

***QUALIFICATION OF THE JEF2.2 CROSS-SECTIONS  
IN THE EPITHERMAL AND THERMAL RANGES  
USING A STATISTICAL APPROACH***

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**BUT** : *Current cross-sections do not satisfy safety design parameter accuracy requirements*

**For Example**

- ◆ +/- 600 pcm on  $K_{\text{eff}}$  for PWR-UO<sub>2</sub> lattice
- ◆ +/- 1000 pcm on  $K_{\text{eff}}$  for PWR-MOx lattice

**Due to Cross-Sections Uncertainties**



- Physicists built Specific Integral Experiments (fundamental or mock-up types) to measure Neutronic Parameters with improved accuracies : for example  $\pm 300$  pcm ( $1\sigma$ ) on  $K_{\text{eff}}$  or  $\pm 1\%$  ( $1\sigma$ ) on fission rate distributions

⇒ A Statistical Approach is used to combine informations coming from these integral experiments and those coming from microscopic cross-section measurements (traditionnaly used for fast reac-tors libraries but not for THERMAL reactors)

Maximum Likelihood Principle  
and the BAYES Theorem

➤ Try to use this statistical technique to qualify thermal cross-section libraries based on the JEF2.2 basic nuclear data set.

- $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ ,  $^{241}\text{Pu}$ ,  $^{242}\text{Pu}$ ,  $^{16}\text{O}$
- Natural Zr,  $^{56}\text{Fe}$ ,  $^{58}\text{Ni}$ ,  $^{52}\text{Cr}$ ,  $^{27}\text{Al}$
- $^{10}\text{B}$ , Natural Gd
- $^{12}\text{C}$ ,  $\text{H}_2\text{O}$
- Capture, Fission,  $\nu$ , elastic and inelastic

➤ *Data Needed to apply this statistical approach*

- Measurement of Fundamental Neutronic Parameters
- Variance/covariance Matrix relative to these Experiments
- Sensitivity Coefficients Matrix of the integral parameters to the cross-sections.
- Variance/covariance matrix relative to the cross-sections



## Analyzed Integral Experiments

- 4 International Experimental Benchmarks
  - TRX-1 ; TRX-2 ; ORNL and PNL spheres
- 10  $UO_2$  Experiments
  - EPICURE-1 ; CAMELEON ; DIMPLE ; VVER and BNL Lattices
- 9  $UPuO_2$  Experiments
  - ERASME ; JAERI ; EPICURE-2
- 1 Spent fuel analysis
  - SHERWOOD

↙ 23  $K_{eff}$

↙ 27 Spectral indices

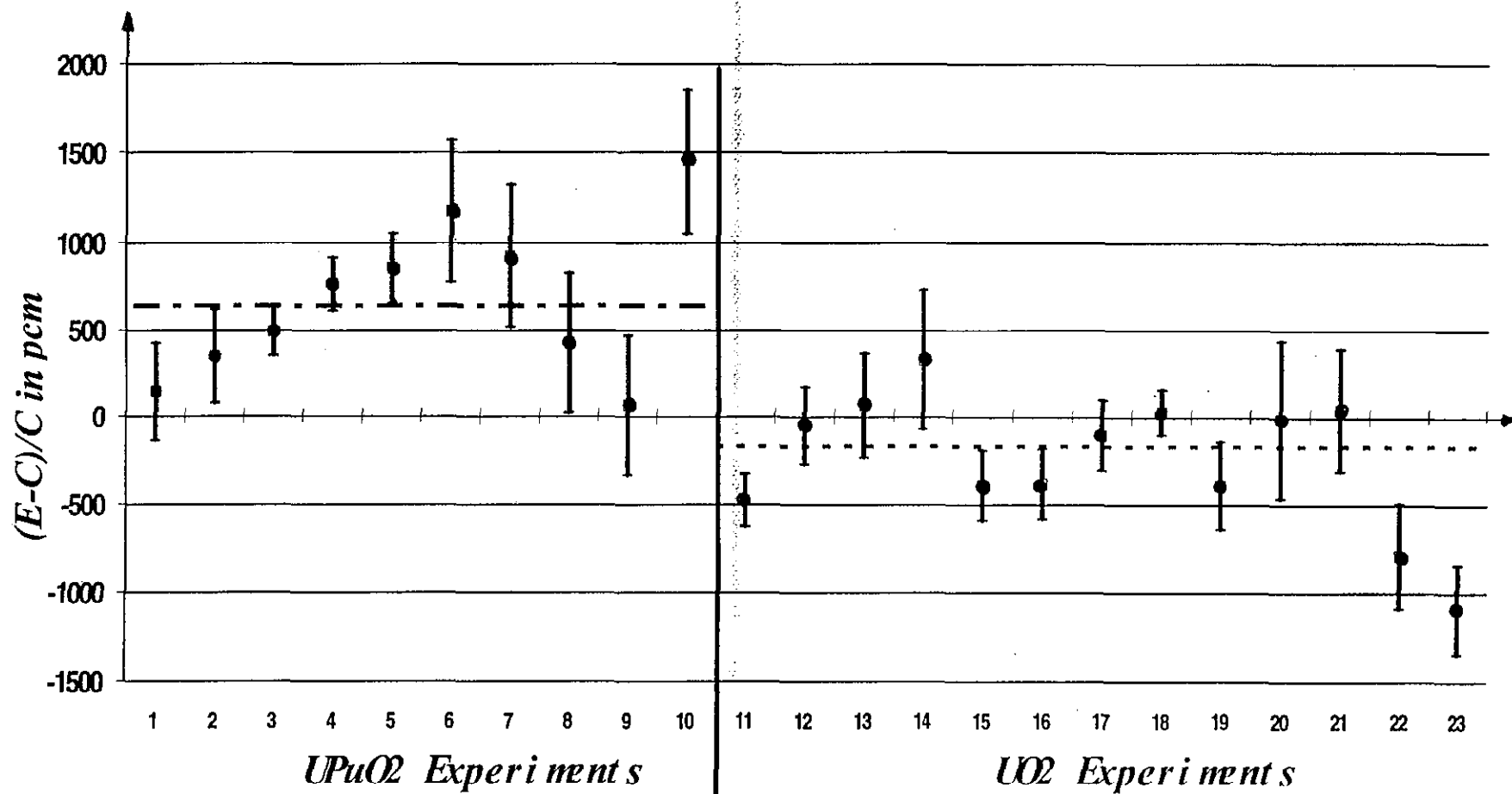
## Results of the Adjustments

- ***A Priori Dispersion Factor***  $\chi^2 = 5.00$
- ***A Posteriori Dispersion Factor***  $\chi^2 = 0.95$

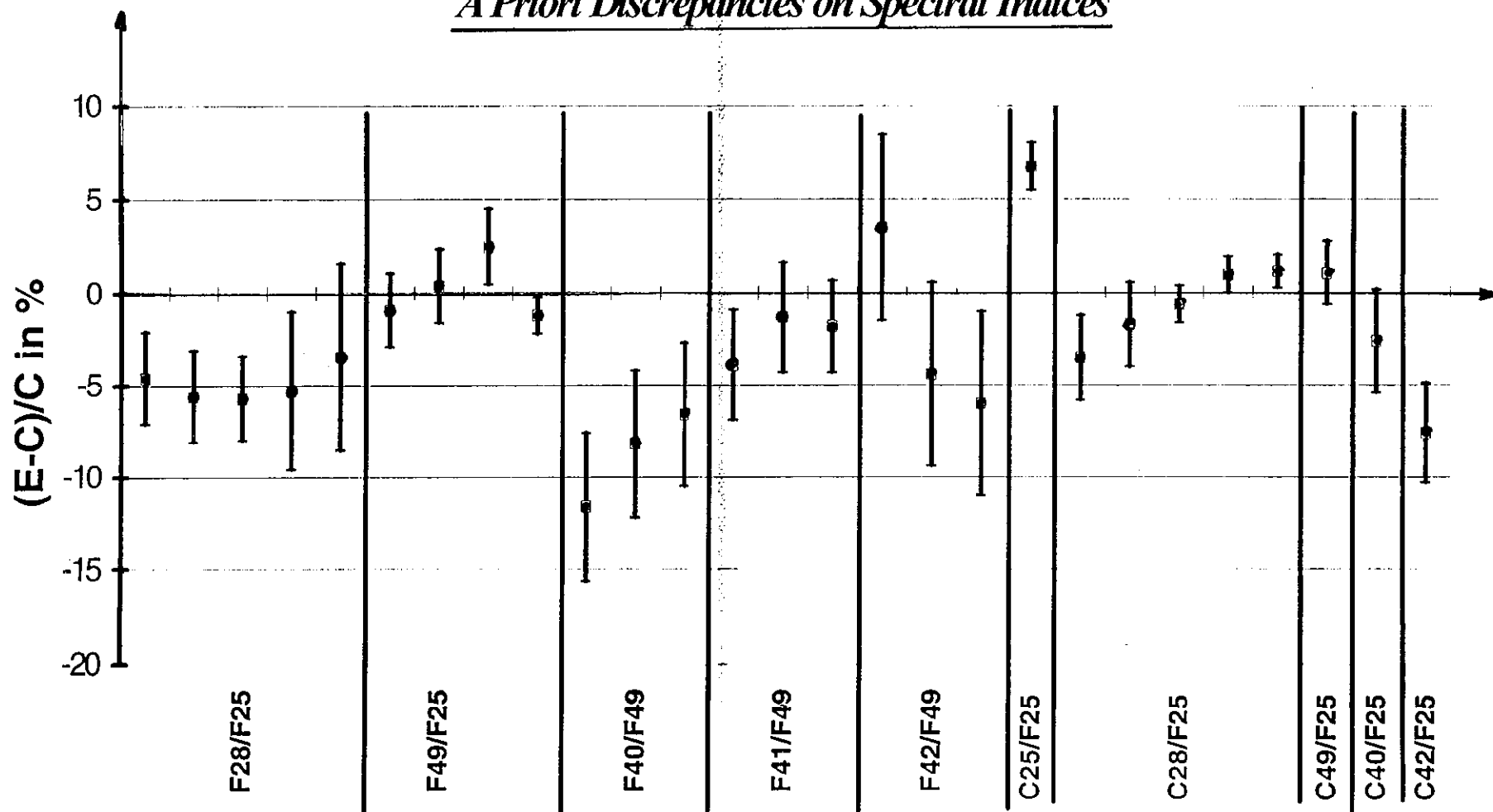
↙ ***Consistent with the statistical enhancement factor, which must be :***

$$1 - \sqrt{\frac{2}{N}} \leq \chi^2 \leq 1 + \sqrt{\frac{2}{N}}$$

*A priori Discrepancies on  $K_{eff}$*

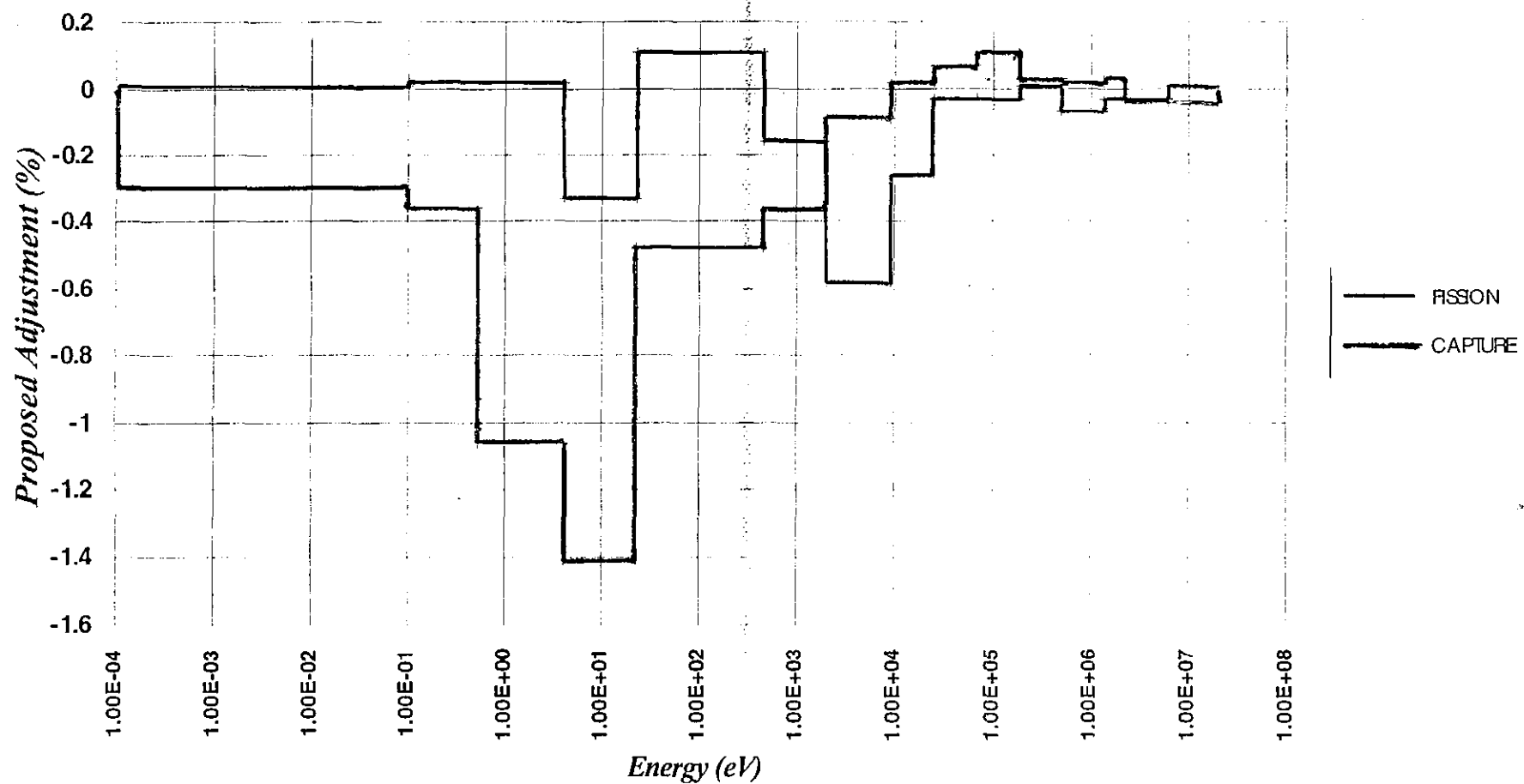


*A Priori Discrepancies on Spectral Indices*



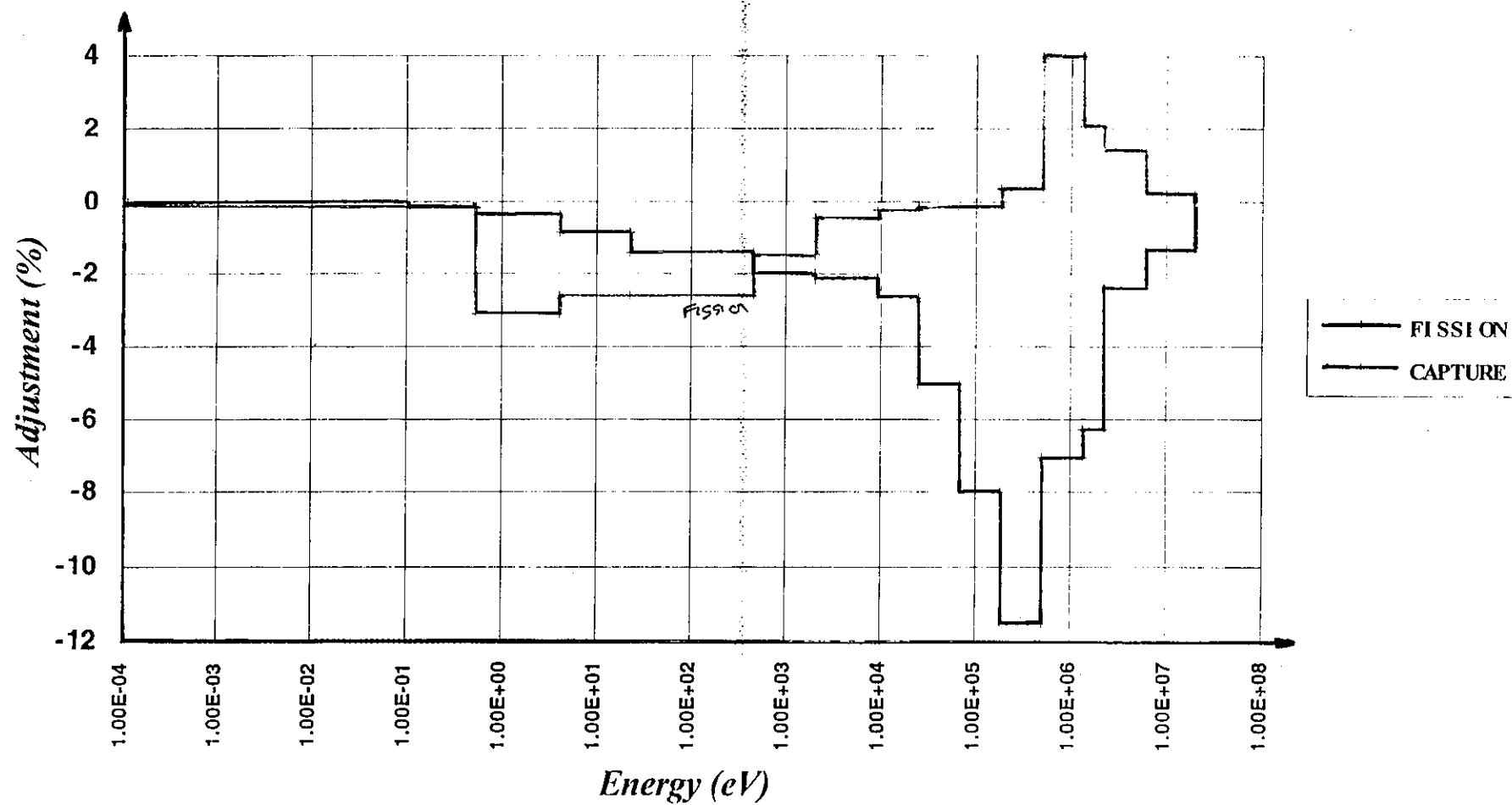


# Cross-Sections of $^{239}\text{Pu}$



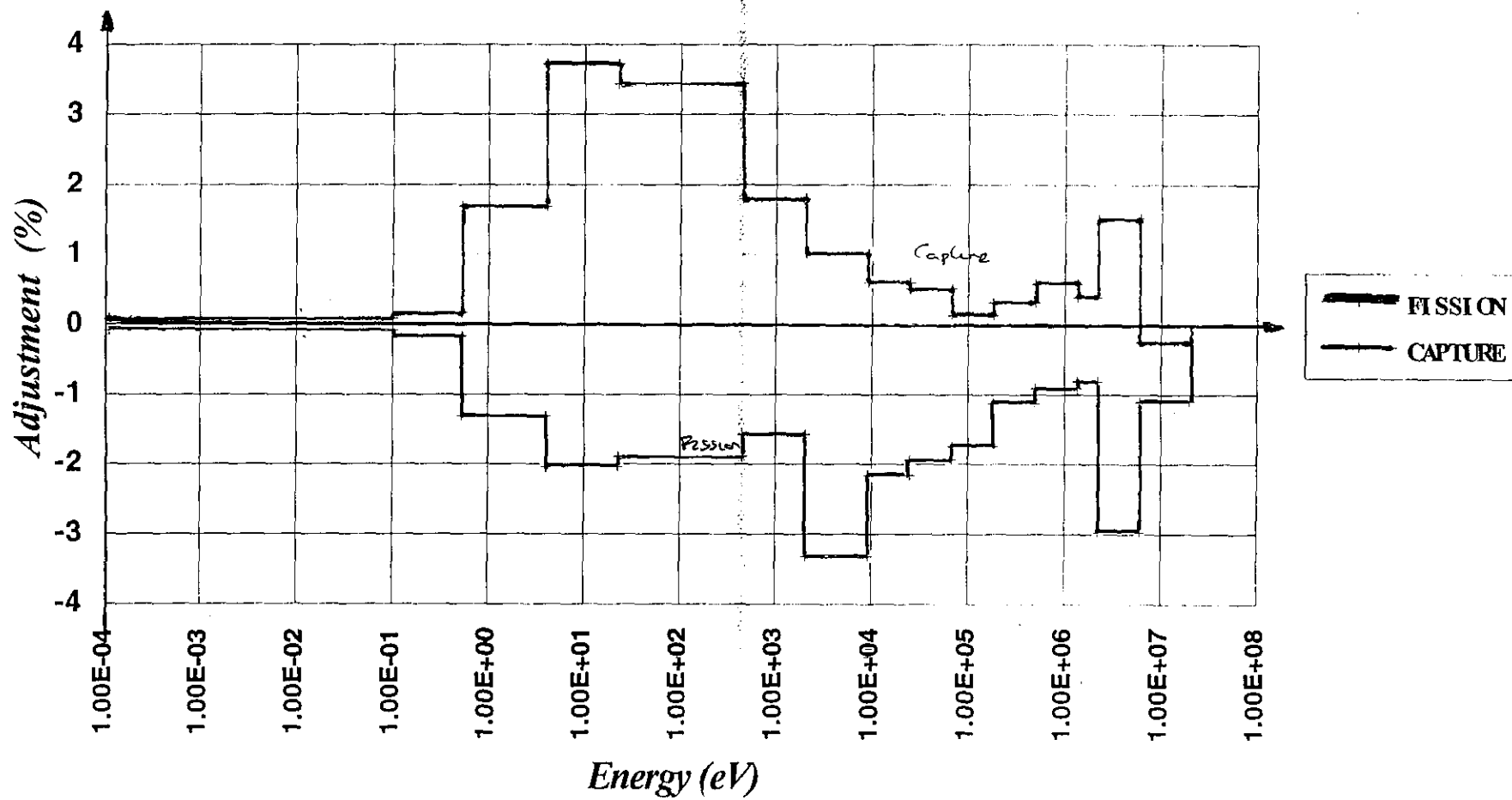


### Cross-Section of $^{240}\text{Pu}$

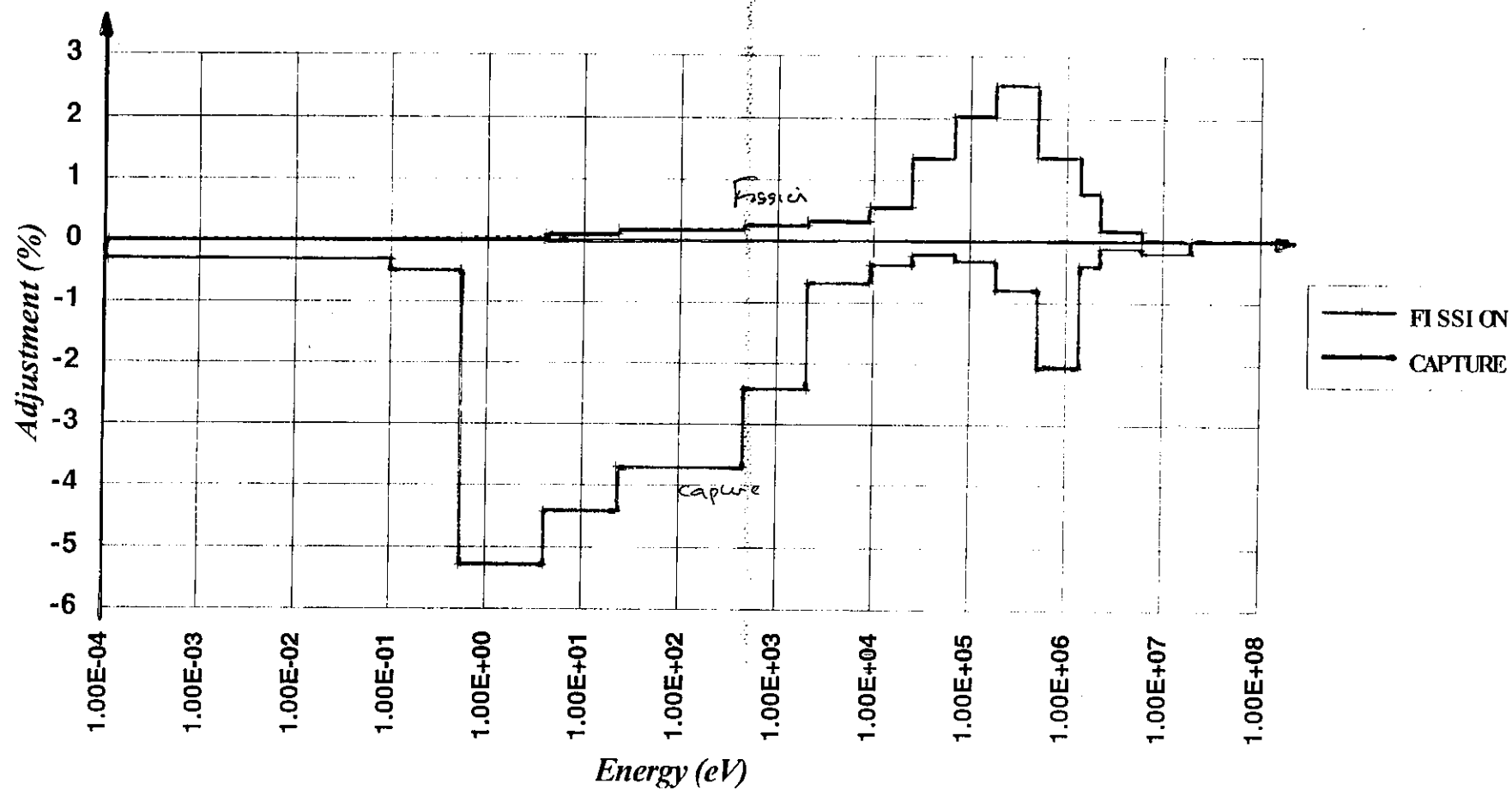




### Cross-Sections of $^{241}\text{Pu}$

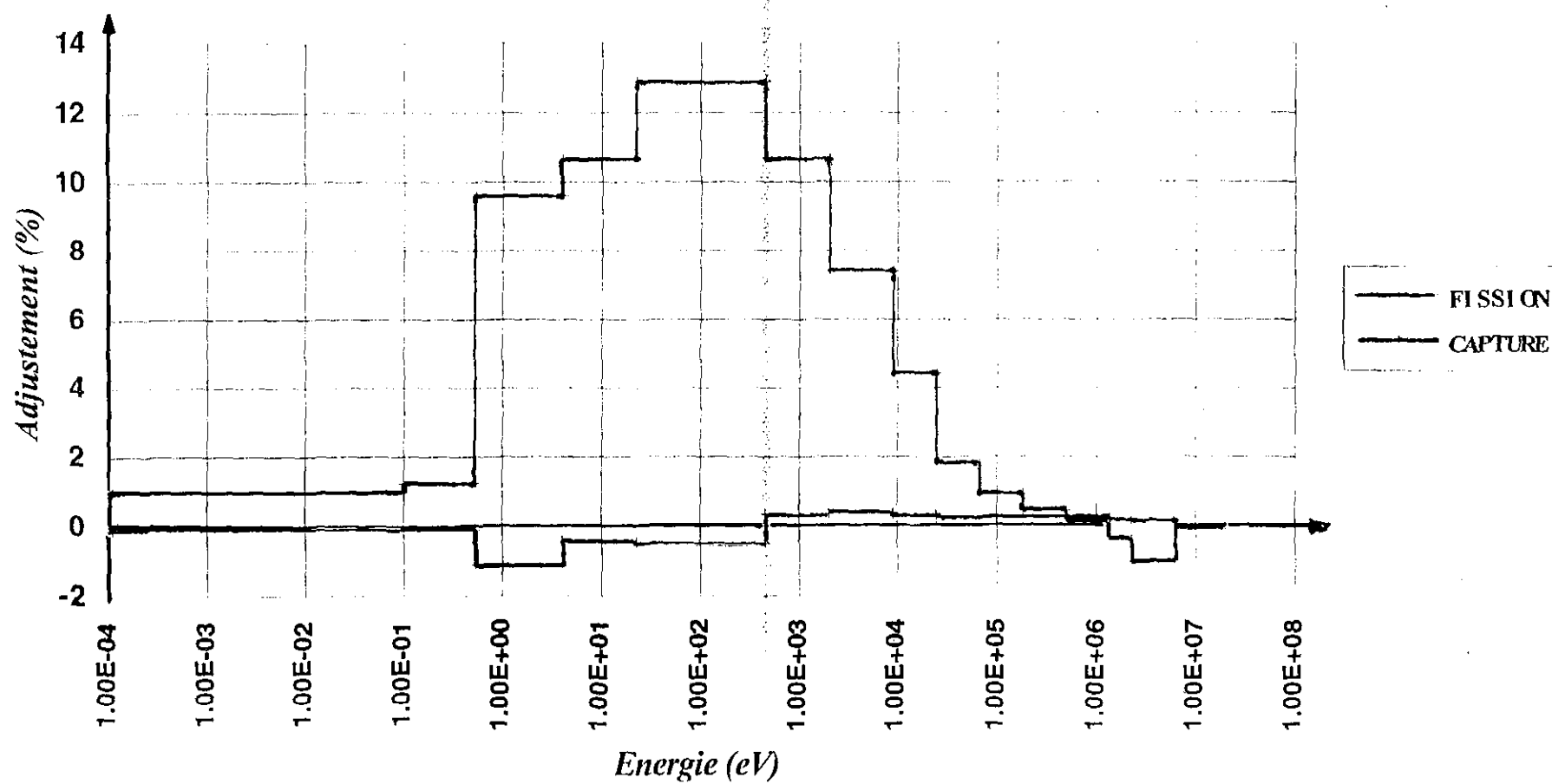


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Cross-Section of  $^{242}\text{Pu}$ 

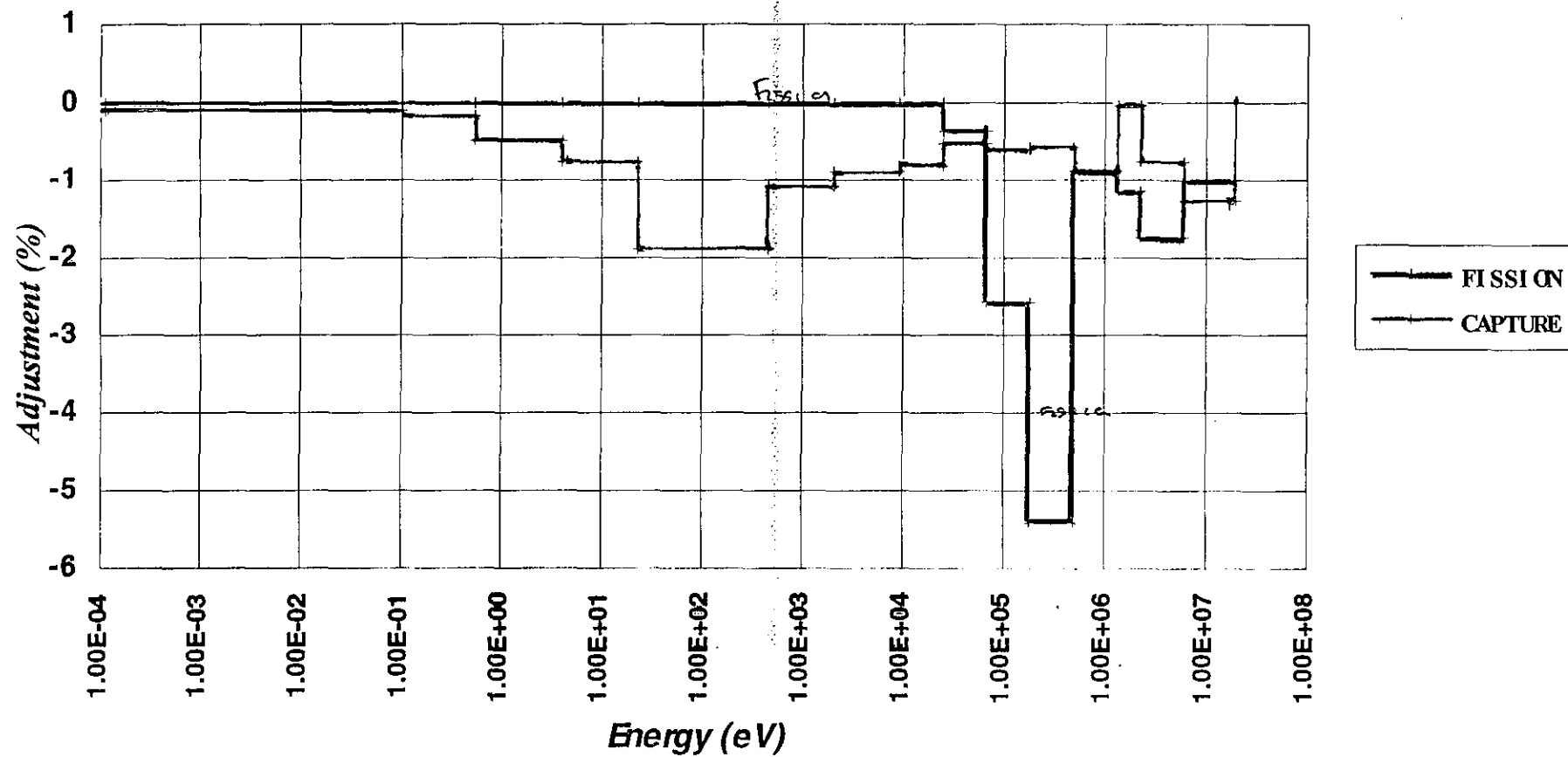


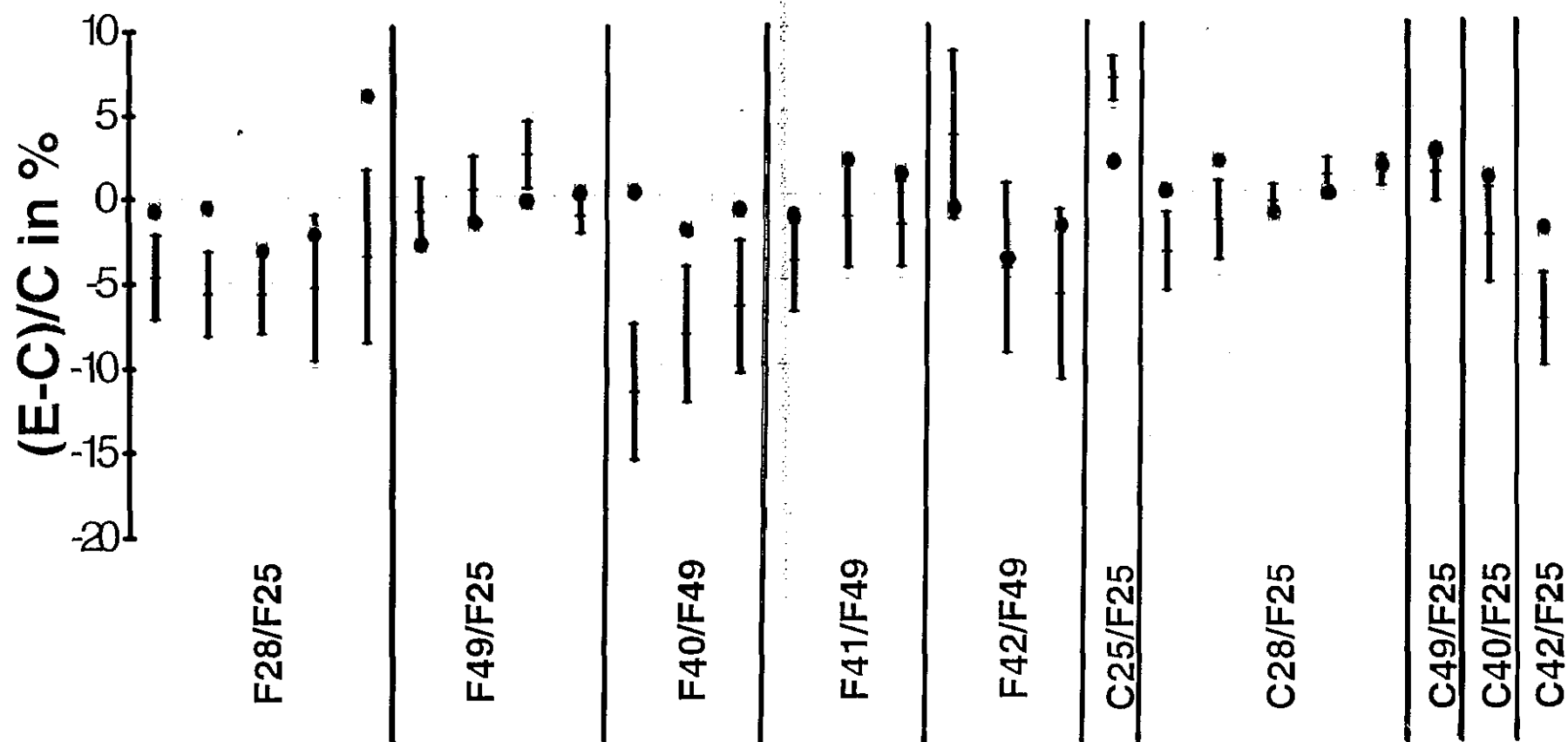
### Cross-Sections of $^{235}\text{U}$



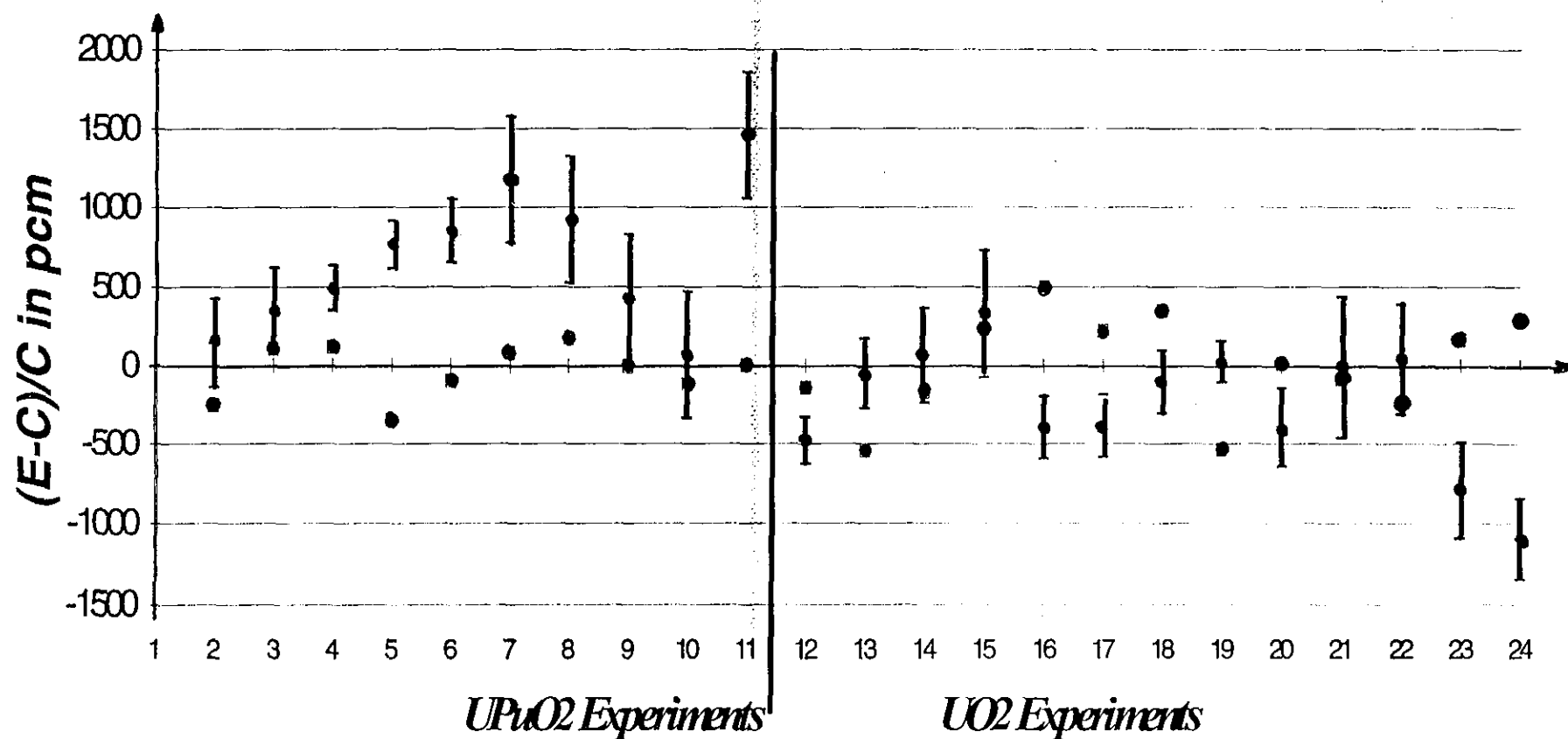
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### Cross-Sections of $^{238}\text{U}$



*A Posteriori Discrepancies on Spectral Indices*

# *A Posteriori Discrepancies on $K_{eff}$*







## Synthesis of the adjustments (1)

### ↙ $^{239}\text{Pu}$

- No significant trend except for a slight decrease (1.5%) of the Capture in the resonance range

### ↙ $^{240}\text{Pu}$

- Large decrease of the fission (11%) and slight decrease of Capture (3.5%) in the first resonance at 1.054 eV.

### ↙ $^{241}\text{Pu}$

- Slight decrease of the fission (3%) and increase (2%) of capture above 0.5 eV.

### ↙ $^{242}\text{Pu}$

- Large decrease (5%) of the capture in the first resonance at 2.67 eV

### ↙ $^{238}\text{U}$

- Large decrease of the fission near the threshold (weighting flux problems)

## Synthesis of the adjutments (2)

### ↳ $^{235}\text{U}$ (JEF2.2 and ENDF-BVI)

- Fission very wellknown but very large increase (up to 12 % !) of the capture cross-section in the resonance energy range.  
⇒ Self-shielding calculations in the APOLLO-2 code (resonance overlapping effect for example)
- ⇒ Evaluation : Mean capture width of around  $\Gamma_\gamma = 33$  meV was used where the usually accepted value is  $\Gamma_\gamma = 37 \pm 2$  meV. The discrepancy is about the same than the recommended adjustment

⇒ **NEW EVALUATION ?**