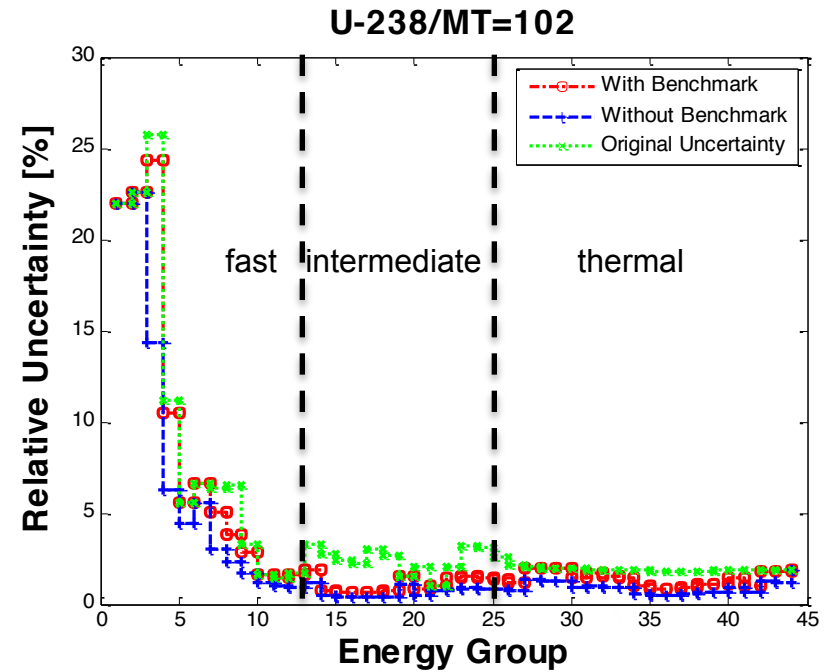
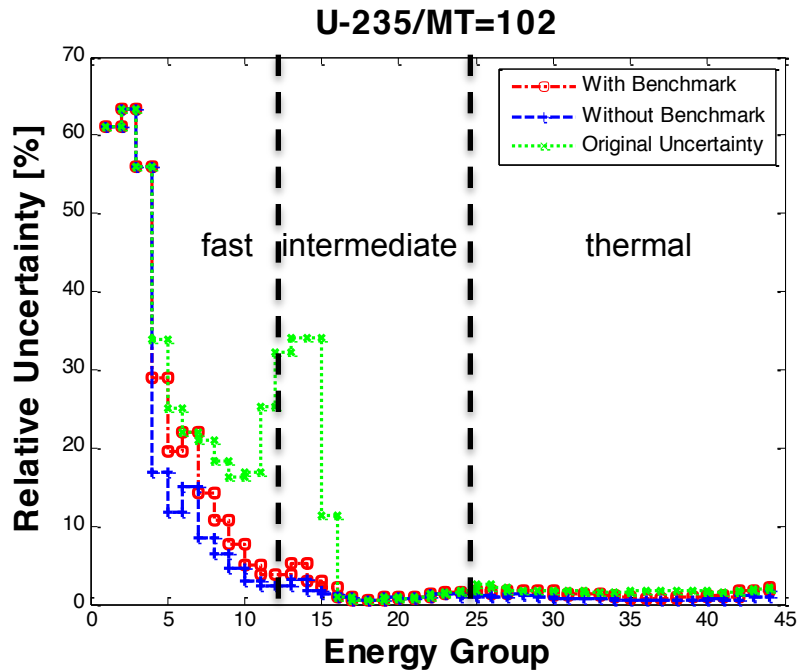
	<i>w/o Benchmark</i>	<i>w/Benchmark</i>
Cost (arb.)	53.3	8.6
$\text{var}(k_{\text{eff}})$	1.0E-06	1.0E-06

- An overall 6-fold decrease in data cost was achieved by including integral benchmarks in the Inverse S/U calculations
- The integral benchmark experiment used in this work is water-moderated UO_2 fuel rods in 2.032-cm square-pitched arrays (LEU-COMP-THERM-001). This experiment was chosen because of its similarity to the PWR fuel-rods.

Cost Function

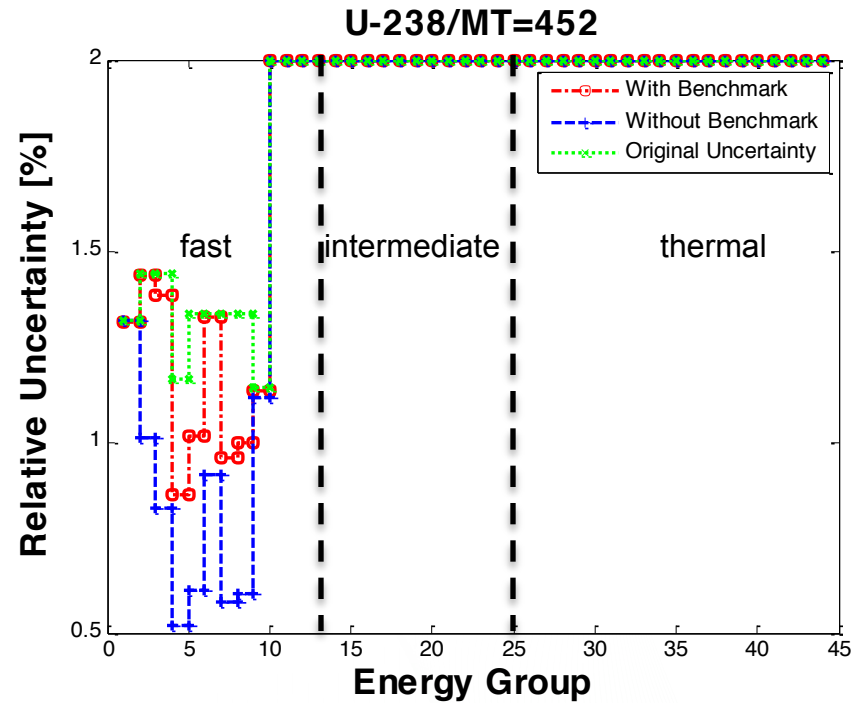
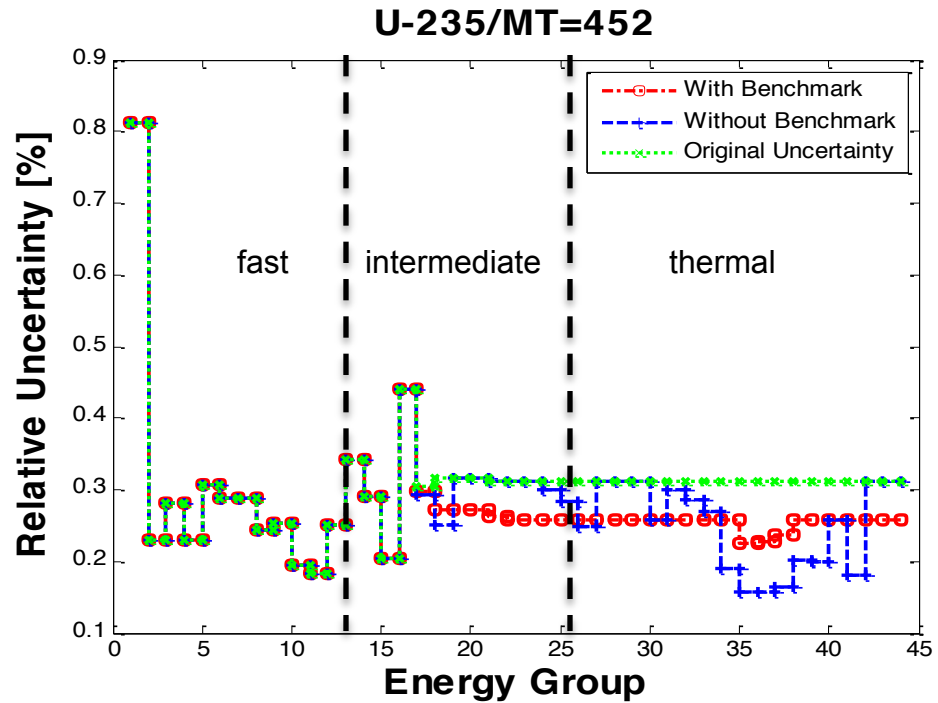
- So far, the cost of a differential experiment has been assumed to be inversely proportional with the uncertainty in the differential data
- A realistic cost function would account for
 - duration of measurements
 - Needed to run the facility, pay the staff, etc.
 - Inversely proportional to the cross section
 - Smaller cross section requires longer run times
 - Cost of the target
 - manufactured or borrowed?
 - In collaboration with Klaus Guber we are devising more realistic cost functions

Inverse S/U Results



Required relative uncertainties (benchmark vs. no benchmark) for neutron capture cross section (i.e. MT=102) for U-235 (left) and for U-238 (right). The plots show that inclusion of a benchmark affords less stringent uncertainties

Inverse S/U Results



For U-235 neutron yield (MT=452) extant uncertainties (green) are already near (or smaller than) the ENDF guidance value of 0.3%. Here too, the IS/U with integral benchmark experiment (IBE) (red) require uncertainties that are not as small as those w/o IBEs (blue)

Summary

- A new application of the Inverse Sensitivity/ Uncertainty to cost-optimized prioritization of nuclear data measurements
- Demonstrated the benefit of using integral benchmarks in the IS/U
 - Without integral benchmark experiments differential data uncertainties may be unachievable
- IS/U capability can be used for various nuclear fuel cycle applications



Outlook

- Formalism sufficiently general to minimize the TOTAL cost of data
 - Differential data and integral benchmark experiments simultaneously
 - Can be adapted to optimize systematic and statistical uncertainties simultaneously
 - It may be extended to optimize and design integral benchmark experiment
- Complexity reduction methods developed by Hany Abdel-Khalik are being applied to decrease the computational load for more complex responses



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